

Material Input Data:

Youngs-Modulus E	$E_Modulus := 72000 \cdot \text{MPa}$
Tensile Yield strength Rp0,2	$\sigma_Rp02 := 130 \cdot \text{MPa}$
Tensile strength Rm	$\sigma_Rm := 240 \cdot \text{MPa}$
Tensile elongation at Rm	$\epsilon_Rm := 1 \cdot \%$

Calculation:

	$\epsilon_sigma_Rp02 := \frac{\sigma_Rp02}{E_Modulus} + 0.002$	$\epsilon_sigma_Rp02 = 0.381 \cdot \%$
Tensile elongation at yield strength	$T_Modulus := \frac{(\sigma_Rm - \sigma_Rp02)}{(\epsilon_Rm - \epsilon_sigma_Rp02)}$	$T_Modulus = 1.776 \times 10^4 \cdot \text{MPa}$
Tangentmodulus T	$\sigma0_Tang := \sigma_Rm - T_Modulus \cdot \epsilon_Rm$	$\sigma0_Tang = 62.422 \cdot \text{MPa}$
Cross point of tangent at ordinate	$\epsilon_Yield_Strength := \frac{\sigma0_Tang}{E_Modulus - T_Modulus}$	$\epsilon_Yield_Strength = 0.1151 \cdot \%$
Cross point tangent to Hooke's curve	$\sigma_Yield_Strength := E_Modulus \cdot \epsilon_Yield_Strength$	$\sigma_Yield_Strength = 82.857 \cdot \text{MPa}$

Output Data for Ansys: (bilinear kinematic hardening)

$\sigma_Yield_Strength = 83 \cdot \text{MPa}$
$T_Modulus = 18 \cdot \text{GPa}$

Index for elongation:

$$\text{imax} := \varepsilon_{\text{Rm}} \cdot 100000 \qquad \text{imax} = 1000$$

$$i := 1 \dots \text{imax}$$

$$\varepsilon_{\text{bilinear}_i} := \frac{i}{100000}$$

$$f0 := 1$$

$$f1 := \text{ceil}(\varepsilon_{\text{Yield_Strength}} \cdot 100000 - 0.5) \qquad f1 = 115$$

$$f2 := \text{imax}$$

$$\sigma := \left[\begin{array}{l} \text{for } i \in f0 \dots f1 \\ \quad m_i \leftarrow E_{\text{Modulus}} \cdot \varepsilon_{\text{bilinear}_i} \\ \text{for } i \in (f1 + 1) \dots f2 \\ \quad m_i \leftarrow \sigma_{0_Tang} + T_{\text{Modulus}} \cdot \varepsilon_{\text{bilinear}_i} \\ m \end{array} \right]$$

$$\sigma_{f1} = 82.8 \cdot \text{MPa}$$

$$\sigma_{\text{Yield_Strength}} = 82.857 \cdot \text{MPa}$$

$$\sigma_{\text{imax}} = 240 \cdot \text{MPa}$$

$$\sigma_{\text{Rm}} = 240 \cdot \text{MPa}$$

$$\varepsilon_{\text{bilinear}_{f1}} = 0.115 \cdot \%$$

$$\varepsilon_{\text{Yield_Strength}} = 0.115 \cdot \%$$

$$\varepsilon_{\text{bilinear}_{\text{imax}}} = 1 \cdot \%$$

$$\varepsilon_{\text{Rm}} = 1 \cdot \%$$

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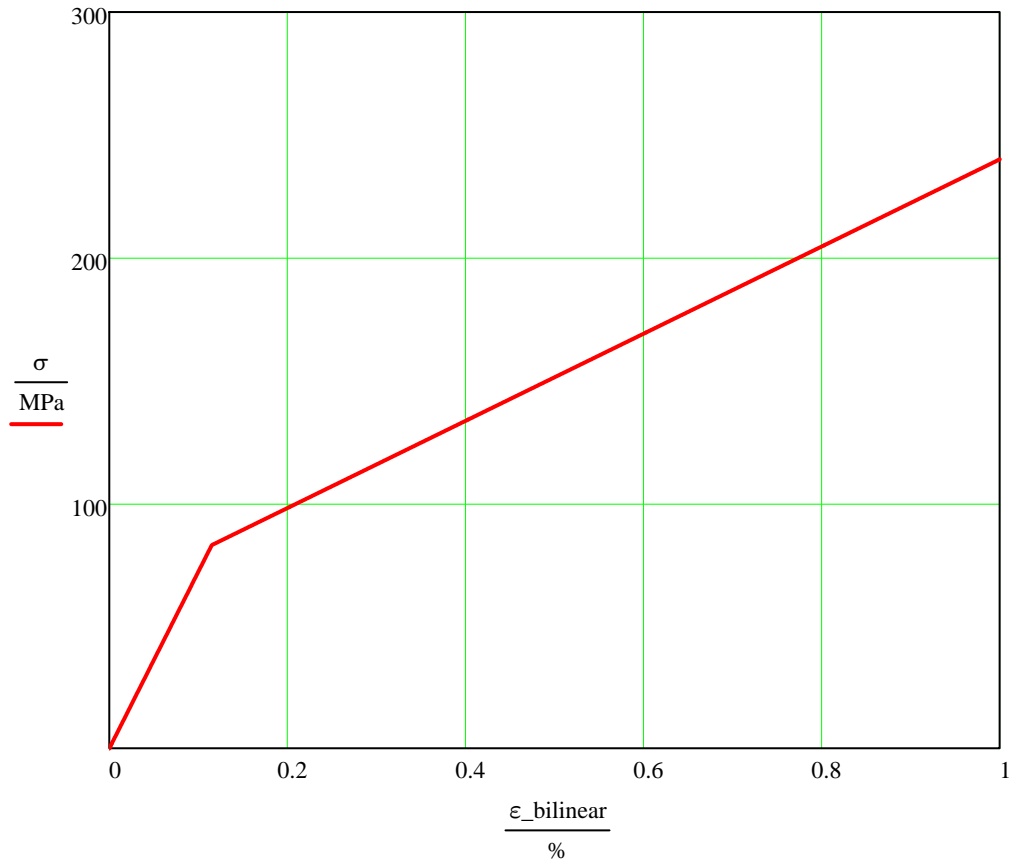
$$\varepsilon_{\text{Rm}} = 1 \cdot \%$$

$$\sigma_{f1} = 82$$

$$\sigma_{\text{imax}} =$$

$$\varepsilon_{\text{bilinear}}$$

$$\varepsilon_{\text{bilinear}}$$



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elongation:

$$\begin{aligned} \text{imax} &:= \varepsilon_{\text{Rm}} \cdot 100000 & \text{imax} &= 1000 \\ i &:= 1 \dots \text{imax} \\ \varepsilon_{\text{bilinear}_i} &:= \frac{i}{100000} \end{aligned}$$

$$\begin{aligned} f0 &:= 1 \\ f1 &:= \text{ceil}(\varepsilon_{\text{Yield_Strength}} \cdot 100000 - 0.5) & f1 &= 115 \\ f2 &:= \text{imax} \end{aligned}$$

$$\sigma := \left[\begin{array}{l} \text{for } i \in f0 \dots f1 \\ \quad m_i \leftarrow E_{\text{Modulus}} \cdot \varepsilon_{\text{bilinear}_i} \\ \text{for } i \in (f1 + 1) \dots f2 \\ \quad m_i \leftarrow \sigma_{0_Tang} + T_{\text{Modulus}} \cdot \varepsilon_{\text{bilinear}_i} \\ m \end{array} \right]$$

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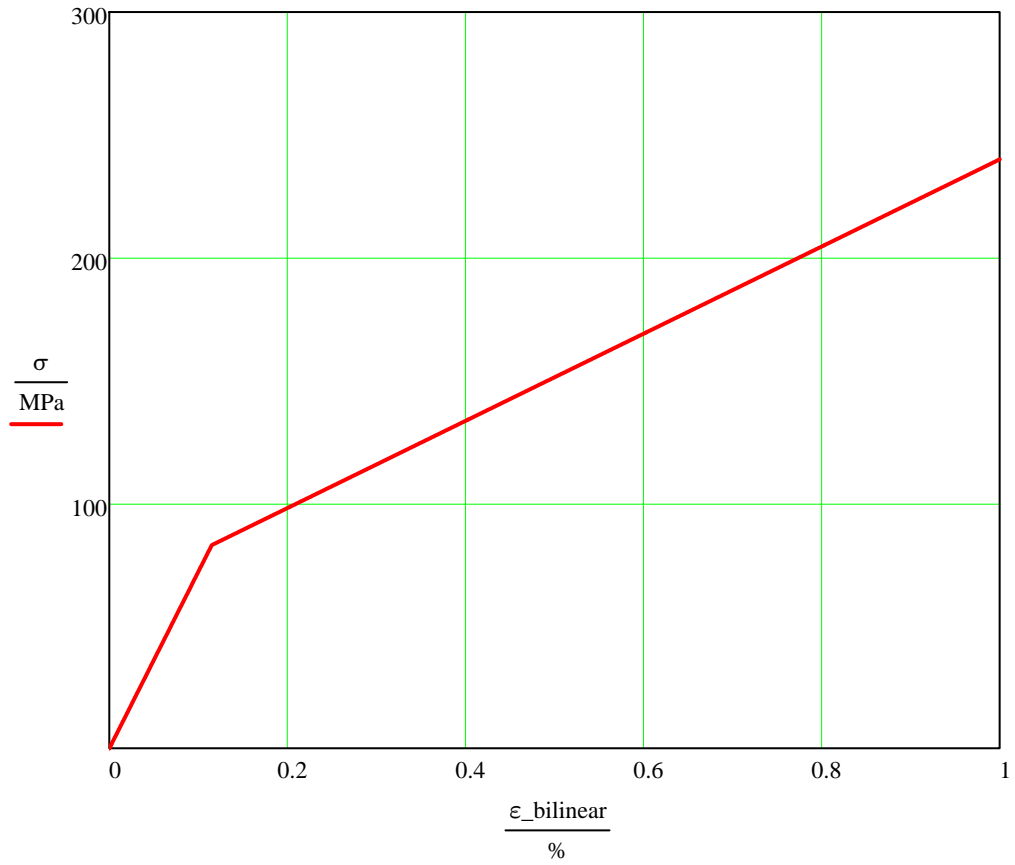
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