

$$\begin{aligned}
& \ln \left[\exp \left(-\frac{t}{\tau_{\text{flow}}} \right) \cdot \left[\frac{\text{fr} * \text{Lasheat} * \tan(\phi) * (1 + \cos(\phi) * \sin(\omega * t - \phi))}{\tau_{\text{cool}} * \omega} + \frac{T_0_{\text{gas}}}{\tau_{\text{flow}}} \right] \right] \quad \text{simplify} \\
& \quad \text{assume, All real} \rightarrow 0 \\
& \quad \text{assume, } 0 < \phi < \pi \\
\\
& \operatorname{Re} \left[\exp \left(-\frac{t}{\tau_{\text{flow}}} \right) \cdot \left[\frac{\text{fr} * \text{Lasheat} * \tan(\phi) * (1 + \cos(\phi) * \sin(\omega * t - \phi))}{\tau_{\text{cool}} * \omega} + \frac{T_0_{\text{gas}}}{\tau_{\text{flow}}} \right] \right] \quad \text{simplify} \\
& \quad \text{assume, All real} \rightarrow \frac{\frac{t}{\tau_{\text{flow}}}}{\text{e}^{-\frac{t}{\tau_{\text{flow}}}} * \left(8 * T_0_{\text{gas}} * \omega * \tau_{\text{cool}} - 2 * \text{Lasheat} * \text{fr} * \tau_{\text{flow}} * \cos(\omega * t) + 8 * T_0_{\text{gas}} * \omega^3 * \tau_{\text{flow}}^2 * \tau_{\text{cool}} - 2 * \text{Lasheat} * \text{fr} * \tau_{\text{flow}} * \cos(4 * \phi - \omega * t) + 2 * \text{Lasheat} * \text{fr} * \tau_{\text{flow}} * \cos(2 * \phi - \omega * t) + 5 * T_0_{\text{gas}} * \omega * \tau_{\text{cool}} * \cos(2 * \phi) - 2 * \text{Lasheat} * \text{fr} * \tau_{\text{flow}}^2 * \sin(\omega * t) + 8 * \text{Lasheat} * \omega^2 * \tau_{\text{flow}}^3 * \sin(2 * \phi) + 8 * T_0_{\text{gas}} * \omega^3 * \tau_{\text{flow}}^2 * \tau_{\text{cool}} * \cos(2 * \phi) - 2 * \text{Lasheat} * \omega * \text{fr} * \tau_{\text{flow}}^2 * \sin(2 * \phi + \omega * t) - 2 * \text{Lasheat} * \omega * \text{fr} * \tau_{\text{flow}}^2 * \sin(4 * \phi - \omega * t) \right)}{8 * \omega * \tau_{\text{cool}} + 8 * \omega^3 * \tau_{\text{flow}}^2 * \tau_{\text{cool}} * \cos(2 * \phi) + 8 * \omega^3 * \tau_{\text{flow}}^2 * \tau_{\text{cool}} * \cos(2 * \phi)} \\
\\
& \int \exp \left(-\frac{t}{\tau_{\text{flow}}} \right) \cdot \left[\frac{\text{fr} * \text{Lasheat} * \tan(\phi) * (1 + \cos(\phi) * \sin(\omega * t - \phi))}{\tau_{\text{cool}} * \omega} + \frac{T_0_{\text{gas}}}{\tau_{\text{flow}}} \right] dt \quad \text{simplify} \\
& \quad \text{assume, All real} \rightarrow \frac{\frac{t}{\tau_{\text{flow}}}}{\text{e}^{-\frac{t}{\tau_{\text{flow}}}} * \left(4 * T_0_{\text{gas}} * \omega * \tau_{\text{cool}} - \text{Lasheat} * \text{fr} * \tau_{\text{flow}} * \cos(\omega * t) + 4 * T_0_{\text{gas}} * \omega^3 * \tau_{\text{flow}}^2 * \tau_{\text{cool}} - \text{Lasheat} * \text{fr} * \tau_{\text{flow}} * \cos(2 * \phi + \omega * t) + \text{Lasheat} * \text{fr} * \tau_{\text{flow}} * \cos(2 * \phi - \omega * t) + \text{Lasheat} * \text{fr} * \tau_{\text{flow}} * \sin(2 * \phi - \omega * t) + 4 * \text{Lasheat} * \text{fr} * \tau_{\text{flow}} * \sin(2 * \phi) + 4 * T_0_{\text{gas}} * \omega * \tau_{\text{cool}} * \cos(2 * \phi) - \text{Lasheat} * \omega * \text{fr} * \tau_{\text{flow}}^2 * \cos(\omega * t) + 4 * \text{Lasheat} * \omega^2 * \text{fr} * \tau_{\text{flow}}^3 * \sin(2 * \phi) + 4 * T_0_{\text{gas}} * \omega^3 * \tau_{\text{flow}}^2 * \tau_{\text{cool}} * \cos(2 * \phi) + \text{Lasheat} * \omega * \text{fr} * \tau_{\text{flow}}^2 * \sin(2 * \phi + \omega * t) - \text{Lasheat} * \omega * \text{fr} * \tau_{\text{flow}}^2 * \sin(4 * \phi - \omega * t) \right)}{4 * \omega * \tau_{\text{cool}} * \left(\omega^2 * \tau_{\text{flow}}^2 + 1 \right) * (\cos(2 * \phi) + 1 + \sin(2 * \phi) * i)} \\
\\
& \int \exp \left(-\frac{t}{\tau_{\text{flow}}} \right) \cdot \left[\frac{8 * \text{Lasheat} * \tan(\phi) * (1 + \cos(\phi) * \sin(\omega * t - \phi))}{\tau_{\text{cool}} * \omega} + \frac{T_0_{\text{gas}}}{\tau_{\text{flow}}} \right] dt \quad \text{simplify} \\
& \quad \text{assume, All real} \rightarrow \frac{\frac{t}{\tau_{\text{flow}}}}{\text{e}^{-\frac{t}{\tau_{\text{flow}}}} * \left(4 * T_0_{\text{gas}} * \omega * \tau_{\text{cool}} - \text{Lasheat} * \text{fr} * \tau_{\text{flow}} * \cos(\omega * t) + 4 * T_0_{\text{gas}} * \omega^3 * \tau_{\text{flow}}^2 * \tau_{\text{cool}} - \text{Lasheat} * \text{fr} * \tau_{\text{flow}} * \cos(2 * \phi + \omega * t) + \text{Lasheat} * \text{fr} * \tau_{\text{flow}} * \cos(2 * \phi - \omega * t) + 4 * \text{Lasheat} * \text{fr} * \tau_{\text{flow}} * \sin(2 * \phi) + 4 * T_0_{\text{gas}} * \omega * \tau_{\text{cool}} * \cos(2 * \phi) - \text{Lasheat} * \omega * \text{fr} * \tau_{\text{flow}}^2 * \sin(\omega * t) + 4 * \text{Lasheat} * \omega^2 * \text{fr} * \tau_{\text{flow}}^3 * \sin(2 * \phi) + 4 * T_0_{\text{gas}} * \omega^3 * \tau_{\text{flow}}^2 * \tau_{\text{cool}} * \cos(2 * \phi) - \text{Lasheat} * \omega * \text{fr} * \tau_{\text{flow}}^2 * \sin(2 * \phi + \omega * t) - \text{Lasheat} * \omega * \text{fr} * \tau_{\text{flow}}^2 * \sin(4 * \phi - \omega * t) \right)}{4 * \omega * \tau_{\text{cool}} * \left(\omega^2 * \tau_{\text{flow}}^2 + 1 \right) * (\cos(2 * \phi) + 1)} \\
\\
& \quad \text{rectangular}
\end{aligned}$$

$$\sin(2\phi - \omega t) - \text{Lasheat} \cdot \omega \cdot f_r \cdot \tau_{\text{flow}}^2 \cdot \sin(4\phi - \omega t) + \text{Lasheat} \cdot f_r \cdot \tau_{\text{flow}}^3 \cdot \cos(2\phi) - \text{Lasheat} \cdot \omega \cdot f_r \cdot \tau_{\text{flow}}^2 \cdot \cos(2\phi - \omega t) + i - \text{Lasheat} \cdot f_r \cdot \tau_{\text{flow}} \cdot \sin(2\phi + \omega t) + i + 4f_r T_0 \cdot \omega \cdot \tau_{\text{cool}} \cdot \sin(2\phi) + 4f_r \text{Lasheat} \cdot \omega^2 \cdot f_r \cdot \tau_{\text{flow}}^3 + \text{Lasheat} \cdot f_r \cdot \tau_{\text{flow}} \cdot \sin(\omega t) + i + 4f_r \text{Lasheat} \cdot f_r \cdot \tau_{\text{flow}} + 4f_r T_0 \cdot \omega^3 \cdot \tau_{\text{flow}}^2 \cdot \tau_{\text{cool}} \cdot \sin(2\phi) + \text{Lasheat} \cdot \omega \cdot f_r \cdot \tau_{\text{flow}}^2 \cdot \cos(2\phi + \omega t) + i \Big)$$