

## 2

# LINEAR ACTIVE FILTERS LIST

First of all some definitions and a few necessary constants:

$$\text{krad} \equiv 10^3 \cdot \text{rad}, \quad \text{Mrad} \equiv 10^6 \cdot \text{rad},$$

$$\text{Amplifier Gain: } A_0,$$

$$\text{Cut off frequency: } f_0,$$

$$\text{Period: } T_0 = \frac{1}{f_0},$$

$$\text{angular frequency: } \omega_0 = 2 \cdot \pi \cdot f_0,$$

$$\text{time constant: } \tau = \frac{1}{\omega_0}$$

$$\text{Quality factor: } Q,$$

$$\text{damping factor: } \zeta = \frac{\omega_0}{2 \cdot Q},$$

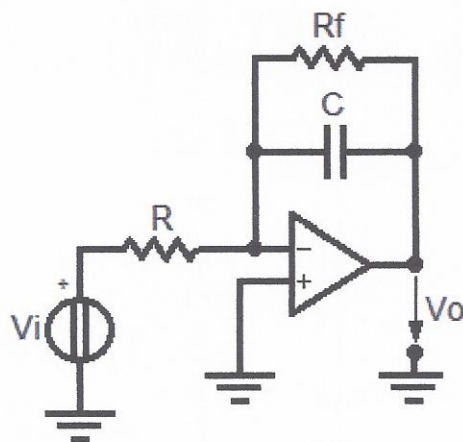
$$\text{sampling frequency: } f_s,$$

$$\text{sampling period: } T_s = \frac{1}{f_s},$$

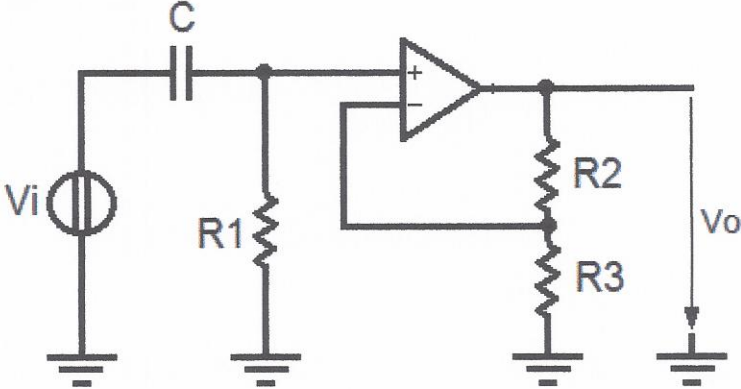
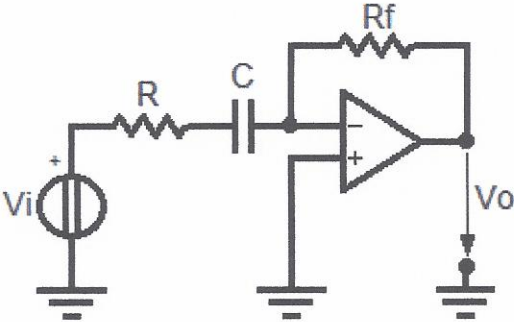
$$\text{sampling angular frequency: } \omega_s = 2 \cdot \pi \cdot f_s.$$

**The eight basic linear active filters transfer functions (t. f.) as Laplace transforms of their impulse responses  $H(t)$ , (functions of the complex frequency  $s=\sigma+j\omega$ ) are:**

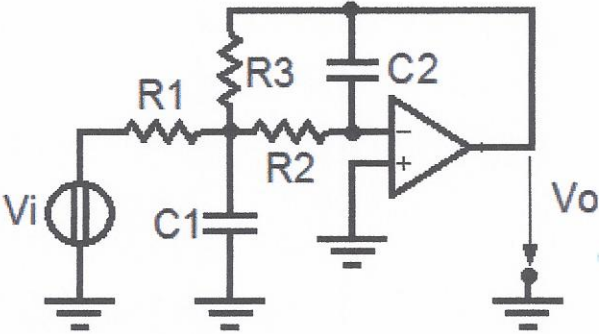
**2.1) Low Pass Filter or inverting integrator (1<sup>o</sup> order):**  $W_1(s) = \frac{A_0 \cdot \omega_0}{s + \omega_0},$



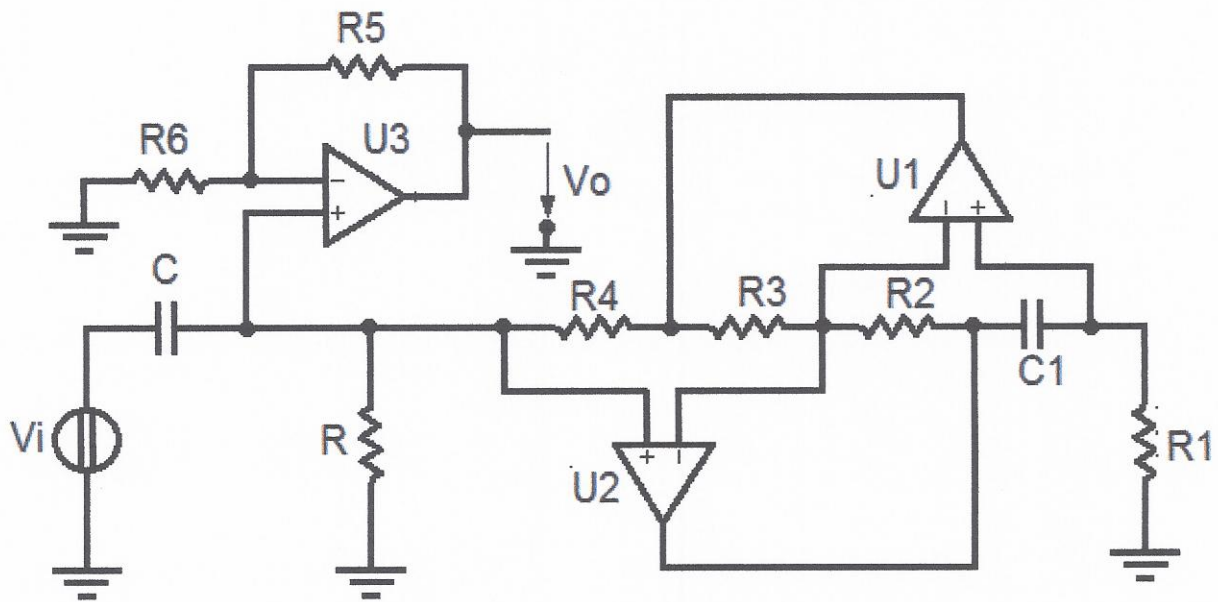
2.2) High Pass or inverting derivator (I° order):  $W2(s) = \frac{A_0 \cdot s}{s + \omega_0}$ ,



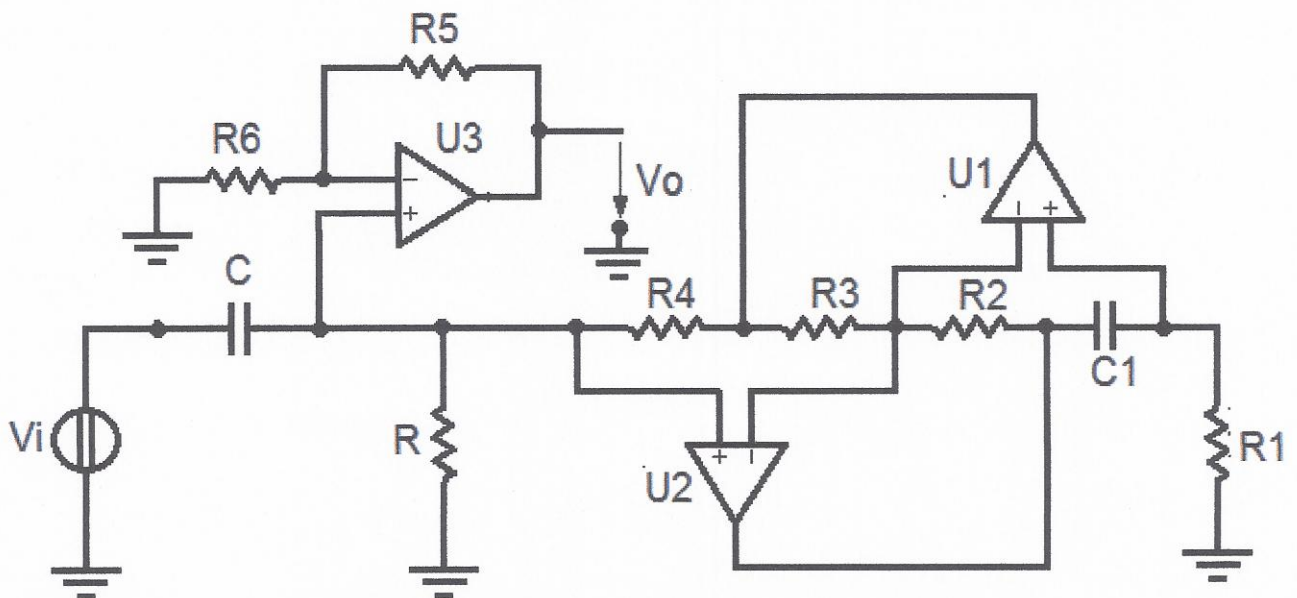
2.3) Low Pass (II° order):  $W3(s) = \frac{A_0 \cdot \omega_0^2}{s^2 + 2 \cdot \zeta \cdot s + \omega_0^2}$ ,



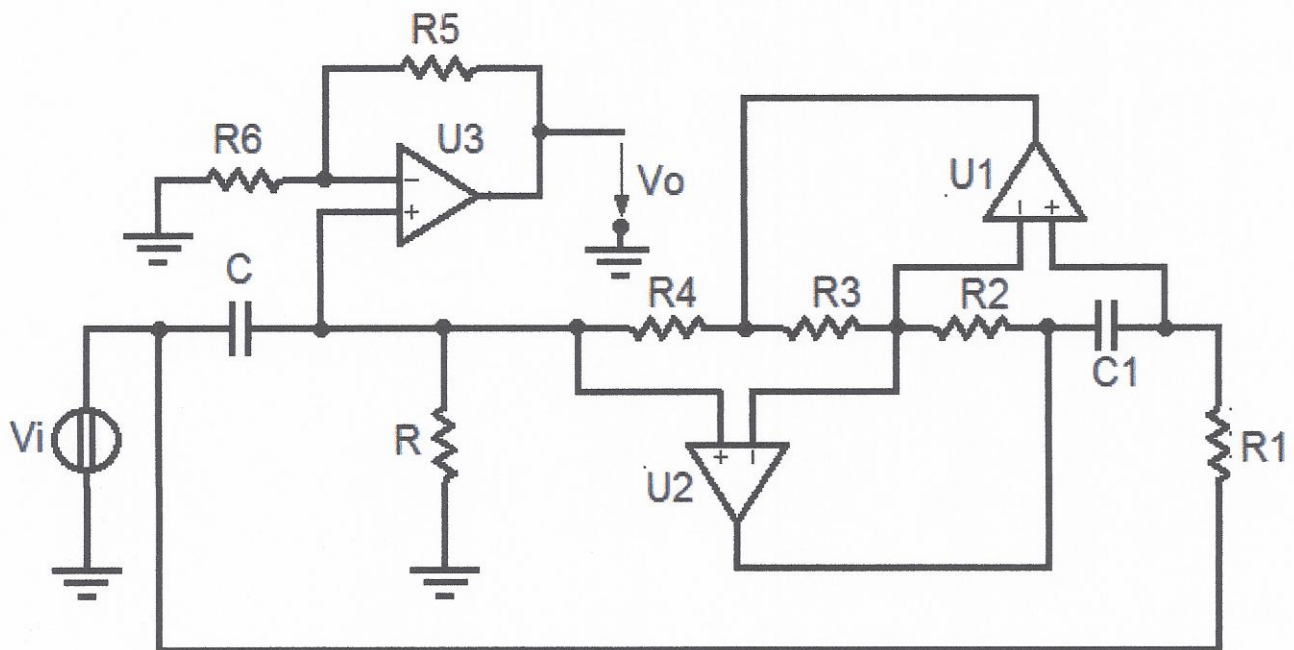
2.4) High Pass (II<sup>o</sup>order):  $W4(s) = \frac{A_0 \cdot s^2}{s^2 + 2 \cdot \zeta \cdot s + \omega_0^2}$ ,



2.5) Band Pass (II<sup>o</sup>order):  $W5(s) = \frac{A_0 \cdot 2 \cdot \zeta \cdot s}{s^2 + 2 \cdot \zeta \cdot s + \omega_0^2}$ ,

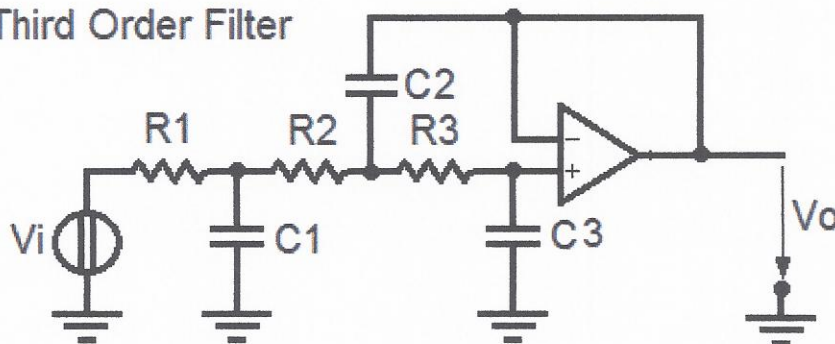


2.6) Band stop (II°order): 
$$W6(s) = \frac{A_0 \cdot (s^2 + \omega_0^2)}{s^2 + 2 \cdot \zeta \cdot s + \omega_0^2}$$



2.7) Butterworth Filter:  $WBw(s) = \frac{A_0}{Bw_n(s)}$ , where we have indicated with  $Bw_n(s)$  the Butterworth polinom of nth grad.

Third Order Filter



**2.8) Chebyshev Filter:**  $W_{Ch}(s) = \frac{A_0}{T_{ch}(s)}$   
 (Starting roll-off, greater than that of Butterworth.)

Fourth order filter

