

# Reaktor-Modell - Veresterung

## Kurzbeschreibung

## Nomenklatur

### Stoffdaten

Molmasse:

Uni. Gaskonstante:

$$M_{N_2} := 28.0135 \frac{gm}{mol}$$

Molmasse N2

$$R := 8.314 \frac{J}{mol K}$$

$$M_A := 102.09 \frac{gm}{mol}$$

Molmasse A = Essigsäureanhydrid

$$M_B := 32.04 \frac{gm}{mol}$$

Molmasse B = Methanol

$$M_C := 74.08 \frac{gm}{mol}$$

Molmasse C = Essigsäuremethylester

$$M_D := 60.06 \frac{gm}{mol}$$

Molmasse D = Essigsäure

kritische Daten:

kritische Temperatur

$$T_{krit\_A} := 606.05 K$$

$$T_{krit\_B} := 513.38 K$$

$$T_{krit\_C} := 506.55 K$$

$$T_{krit\_D} := 591.95 K$$

kritischer Druck

$$p_{krit\_A} := 40 bar$$

$$p_{krit\_B} := 82.16 bar$$

$$p_{krit\_C} := 47.5 bar$$

$$p_{krit\_D} := 57.86 bar$$

kritischer Dichte

$$\rho_{krit\_A} := 352 \frac{kg}{m^3}$$

$$\rho_{krit\_B} := 282 \frac{kg}{m^3}$$

$$\rho_{krit\_C} := 334 \frac{kg}{m^3}$$

$$\rho_{krit\_D} := 325 \frac{kg}{m^3}$$

Dichte:

$$\rho_A(Temp) := \text{linterp} \left( \begin{bmatrix} \vdots \\ 60 \text{ } ^\circ\text{C} \\ \vdots \end{bmatrix}, \begin{bmatrix} \vdots \\ 1081.719 \frac{kg}{m^3} \\ \vdots \end{bmatrix}, Temp \right) \text{ Dichte A}$$

$$\rho_B(Temp) := \text{linterp} \left( \begin{bmatrix} \vdots \\ 0 \text{ } ^\circ\text{C} \\ \vdots \end{bmatrix}, \begin{bmatrix} \vdots \\ 792.033 \frac{kg}{m^3} \\ \vdots \end{bmatrix}, Temp \right) \text{ Dichte B}$$

$$\rho_C(Temp) := \text{linterp} \left( \begin{bmatrix} \vdots \\ 0 \text{ } ^\circ\text{C} \\ \vdots \end{bmatrix}, \begin{bmatrix} \vdots \\ 968.454 \frac{kg}{m^3} \\ \vdots \end{bmatrix}, Temp \right) \text{ Dichte C}$$

$$\rho_D(Temp) := \text{linterp} \left( \begin{bmatrix} \vdots \\ 0 \text{ } ^\circ\text{C} \\ \vdots \end{bmatrix}, \begin{bmatrix} \vdots \\ 1059.282 \frac{kg}{m^3} \\ \vdots \end{bmatrix}, Temp \right) \text{ Dichte D}$$

Verdampfungsenthalpie:

$$\Delta h_{V,A}(Temp) := \text{linterp} \left( \begin{bmatrix} 0 \text{ } ^\circ\text{C} \\ \vdots \end{bmatrix}, \begin{bmatrix} 491852.490 \frac{\text{J}}{\text{kg}} \\ \vdots \end{bmatrix}, Temp \right) \quad \text{Verdampfungsenthalpie A}$$

$$\Delta h_{V,B}(Temp) := \text{linterp} \left( \begin{bmatrix} 0 \text{ } ^\circ\text{C} \\ \vdots \end{bmatrix}, \begin{bmatrix} 1205835.116 \frac{\text{J}}{\text{kg}} \\ \vdots \end{bmatrix}, Temp \right) \quad \text{Verdampfungsenthalpie B}$$

$$\Delta h_{V,C}(Temp) := \text{linterp} \left( \begin{bmatrix} 0 \text{ } ^\circ\text{C} \\ \vdots \end{bmatrix}, \begin{bmatrix} 457174.672 \frac{\text{J}}{\text{kg}} \\ \vdots \end{bmatrix}, Temp \right) \quad \text{Verdampfungsenthalpie C}$$

$$\Delta h_{V,D}(Temp) := \text{linterp} \left( \begin{bmatrix} 0 \text{ } ^\circ\text{C} \\ \vdots \end{bmatrix}, \begin{bmatrix} 393408.254 \frac{\text{J}}{\text{kg}} \\ \vdots \end{bmatrix}, Temp \right) \quad \text{Verdampfungsenthalpie D}$$

## Bildungsenthalpien:

$$\Delta H_{B,A} := \frac{-624400 \frac{\text{J}}{\text{mol}}}{M_A} = -6116172.005 \frac{\text{J}}{\text{kg}} \quad \text{Bildungsenthalpie A}$$

$$\Delta H_{B,B} := \frac{-201000 \frac{\text{J}}{\text{mol}}}{M_B} = -6273408.24 \frac{\text{J}}{\text{kg}} \quad \text{Bildungsenthalpie B}$$

$$\Delta H_{B,C} := \frac{-445900 \frac{\text{J}}{\text{mol}}}{M_C} = -6019168.467 \frac{\text{J}}{\text{kg}} \quad \text{Bildungsenthalpie C}$$

$$\Delta H_{B,D} := \frac{-433000 \frac{\text{J}}{\text{mol}}}{M_D} = -7209457.209 \frac{\text{J}}{\text{kg}} \quad \text{Bildungsenthalpie D}$$

$$\Delta H_{B,N_2} := 0 \frac{\text{J}}{\text{kg}} \quad \text{Bildungsenthalpie N}_2$$

## Wärmekapazität Flüssigkeit:

$$c_{pL,A}(Temp) := \text{linterp} \left( \begin{bmatrix} 0 \text{ } ^\circ\text{C} \\ \vdots \end{bmatrix}, \begin{bmatrix} 1.726 \frac{\text{J}}{\text{gm K}} \\ \vdots \end{bmatrix}, Temp \right) \quad \text{Wärmekapazität A}$$

$$c_{pL,B}(Temp) := \text{linterp} \left( \begin{bmatrix} 0 \text{ } ^\circ\text{C} \\ \vdots \end{bmatrix}, \begin{bmatrix} 2.403 \frac{\text{J}}{\text{gm K}} \\ \vdots \end{bmatrix}, Temp \right) \quad \text{Wärmekapazität B}$$

$$c_{pL,C}(Temp) := \text{linterp} \left( \begin{bmatrix} 0 \text{ } ^\circ\text{C} \\ \vdots \end{bmatrix}, \begin{bmatrix} 1.826 \frac{\text{J}}{\text{gm K}} \\ \vdots \end{bmatrix}, Temp \right) \quad \text{Wärmekapazität C}$$

$$c_{pL,D}(Temp) := \text{linterp} \left( \begin{bmatrix} 0 \text{ } ^\circ\text{C} \\ \vdots \end{bmatrix}, \begin{bmatrix} 1.931 \frac{\text{J}}{\text{gm K}} \\ \vdots \end{bmatrix}, Temp \right) \quad \text{Wärmekapazität D}$$

## Wärmekapazität Gas (isobar):

$$c_{pg,A}(Temp) := \text{linterp} \left( \begin{bmatrix} 0 \text{ } ^\circ\text{C} \\ \vdots \end{bmatrix}, \begin{bmatrix} 0.908 \frac{\text{J}}{\text{gm K}} \\ \vdots \end{bmatrix}, Temp \right) \quad \text{Wärmekapazität A}$$

$$c_{pg,B}(Temp) := \text{linterp} \left( \begin{bmatrix} 0 \text{ } ^\circ\text{C} \\ \vdots \end{bmatrix}, \begin{bmatrix} 1.328 \frac{\text{J}}{\text{gm K}} \\ \vdots \end{bmatrix}, Temp \right) \quad \text{Wärmekapazität B}$$

$$c_{pg,C}(Temp) := \text{linterp} \left( \begin{bmatrix} 0 \text{ } ^\circ\text{C} \\ \vdots \end{bmatrix}, \begin{bmatrix} 1.084 \frac{\text{J}}{\text{gm} \cdot \text{K}} \\ \vdots \end{bmatrix}, Temp \right)$$

Wärmekapazität C

$$c_{pg,D}(Temp) := \text{linterp} \left( \begin{bmatrix} 0 \text{ } ^\circ\text{C} \\ \vdots \end{bmatrix}, \begin{bmatrix} 0.987 \frac{\text{J}}{\text{gm} \cdot \text{K}} \\ \vdots \end{bmatrix}, Temp \right)$$

Wärmekapazität D

$$c_{pg,N2} := 1.040 \frac{\text{J}}{\text{gm} \cdot \text{K}}$$

Wärmekapazität N2

Wärmekapazität Gas (isochor):

$$c_{vg,A}(Temp) := \text{linterp} \left( \begin{bmatrix} 0 \text{ } ^\circ\text{C} \\ \vdots \end{bmatrix}, \begin{bmatrix} 0.908 \frac{\text{J}}{\text{gm} \cdot \text{K}} \\ \vdots \end{bmatrix}, Temp \right) - \frac{R}{M_A}$$

Wärmekapazität A

$$c_{vg,B}(Temp) := \text{linterp} \left( \begin{bmatrix} 0 \text{ } ^\circ\text{C} \\ \vdots \end{bmatrix}, \begin{bmatrix} 1.328 \frac{\text{J}}{\text{gm} \cdot \text{K}} \\ \vdots \end{bmatrix}, Temp \right) - \frac{R}{M_B}$$

Wärmekapazität B

$$c_{vg,C}(Temp) := \text{linterp} \left( \begin{bmatrix} 0 \text{ } ^\circ\text{C} \\ \vdots \end{bmatrix}, \begin{bmatrix} 1.084 \frac{\text{J}}{\text{gm} \cdot \text{K}} \\ \vdots \end{bmatrix}, Temp \right) - \frac{R}{M_C}$$

Wärmekapazität C

$$c_{vg,D}(Temp) := \text{linterp} \left( \begin{bmatrix} 0 \text{ } ^\circ\text{C} \\ \vdots \end{bmatrix}, \begin{bmatrix} 0.987 \frac{\text{J}}{\text{gm} \cdot \text{K}} \\ \vdots \end{bmatrix}, Temp \right) - \frac{R}{M_D}$$

Wärmekapazität D

$$c_{vg,N2}(Temp) := c_{pg,N2} - \frac{R}{M_{N2}} = 0.743 \frac{\text{J}}{\text{gm} \cdot \text{K}}$$

Wärmekapazität N2

Dampfdruck:

Parameter A	Parameter B	Parameter C	Parameter D
$A_{ps,A} := -8.15436$	$A_{ps,B} := -8.72963$	$A_{ps,C} := -8.57584$	$A_{ps,D} := -9.34304$
$B_{ps,A} := 1.80785$	$B_{ps,B} := 1.4586$	$B_{ps,C} := 4.22791$	$B_{ps,D} := 3.77735$
$C_{ps,A} := -3.76039$	$C_{ps,B} := -2.78449$	$C_{ps,C} := -5.37346$	$C_{ps,D} := -3.59092$
$D_{ps,A} := -3.04616$	$D_{ps,B} := -0.70669$	$D_{ps,C} := -0.82045$	$D_{ps,D} := -1.57006$

$$p_{s,A}(Temp) := p_{krit,A} \cdot e^{\left( \frac{T_{krit,A}}{Temp} \cdot \left( A_{ps,A} \cdot \left( 1 - \frac{Temp}{T_{krit,A}} \right) + B_{ps,A} \cdot \left( 1 - \frac{Temp}{T_{krit,A}} \right)^{1.5} + C_{ps,A} \cdot \left( 1 - \frac{Temp}{T_{krit,A}} \right)^{2.5} + D_{ps,A} \cdot \left( 1 - \frac{Temp}{T_{krit,A}} \right)^5 \right) \right)}$$

$$p_{s,B}(Temp) := p_{krit,B} \cdot e^{\left( \frac{T_{krit,B}}{Temp} \cdot \left( A_{ps,B} \cdot \left( 1 - \frac{Temp}{T_{krit,B}} \right) + B_{ps,B} \cdot \left( 1 - \frac{Temp}{T_{krit,B}} \right)^{1.5} + C_{ps,B} \cdot \left( 1 - \frac{Temp}{T_{krit,B}} \right)^{2.5} + D_{ps,B} \cdot \left( 1 - \frac{Temp}{T_{krit,B}} \right)^5 \right) \right)}$$

$$p_{s,C}(Temp) := p_{krit,C} \cdot e^{\left( \frac{T_{krit,C}}{Temp} \cdot \left( A_{ps,C} \cdot \left( 1 - \frac{Temp}{T_{krit,C}} \right) + B_{ps,C} \cdot \left( 1 - \frac{Temp}{T_{krit,C}} \right)^{1.5} + C_{ps,C} \cdot \left( 1 - \frac{Temp}{T_{krit,C}} \right)^{2.5} + D_{ps,C} \cdot \left( 1 - \frac{Temp}{T_{krit,C}} \right)^5 \right) \right)}$$

$$p_{s,D}(Temp) := p_{krit,D} \cdot e^{\left( \frac{T_{krit,D}}{Temp} \cdot \left( A_{ps,D} \cdot \left( 1 - \frac{Temp}{T_{krit,D}} \right) + B_{ps,D} \cdot \left( 1 - \frac{Temp}{T_{krit,D}} \right)^{1.5} + C_{ps,D} \cdot \left( 1 - \frac{Temp}{T_{krit,D}} \right)^{2.5} + D_{ps,D} \cdot \left( 1 - \frac{Temp}{T_{krit,D}} \right)^5 \right) \right)}$$

## Kinetik

Geschw.koeffizient:

$$k_{0,1}(x) := -1.36 \cdot 10^8 \frac{\text{L}}{\text{mol s}} + 1.36 \cdot 10^8 \cdot \exp(2.2 \cdot x) \cdot \frac{\text{L}}{\text{mol s}}$$

$$k_{0,2}(x) := 2 \cdot 10^7 \cdot \exp(-12.28 \cdot x) \cdot \frac{\text{L}^2}{\text{mol}^2 \text{ s}}$$

Aktivierungsenergie:

$$E_{A,1}(x) := -15924 \cdot x^2 \frac{\text{J}}{\text{mol}} + 20568 \cdot x \frac{\text{J}}{\text{mol}} + 77337 \frac{\text{J}}{\text{mol}}$$

$$E_{A,2}(x) := -40472 \cdot x \frac{\text{J}}{\text{mol}} + 80750 \frac{\text{J}}{\text{mol}}$$

Reaktionsenthalpie:

$$\Delta H_R := -66300 \frac{\text{J}}{\text{mol}} = -66300 \frac{\text{J}}{\text{mol}}$$

## Prozessdaten

Referenztemperatur:

$$T_{ref} := 298.15 \text{ K}$$

Referenzdruck:

$$p_{ref} := 1 \text{ bar}$$

Dosierstrom:

$$m_{B,F} := 0 \frac{\text{kg}}{\text{s}}$$

Dosiertemperatur:

$$T_{B,F} := 80 \text{ °C}$$

## Berechnung des Anfangszustand im Reaktor pT-Flash

pT-Flash --> Druck und Temperatur sind bekannt und konstant. Gesucht ist die Zusammensetzung der Flüssigkeit und Gasphase bzw. ihre Massen je Komponente.

$$pT\_Flash(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) := \left| \begin{array}{l} x_{spec,A} \leftarrow \frac{\frac{m_{0,A}}{M_A}}{\frac{m_{0,A}}{M_A} + \frac{m_{0,B}}{M_B} + \frac{m_{0,C}}{M_C} + \frac{m_{0,D}}{M_D}} \\ x_{spec,B} \leftarrow \frac{\frac{m_{0,B}}{M_B}}{\frac{m_{0,A}}{M_A} + \frac{m_{0,B}}{M_B} + \frac{m_{0,C}}{M_C} + \frac{m_{0,D}}{M_D}} \\ m_{0,C} \end{array} \right.$$

$$x_{spec\_C} \leftarrow \frac{\frac{m_{0\_C}}{M_C}}{\frac{m_{0\_A}}{M_A} + \frac{m_{0\_B}}{M_B} + \frac{m_{0\_C}}{M_C} + \frac{m_{0\_D}}{M_D}}$$

$$x_{spec\_D} \leftarrow \frac{\frac{m_{0\_D}}{M_D}}{\frac{m_{0\_A}}{M_A} + \frac{m_{0\_B}}{M_B} + \frac{m_{0\_C}}{M_C} + \frac{m_{0\_D}}{M_D}}$$

$$p_{sat\_A} \leftarrow p_{s\_A}(Temp)$$

$$p_{sat\_B} \leftarrow p_{s\_B}(Temp)$$

$$p_{sat\_C} \leftarrow p_{s\_C}(Temp)$$

$$p_{sat\_D} \leftarrow p_{s\_D}(Temp)$$

$$p_{spec} \leftarrow x_{spec\_A} \cdot p_{sat\_A} + x_{spec\_B} \cdot p_{sat\_B} + x_{spec\_C} \cdot p_{sat\_C} + x_{spec\_D} \cdot p_{sat\_D}$$

for  $i \in 0 \dots 10$

$$m_l \leftarrow \frac{m_{0\_A} + m_{0\_B} + m_{0\_C} + m_{0\_D} - \frac{Vol}{R \cdot Temp} (x_{spec\_A} \cdot p_{sat\_A} \cdot M_A + x_{spec\_B} \cdot p_{sat\_B} \cdot M_B + x_{spec\_C} \cdot p_{sat\_C} \cdot M_C + x_{spec\_D} \cdot p_{sat\_D} \cdot M_D)}{1 - \frac{1}{R \cdot Temp} (x_{spec\_A} \cdot M_A + x_{spec\_B} \cdot M_B + x_{spec\_C} \cdot M_C + x_{spec\_D} \cdot M_D) \cdot \left( \frac{x_{spec\_A} \cdot M_A}{\rho_A(Temp)} + \frac{x_{spec\_B} \cdot M_B}{\rho_B(Temp)} + \frac{x_{spec\_C} \cdot M_C}{\rho_C(Temp)} + \frac{x_{spec\_D} \cdot M_D}{\rho_D(Temp)} \right) \cdot (x_{spec\_A} \cdot p_{sat\_A} \cdot M_A + x_{spec\_B} \cdot p_{sat\_B} \cdot M_B + x_{spec\_C} \cdot p_{sat\_C} \cdot M_C + x_{spec\_D} \cdot p_{sat\_D} \cdot M_D)}$$

$$V_l \leftarrow \frac{m_l}{x_{spec\_A} \cdot M_A + x_{spec\_B} \cdot M_B + x_{spec\_C} \cdot M_C + x_{spec\_D} \cdot M_D} \cdot \left( \frac{x_{spec\_A} \cdot M_A}{\rho_A(Temp)} + \frac{x_{spec\_B} \cdot M_B}{\rho_B(Temp)} + \frac{x_{spec\_C} \cdot M_C}{\rho_C(Temp)} + \frac{x_{spec\_D} \cdot M_D}{\rho_D(Temp)} \right)$$

$$V_g \leftarrow Vol - V_l$$

$$m_{g\_A} \leftarrow \frac{x_{spec\_A} \cdot p_{sat\_A} \cdot V_g \cdot M_A}{R \cdot Temp}$$

$$m_{g\_B} \leftarrow \frac{x_{spec\_B} \cdot p_{sat\_B} \cdot V_g \cdot M_B}{R \cdot Temp}$$

$$m_{g\_C} \leftarrow \frac{x_{spec\_C} \cdot p_{sat\_C} \cdot V_g \cdot M_C}{R \cdot Temp}$$

$$m_{g\_D} \leftarrow \frac{x_{spec\_D} \cdot p_{sat\_D} \cdot V_g \cdot M_D}{R \cdot Temp}$$

$$m_{g\_N2} \leftarrow \frac{(p_{spec} - x_{spec\_A} \cdot p_{sat\_A} - x_{spec\_B} \cdot p_{sat\_B} - x_{spec\_C} \cdot p_{sat\_C} - x_{spec\_D} \cdot p_{sat\_D}) \cdot V_g \cdot M_{N2}}{R \cdot Temp}$$

$$m_g \leftarrow m_{g\_N2} + m_{g\_A} + m_{g\_B} + m_{g\_C} + m_{g\_D}$$

$$m_{l\_A} \leftarrow m_{0\_A} - m_{g\_A}$$

$$m_{l\_B} \leftarrow m_{0\_B} - m_{g\_B}$$

$$m_{l\_C} \leftarrow m_{0\_C} - m_{g\_C}$$

$$m_{l\_D} \leftarrow m_{0\_D} - m_{g\_D}$$

$$x_{spec\_A} \leftarrow \frac{\frac{m_{l\_A}}{M_A}}{\frac{m_{l\_A}}{M_A} + \frac{m_{l\_B}}{M_B} + \frac{m_{l\_C}}{M_C} + \frac{m_{l\_D}}{M_D}}$$

$$x_{spec\_B} \leftarrow \frac{\frac{m_{l\_B}}{M_B}}{\frac{m_{l\_A}}{M_A} + \frac{m_{l\_B}}{M_B} + \frac{m_{l\_C}}{M_C} + \frac{m_{l\_D}}{M_D}}$$

$$x_{spec\_C} \leftarrow \frac{\frac{m_{l\_C}}{M_C}}{\frac{m_{l\_A}}{M_A} + \frac{m_{l\_B}}{M_B} + \frac{m_{l\_C}}{M_C} + \frac{m_{l\_D}}{M_D}}$$

$$x_{spec\_D} \leftarrow \frac{\frac{m_{l\_D}}{M_D}}{\frac{m_{l\_A}}{M_A} + \frac{m_{l\_B}}{M_B} + \frac{m_{l\_C}}{M_C} + \frac{m_{l\_D}}{M_D}}$$

$$y_{spec\_A} \leftarrow \frac{\frac{m_{g\_A}}{M_A}}{\frac{m_{g\_A}}{M_A} + \frac{m_{g\_B}}{M_B} + \frac{m_{g\_C}}{M_C} + \frac{m_{g\_D}}{M_D} + \frac{m_{g\_N2}}{M_{N2}}}$$

$$\begin{aligned}
 & \begin{matrix} \text{---A} & \text{---B} & \text{---C} & \text{---D} & \text{---N}_2 \\ & & \frac{m_{g,B}}{M_B} & & \\ y_{spec,B} \leftarrow & \frac{m_{g,A}}{M_A} + \frac{m_{g,B}}{M_B} + \frac{m_{g,C}}{M_C} + \frac{m_{g,D}}{M_D} + \frac{m_{g,N_2}}{M_{N_2}} & & & \\ & & \frac{m_{g,C}}{M_C} & & \\ y_{spec,C} \leftarrow & \frac{m_{g,A}}{M_A} + \frac{m_{g,B}}{M_B} + \frac{m_{g,C}}{M_C} + \frac{m_{g,D}}{M_D} + \frac{m_{g,N_2}}{M_{N_2}} & & & \\ & & \frac{m_{g,D}}{M_D} & & \\ y_{spec,D} \leftarrow & \frac{m_{g,A}}{M_A} + \frac{m_{g,B}}{M_B} + \frac{m_{g,C}}{M_C} + \frac{m_{g,D}}{M_D} + \frac{m_{g,N_2}}{M_{N_2}} & & & \\ & & \frac{m_{g,N_2}}{M_{N_2}} & & \\ y_{spec,N_2} \leftarrow & \frac{m_{g,A}}{M_A} + \frac{m_{g,B}}{M_B} + \frac{m_{g,C}}{M_C} + \frac{m_{g,D}}{M_D} + \frac{m_{g,N_2}}{M_{N_2}} & & & \\ p_{spec} \leftarrow & x_{spec,A} \cdot p_{sat,A} + x_{spec,B} \cdot p_{sat,B} + x_{spec,C} \cdot p_{sat,C} + x_{spec,D} \cdot p_{sat,D} + \frac{m_{g,N_2} \cdot R \cdot Temp}{V_g \cdot M_{N_2}} & & & \\ \left[ x_{spec,A} & x_{spec,B} & x_{spec,C} & x_{spec,D} & y_{spec,A} & y_{spec,B} & y_{spec,C} & y_{spec,D} & y_{spec,N_2} & m_l & m_g & V_l & V_g & p_{spec} \right]^T
 \end{matrix}
 \end{aligned}$$

Startzusammensetzung Flüssigkeit:

$$x_{0,A}(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) := pT\_Flash(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D})_0$$

$$x_{0,B}(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) := pT\_Flash(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D})_1$$

$$x_{0,C}(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) := pT\_Flash(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D})_2$$

$$x_{0,D}(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) := pT\_Flash(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D})_3$$

Startzusammensetzung Gas:

$$y_{0,A}(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) := pT\_Flash(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D})_4$$

$$y_{0,B}(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) := pT\_Flash(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D})_5$$

$$y_{0,C}(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) := pT\_Flash(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D})_6$$

$$y_{0,D}(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) := pT\_Flash(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D})_7$$

$$y_{0,N_2}(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) := pT\_Flash(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D})_8$$

Startmassen und Startvolumen:

$$m_{0,l}(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) := pT\_Flash(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D})_9$$

$$m_{0,g}(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) := pT\_Flash(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D})_{10}$$

$$m_0(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) := m_{0,l}(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) + m_{0,g}(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D})$$



$$m_{0\_g\_N2}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) := m_{0\_g}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) \cdot \zeta_{0\_g\_N2}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D})$$

$$m_{0\_A}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) := m_{0\_l\_A}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) + m_{0\_g\_A}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D})$$

$$m_{0\_B}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) := m_{0\_l\_B}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) + m_{0\_g\_B}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D})$$

$$m_{0\_C}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) := m_{0\_l\_C}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) + m_{0\_g\_C}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D})$$

$$m_{0\_D}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) := m_{0\_l\_D}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) + m_{0\_g\_D}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D})$$

$$x_0(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) := \frac{\frac{m_{0\_l\_A}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D})}{M_A}}{\frac{m_{0\_l\_A}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D})}{M_A} + \frac{m_{0\_l\_B}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D})}{M_B}}$$

Innere Energien zum Startzeitpunkt:

$$h_{0\_l}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) := \zeta_{0\_l\_A}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) \downarrow$$

- $(\Delta H_{B\_A} + c_{pl\_A}(Temp) \cdot (Temp - T_{ref}) - \Delta h_{V\_A}(Temp)) \downarrow$
- +  $\zeta_{0\_l\_B}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) \downarrow$
- $(\Delta H_{B\_B} + c_{pl\_B}(Temp) \cdot (Temp - T_{ref}) - \Delta h_{V\_B}(Temp)) \downarrow$
- +  $\zeta_{0\_l\_C}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) \downarrow$
- $(\Delta H_{B\_C} + c_{pl\_C}(Temp) \cdot (Temp - T_{ref}) - \Delta h_{V\_C}(Temp)) \downarrow$
- +  $\zeta_{0\_l\_D}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) \downarrow$
- $(\Delta H_{B\_D} + c_{pl\_D}(Temp) \cdot (Temp - T_{ref}) - \Delta h_{V\_D}(Temp)) \downarrow$

$$h_{0\_g}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) := \zeta_{0\_g\_A}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) \downarrow$$

- $(\Delta H_{B\_A} + c_{pg\_A}(Temp) \cdot (Temp - T_{ref})) \downarrow$
- +  $\zeta_{0\_g\_B}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) \downarrow$
- $(\Delta H_{B\_B} + c_{pg\_B}(Temp) \cdot (Temp - T_{ref})) \downarrow$
- +  $\zeta_{0\_g\_C}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) \downarrow$
- $(\Delta H_{B\_C} + c_{pg\_C}(Temp) \cdot (Temp - T_{ref})) \downarrow$
- +  $\zeta_{0\_g\_D}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) \downarrow$
- $(\Delta H_{B\_D} + c_{pg\_D}(Temp) \cdot (Temp - T_{ref})) \downarrow$
- +  $\zeta_{0\_g\_N2}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) \downarrow$
- $(\Delta H_{B\_N2} + c_{pg\_N2} \cdot (Temp - T_{ref})) \downarrow$

$$H_0(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) := h_{0\_l}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) \cdot m_{0\_l}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) \downarrow$$

$$+ h_{0\_g}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) \cdot m_{0\_g}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D})$$

$$U_0(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) := H_0(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) \downarrow$$

$$- p_0(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D}) \cdot Vol$$

	Temp
$p_0(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D})$	
	Vol
$V_{0\_l}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D})$	
$V_{0\_g}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D})$	
$x_{0\_A}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D})$	
$x_{0\_B}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D})$	
$x_{0\_C}(Vol, Temp, m_{0\_A}, m_{0\_B}, m_{0\_C}, m_{0\_D})$	

$$\text{Startbed}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) := \begin{bmatrix} x_{0,D}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ y_{0,A}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ y_{0,B}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ y_{0,C}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ y_{0,D}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ y_{0,N2}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ m_0(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ m_{0,l}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ m_{0,g}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ \zeta_{0,l,A}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ \zeta_{0,l,B}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ \zeta_{0,l,C}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ \zeta_{0,l,D}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ \zeta_{0,g,A}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ \zeta_{0,g,B}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ \zeta_{0,g,C}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ \zeta_{0,g,D}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ \zeta_{0,g,N2}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ m_{0,l,A}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ m_{0,l,B}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ m_{0,l,C}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ m_{0,l,D}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ m_{0,g,A}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ m_{0,g,B}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ m_{0,g,C}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ m_{0,g,D}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ m_{0,g,N2}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ m_{0,A} \\ m_{0,B} \\ m_{0,C} \\ m_{0,D} \\ U_0(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \\ x_0(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}) \end{bmatrix}$$

**UVm-Flash**

UVm-Flash --> Innere Energie, Volumen und Gesamtmasse sind bekannt und konstant für einen Zeitpunkt t. Gesucht ist die Zusammensetzung der Flüssigkeit und Gasphase bzw. ihre Massen je Komponente, sowie die intensiven Zustandsgrößen p und T.

$$\text{UVm\_Flash}(\text{InnerEnergie}, \text{Vol}, \text{Mass}, \text{MasseA}, \text{MasseB}, \text{MasseC}, \text{MasseD}, p_{\text{spec}}, T_{\text{spec}}, x_{\text{spec},A}, x_{\text{spec},B}, x_{\text{spec},C}, x_{\text{spec},D}) := \begin{bmatrix} K_{\text{spec},A} \leftarrow \frac{p_{s,A}(T_{\text{spec}})}{p_{\text{spec}}} \\ K_{\text{spec},B} \leftarrow \frac{p_{s,B}(T_{\text{spec}})}{p_{\text{spec}}} \\ K_{\text{spec},C} \leftarrow \frac{p_{s,C}(T_{\text{spec}})}{p_{\text{spec}}} \\ K_{\text{spec},D} \leftarrow \frac{p_{s,D}(T_{\text{spec}})}{p_{\text{spec}}} \\ j \leftarrow 0 \\ \varepsilon \leftarrow 10^{-3} \\ \text{for } i \in 0 \dots 15 \\ \begin{bmatrix} p_{\text{sat},A} \leftarrow p_{s,A}(T_{\text{spec}}) \\ p_{\text{sat},B} \leftarrow p_{s,B}(T_{\text{spec}}) \\ p_{\text{sat},C} \leftarrow p_{s,C}(T_{\text{spec}}) \\ p_{\text{sat},D} \leftarrow p_{s,D}(T_{\text{spec}}) \end{bmatrix} \end{bmatrix}$$



$$\begin{aligned} \rho_{spec\_A} &\leftarrow \rho_A(T_{spec}) \\ \rho_{spec\_B} &\leftarrow \rho_B(T_{spec}) \\ \rho_{spec\_C} &\leftarrow \rho_C(T_{spec}) \\ \rho_{spec\_D} &\leftarrow \rho_D(T_{spec}) \\ m_l &\leftarrow \frac{MasseA + MasseB + MasseC + MasseD - \frac{Vol}{R \cdot T_{spec}} (x_{spec\_A} \cdot p_{sat\_A} \cdot M_A + x_{spec\_B} \cdot p_{sat\_B} \cdot M_B + x_{spec\_C} \cdot p_{sat\_C} \cdot M_C + x_{spec\_D} \cdot p_{sat\_D} \cdot M_D)}{1 - \frac{1}{R \cdot T_{spec}} \cdot (x_{spec\_A} \cdot M_A + x_{spec\_B} \cdot M_B + x_{spec\_C} \cdot M_C + x_{spec\_D} \cdot M_D) \cdot \left( \frac{x_{spec\_A} \cdot M_A}{\rho_{spec\_A}} + \frac{x_{spec\_B} \cdot M_B}{\rho_{spec\_B}} + \frac{x_{spec\_C} \cdot M_C}{\rho_{spec\_C}} + \frac{x_{spec\_D} \cdot M_D}{\rho_{spec\_D}} \right)} \cdot (x_{spec\_A} \cdot p_{sat\_A} \cdot M_A + x_{spec\_B} \cdot p_{sat\_B} \cdot M_B + \dots) \\ m_g &\leftarrow Mass - m_l \\ V_l &\leftarrow \frac{m_l}{x_{spec\_A} \cdot M_A + x_{spec\_B} \cdot M_B + x_{spec\_C} \cdot M_C + x_{spec\_D} \cdot M_D} \cdot \left( \frac{x_{spec\_A} \cdot M_A}{\rho_{spec\_A}} + \frac{x_{spec\_B} \cdot M_B}{\rho_{spec\_B}} + \frac{x_{spec\_C} \cdot M_C}{\rho_{spec\_C}} + \frac{x_{spec\_D} \cdot M_D}{\rho_{spec\_D}} \right) \\ V_g &\leftarrow Vol - V_l \\ m_{g\_A} &\leftarrow \frac{x_{spec\_A} \cdot p_{sat\_A} \cdot V_g \cdot M_A}{R \cdot T_{spec}} \\ m_{g\_B} &\leftarrow \frac{x_{spec\_B} \cdot p_{sat\_B} \cdot V_g \cdot M_B}{R \cdot T_{spec}} \\ m_{g\_C} &\leftarrow \frac{x_{spec\_C} \cdot p_{sat\_C} \cdot V_g \cdot M_C}{R \cdot T_{spec}} \\ m_{g\_D} &\leftarrow \frac{x_{spec\_D} \cdot p_{sat\_D} \cdot V_g \cdot M_D}{R \cdot T_{spec}} \\ m_{g\_N2} &\leftarrow m_g - m_{g\_A} - m_{g\_B} - m_{g\_C} - m_{g\_D} \\ m_{l\_A} &\leftarrow MasseA - m_{g\_A} \\ m_{l\_B} &\leftarrow MasseB - m_{g\_B} \\ m_{l\_C} &\leftarrow MasseC - m_{g\_C} \\ m_{l\_D} &\leftarrow MasseD - m_{g\_D} \\ \zeta_{spec\_lA} &\leftarrow \frac{m_{l\_A}}{m_{l\_A} + m_{l\_B} + m_{l\_C} + m_{l\_D}} \\ \zeta_{spec\_lB} &\leftarrow \frac{m_{l\_B}}{m_{l\_A} + m_{l\_B} + m_{l\_C} + m_{l\_D}} \\ \zeta_{spec\_lC} &\leftarrow \frac{m_{l\_C}}{m_{l\_A} + m_{l\_B} + m_{l\_C} + m_{l\_D}} \\ \zeta_{spec\_lD} &\leftarrow \frac{m_{l\_D}}{m_{l\_A} + m_{l\_B} + m_{l\_C} + m_{l\_D}} \\ \zeta_{spec\_gA} &\leftarrow \frac{m_{g\_A}}{m_{g\_A} + m_{g\_B} + m_{g\_C} + m_{g\_D} + m_{g\_N2}} \\ \zeta_{spec\_gB} &\leftarrow \frac{m_{g\_B}}{m_{g\_A} + m_{g\_B} + m_{g\_C} + m_{g\_D} + m_{g\_N2}} \\ \zeta_{spec\_gC} &\leftarrow \frac{m_{g\_C}}{m_{g\_A} + m_{g\_B} + m_{g\_C} + m_{g\_D} + m_{g\_N2}} \\ \zeta_{spec\_gD} &\leftarrow \frac{m_{g\_D}}{m_{g\_A} + m_{g\_B} + m_{g\_C} + m_{g\_D} + m_{g\_N2}} \\ \zeta_{spec\_gN2} &\leftarrow \frac{m_{g\_N2}}{m_{g\_A} + m_{g\_B} + m_{g\_C} + m_{g\_D} + m_{g\_N2}} \\ x_{spec\_A} &\leftarrow \frac{\frac{m_{l\_A}}{M_A}}{\frac{m_{l\_A}}{M_A} + \frac{m_{l\_B}}{M_B} + \frac{m_{l\_C}}{M_C} + \frac{m_{l\_D}}{M_D}} \\ x_{spec\_B} &\leftarrow \frac{\frac{m_{l\_B}}{M_B}}{\frac{m_{l\_A}}{M_A} + \frac{m_{l\_B}}{M_B} + \frac{m_{l\_C}}{M_C} + \frac{m_{l\_D}}{M_D}} \\ x_{spec\_C} &\leftarrow \frac{\frac{m_{l\_C}}{M_C}}{\frac{m_{l\_A}}{M_A} + \frac{m_{l\_B}}{M_B} + \frac{m_{l\_C}}{M_C} + \frac{m_{l\_D}}{M_D}} \end{aligned}$$



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x_spec_D ← 1 - x_spec_A - x_spec_B - x_spec_C
y_spec_A ←  $\frac{\frac{m_{g,A}}{M_A}}{\frac{m_{g,A}}{M_A} + \frac{m_{g,B}}{M_B} + \frac{m_{g,C}}{M_C} + \frac{m_{g,D}}{M_D} + \frac{m_{g,N_2}}{M_{N_2}}}$ 
y_spec_B ←  $\frac{\frac{m_{g,B}}{M_B}}{\frac{m_{g,A}}{M_A} + \frac{m_{g,B}}{M_B} + \frac{m_{g,C}}{M_C} + \frac{m_{g,D}}{M_D} + \frac{m_{g,N_2}}{M_{N_2}}}$ 
y_spec_C ←  $\frac{\frac{m_{g,C}}{M_C}}{\frac{m_{g,A}}{M_A} + \frac{m_{g,B}}{M_B} + \frac{m_{g,C}}{M_C} + \frac{m_{g,D}}{M_D} + \frac{m_{g,N_2}}{M_{N_2}}}$ 
y_spec_D ←  $\frac{\frac{m_{g,D}}{M_D}}{\frac{m_{g,A}}{M_A} + \frac{m_{g,B}}{M_B} + \frac{m_{g,C}}{M_C} + \frac{m_{g,D}}{M_D} + \frac{m_{g,N_2}}{M_{N_2}}}$ 
y_spec_N2 ←  $\frac{1 - y_spec_A - y_spec_B - y_spec_C - y_spec_D}{\frac{m_{g,N_2}}{M_{N_2}}}$ 
T_spec ←  $\frac{InnerEnergie + p_{spec} \cdot Vol - m_l \cdot (\zeta_{spec,l,A} \cdot (\Delta H_{B,A} - \Delta h_{V,A}(T_{spec})) + \zeta_{spec,l,B} \cdot (\Delta H_{B,B} - \Delta h_{V,B}(T_{spec})) + \zeta_{spec,l,C} \cdot (\Delta H_{B,C} - \Delta h_{V,C}(T_{spec})) + \zeta_{spec,l,D} \cdot (\Delta H_{B,D} - \Delta h_{V,D}(T_{spec})) + m_g \cdot (\zeta_{spec,g,A} \cdot c_{pg,A}(T_{spec}) + \zeta_{spec,g,B} \cdot c_{pg,B}(T_{spec}))}{m_l \cdot (\zeta_{spec,l,A} \cdot c_{pl,A}(T_{spec}) + \zeta_{spec,l,B} \cdot c_{pl,B}(T_{spec}) + \zeta_{spec,l,C} \cdot c_{pl,C}(T_{spec}) + \zeta_{spec,l,D} \cdot c_{pl,D}(T_{spec})) + m_g \cdot (\zeta_{spec,g,A} \cdot c_{pg,A}(T_{spec}) + \zeta_{spec,g,B} \cdot c_{pg,B}(T_{spec}))}$ 
p_spec ←  $\frac{x_{spec,A} \cdot p_{sat,A} + x_{spec,B} \cdot p_{sat,B} + x_{spec,C} \cdot p_{sat,C} + x_{spec,D} \cdot p_{sat,D} + \frac{m_{g,N_2} \cdot R \cdot T_{spec}}{V_g \cdot M_{N_2}}}{K_{spec\_new\_A} \leftarrow \frac{p_{sat,A}}{p_{spec}}$ 
K_spec_new_B ←  $\frac{p_{sat,B}}{p_{spec}}$ 
K_spec_new_C ←  $\frac{p_{sat,C}}{p_{spec}}$ 
K_spec_new_D ←  $\frac{p_{sat,D}}{p_{spec}}$ 
if  $\frac{|K_{spec\_new\_A} - K_{spec,A}|}{K_{spec,A}} < \epsilon \wedge \frac{|K_{spec\_new\_B} - K_{spec,B}|}{K_{spec,B}} < \epsilon \wedge \frac{|K_{spec\_new\_C} - K_{spec,C}|}{K_{spec,C}} < \epsilon \wedge \frac{|K_{spec\_new\_D} - K_{spec,D}|}{K_{spec,D}} < \epsilon$ 
    break
else
    j ← j + 1
    K_spec_A ← K_spec_new_A
    K_spec_B ← K_spec_new_B
    K_spec_C ← K_spec_new_C
    K_spec_D ← K_spec_new_D

```

$[x_{spec,A} \ x_{spec,B} \ x_{spec,C} \ x_{spec,D} \ y_{spec,A} \ y_{spec,B} \ y_{spec,C} \ y_{spec,D} \ y_{spec,N_2} \ m_l \ m_g \ V_l \ V_g \ T_{spec} \ p_{spec} \ j]^T$

**DGL-System für Reaktor**

Numerische Eingaben:

TOL := 10<sup>-7</sup>      CTOL := 10<sup>-7</sup>

Anfangsbedingungen:

$m_{l,A}(0 \ s) = Startbed(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D})_{26}$

$m_{l,B}(0 \ s) = Startbed(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D})$



$$\zeta_{g,N_2}(0 \mathbf{s}) = \text{Startbed}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D})_{25}$$

$$m_i(0 \mathbf{s}) = \text{Startbed}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D})_{15}$$

$$m_g(0 \mathbf{s}) = \text{Startbed}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D})_{16}$$

$$V_l(0 \mathbf{s}) = \text{Startbed}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D})_3$$

$$V_g(0 \mathbf{s}) = \text{Startbed}(\text{Vol}, \text{Temp}, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D})_4$$

## Massenbilanzen:

$$\frac{d}{dt} m_{l,A}(t) = -k_{0,1}(x_0) \cdot \exp\left(\frac{E_{A,1}(x_0)}{R \cdot T(t)}\right) \cdot \frac{m_i(t)^2 \cdot \zeta_{l,A}(t) \cdot \zeta_{l,B}(t)}{M_B \cdot V_l(t)} - k_{0,2}(x_0) \cdot \exp\left(\frac{E_{A,2}(x_0)}{R \cdot T(t)}\right) \cdot \frac{m_i(t)^3 \cdot \zeta_{l,A}(t) \cdot \zeta_{l,B}(t) \cdot \zeta_{l,D}(t)}{M_D \cdot M_B \cdot V_l(t)^2}$$

$$\frac{d}{dt} m_{l,B}(t) = m_{B,F} - k_{0,1}(x_0) \cdot \exp\left(\frac{E_{A,1}(x_0)}{R \cdot T(t)}\right) \cdot \frac{m_i(t)^2 \cdot \zeta_{l,A}(t) \cdot \zeta_{l,B}(t)}{M_A \cdot V_l(t)} - k_{0,2}(x_0) \cdot \exp\left(\frac{E_{A,2}(x_0)}{R \cdot T(t)}\right) \cdot \frac{m_i(t)^3 \cdot \zeta_{l,A}(t) \cdot \zeta_{l,B}(t) \cdot \zeta_{l,D}(t)}{M_A \cdot M_D \cdot V_l(t)^2}$$

$$\frac{d}{dt} m_{l,C}(t) = k_{0,1}(x_0) \cdot \exp\left(\frac{E_{A,1}(x_0)}{R \cdot T(t)}\right) \cdot \frac{m_i(t)^2 \cdot \zeta_{l,A}(t) \cdot \zeta_{l,B}(t)}{M_A \cdot M_B \cdot V_l(t)} \cdot M_C + k_{0,2}(x_0) \cdot \exp\left(\frac{E_{A,2}(x_0)}{R \cdot T(t)}\right) \cdot \frac{m_i(t)^3 \cdot \zeta_{l,A}(t) \cdot \zeta_{l,B}(t) \cdot \zeta_{l,D}(t)}{M_A \cdot M_B \cdot M_D \cdot V_l(t)^2} \cdot M_C$$

$$\frac{d}{dt} m_{l,D}(t) = k_{0,1}(x_0) \cdot \exp\left(\frac{E_{A,1}(x_0)}{R \cdot T(t)}\right) \cdot \frac{m_i(t)^2 \cdot \zeta_{l,A}(t) \cdot \zeta_{l,B}(t)}{M_A \cdot M_B \cdot V_l(t)} \cdot M_D + k_{0,2}(x_0) \cdot \exp\left(\frac{E_{A,2}(x_0)}{R \cdot T(t)}\right) \cdot \frac{m_i(t)^3 \cdot \zeta_{l,A}(t) \cdot \zeta_{l,B}(t) \cdot \zeta_{l,D}(t)}{M_A \cdot M_B \cdot M_D \cdot V_l(t)^2} \cdot M_D$$

$$\frac{d}{dt} m_{N_2}(t) = 0$$

$$m(t) = m_{l,A}(t) + m_g(t) \cdot \zeta_{g,A}(t) + m_{l,B}(t) + m_g(t) \cdot \zeta_{g,B}(t) + m_{l,C}(t) + m_g(t) \cdot \zeta_{g,C}(t) + m_{l,D}(t) + m_g(t) \cdot \zeta_{g,D}(t) + m_{N_2}(t)$$

## Energiebilanz:

$$\frac{d}{dt} xU(t) = m_{B,F} \cdot (\Delta H_{B,B} + c_{p,g,B}(T_{B,F}) \cdot (T_{B,F} - T_{ref}) - \Delta h_{v,B}(T_{B,F})) - \Delta H_R \cdot \left( k_{0,1}(x_0) \cdot \exp\left(\frac{E_{A,1}(x_0)}{R \cdot T(t)}\right) \cdot \frac{m_i(t)^2 \cdot \zeta_{l,A}(t) \cdot \zeta_{l,B}(t)}{M_A \cdot M_B \cdot V_l(t)} + k_{0,2}(x_0) \cdot \exp\left(\frac{E_{A,2}(x_0)}{R \cdot T(t)}\right) \cdot \frac{m_i(t)^3 \cdot \zeta_{l,A}(t) \cdot \zeta_{l,B}(t) \cdot \zeta_{l,D}(t)}{M_A \cdot M_B \cdot M_D \cdot V_l(t)^2} \right)$$

## Flash Berechnung:

$$x_A(t) = UVm\_Flash(xU(t), \text{Vol}, m(t), m_{l,A}(t) + m_g(t) \cdot \zeta_{g,A}(t), m_{l,B}(t) + m_g(t) \cdot \zeta_{g,B}(t), m_{l,C}(t) + m_g(t) \cdot \zeta_{g,C}(t), m_{l,D}(t) + m_g(t) \cdot \zeta_{g,D}(t), p(t), T(t), x_A(t), x_B(t), x_C(t), x_D(t))_0$$

$$x_B(t) = UVm\_Flash(xU(t), \text{Vol}, m(t), m_{l,A}(t) + m_g(t) \cdot \zeta_{g,A}(t), m_{l,B}(t) + m_g(t) \cdot \zeta_{g,B}(t), m_{l,C}(t) + m_g(t) \cdot \zeta_{g,C}(t), m_{l,D}(t) + m_g(t) \cdot \zeta_{g,D}(t), p(t), T(t), x_A(t), x_B(t), x_C(t), x_D(t))_1$$

$$x_C(t) = UVm\_Flash(xU(t), \text{Vol}, m(t), m_{l,A}(t) + m_g(t) \cdot \zeta_{g,A}(t), m_{l,B}(t) + m_g(t) \cdot \zeta_{g,B}(t), m_{l,C}(t) + m_g(t) \cdot \zeta_{g,C}(t), m_{l,D}(t) + m_g(t) \cdot \zeta_{g,D}(t), p(t), T(t), x_A(t), x_B(t), x_C(t), x_D(t))_2$$

$$x_D(t) = UVm\_Flash(xU(t), \text{Vol}, m(t), m_{l,A}(t) + m_g(t) \cdot \zeta_{g,A}(t), m_{l,B}(t) + m_g(t) \cdot \zeta_{g,B}(t), m_{l,C}(t) + m_g(t) \cdot \zeta_{g,C}(t), m_{l,D}(t) + m_g(t) \cdot \zeta_{g,D}(t), p(t), T(t), x_A(t), x_B(t), x_C(t), x_D(t))_3$$

$$y_A(t) = \frac{x_A(t) \cdot p_{s,A}(T(t))}{p(t)}$$

$$y_B(t) = \frac{x_B(t) \cdot p_{s,B}(T(t))}{p(t)}$$

$$y_C(t) = \frac{x_C(t) \cdot p_{s,C}(T(t))}{p(t)}$$

$$y_D(t) = \frac{x_D(t) \cdot p_{s,D}(T(t))}{p(t)}$$

$$y_{N2}(t) = 1 - y_A(t) - y_B(t) - y_C(t) - y_D(t)$$

$$\zeta_{l,A}(t) = \frac{x_A(t) \cdot M_A}{x_A(t) \cdot M_A + x_B(t) \cdot M_B + x_C(t) \cdot M_C + x_D(t) \cdot M_D}$$

$$\zeta_{l,B}(t) = \frac{x_B(t) \cdot M_B}{x_A(t) \cdot M_A + x_B(t) \cdot M_B + x_C(t) \cdot M_C + x_D(t) \cdot M_D}$$

$$\zeta_{l,C}(t) = \frac{x_C(t) \cdot M_C}{x_A(t) \cdot M_A + x_B(t) \cdot M_B + x_C(t) \cdot M_C + x_D(t) \cdot M_D}$$

$$\zeta_{l,D}(t) = 1 - \zeta_{l,A}(t) - \zeta_{l,B}(t) - \zeta_{l,C}(t)$$

$$\zeta_{g,A}(t) = \frac{y_A(t) \cdot M_A}{y_A(t) \cdot M_A + y_B(t) \cdot M_B + y_C(t) \cdot M_C + y_D(t) \cdot M_D + y_{N2}(t) \cdot M_{N2}}$$

$$\zeta_{g,B}(t) = \frac{y_B(t) \cdot M_B}{y_A(t) \cdot M_A + y_B(t) \cdot M_B + y_C(t) \cdot M_C + y_D(t) \cdot M_D + y_{N2}(t) \cdot M_{N2}}$$

$$\zeta_{g,C}(t) = \frac{y_C(t) \cdot M_C}{y_A(t) \cdot M_A + y_B(t) \cdot M_B + y_C(t) \cdot M_C + y_D(t) \cdot M_D + y_{N2}(t) \cdot M_{N2}}$$

$$\zeta_{g,D}(t) = \frac{y_D(t) \cdot M_D}{y_A(t) \cdot M_A + y_B(t) \cdot M_B + y_C(t) \cdot M_C + y_D(t) \cdot M_D + y_{N2}(t) \cdot M_{N2}}$$

$$\zeta_{g,N2}(t) = 1 - \zeta_{g,A}(t) - \zeta_{g,B}(t) - \zeta_{g,C}(t) - \zeta_{g,D}(t)$$

$$m_l(t) = UVm\_Flash(xU(t), Vol, m(t), m_{l,A}(t) + m_g(t) \cdot \zeta_{g,A}(t), m_{l,B}(t) + m_g(t) \cdot \zeta_{g,B}(t), m_{l,C}(t) + m_g(t) \cdot \zeta_{g,C}(t), m_{l,D}(t) + m_g(t) \cdot \zeta_{g,D}(t), p(t), T(t), x_A(t), x_B(t), x_C(t), x_D(t))_9$$

$$m_g(t) = UVm\_Flash(xU(t), Vol, m(t), m_{l,A}(t) + m_g(t) \cdot \zeta_{g,A}(t), m_{l,B}(t) + m_g(t) \cdot \zeta_{g,B}(t), m_{l,C}(t) + m_g(t) \cdot \zeta_{g,C}(t), m_{l,D}(t) + m_g(t) \cdot \zeta_{g,D}(t), p(t), T(t), x_A(t), x_B(t), x_C(t), x_D(t))_{10}$$

$$V_l(t) = UVm\_Flash(xU(t), Vol, m(t), m_{l,A}(t) + m_g(t) \cdot \zeta_{g,A}(t), m_{l,B}(t) + m_g(t) \cdot \zeta_{g,B}(t), m_{l,C}(t) + m_g(t) \cdot \zeta_{g,C}(t), m_{l,D}(t) + m_g(t) \cdot \zeta_{g,D}(t), p(t), T(t), x_A(t), x_B(t), x_C(t), x_D(t))_{11}$$

$$V_g(t) = UVm\_Flash(xU(t), Vol, m(t), m_{l,A}(t) + m_g(t) \cdot \zeta_{g,A}(t), m_{l,B}(t) + m_g(t) \cdot \zeta_{g,B}(t), m_{l,C}(t) + m_g(t) \cdot \zeta_{g,C}(t), m_{l,D}(t) + m_g(t) \cdot \zeta_{g,D}(t), p(t), T(t), x_A(t), x_B(t), x_C(t), x_D(t))_{12}$$

$$T(t) = UVm\_Flash(xU(t), Vol, m(t), m_{l,A}(t) + m_g(t) \cdot \zeta_{g,A}(t), m_{l,B}(t) + m_g(t) \cdot \zeta_{g,B}(t), m_{l,C}(t) + m_g(t) \cdot \zeta_{g,C}(t), m_{l,D}(t) + m_g(t) \cdot \zeta_{g,D}(t), p(t), T(t), x_A(t), x_B(t), x_C(t), x_D(t))_{13}$$

$$p(t) = UVm\_Flash(xU(t), Vol, m(t), m_{l,A}(t) + m_g(t) \cdot \zeta_{g,A}(t), m_{l,B}(t) + m_g(t) \cdot \zeta_{g,B}(t), m_{l,C}(t) + m_g(t) \cdot \zeta_{g,C}(t), m_{l,D}(t) + m_g(t) \cdot \zeta_{g,D}(t), p(t), T(t), x_A(t), x_B(t), x_C(t), x_D(t))_{14}$$

DAE-System lösen



$$Lsg(Vol, Temp, m_{0,A}, m_{0,B}, m_{0,C}, m_{0,D}, x_0, t_{end}, n) := \text{odesolve} \left( \begin{matrix} m_{L,A}(t) \\ m_{L,B}(t) \\ m_{L,C}(t) \\ m_{L,D}(t) \\ m_{N_2}(t) \\ m(t) \\ x_U(t) \\ T(t) \\ p(t) \\ x_A(t) \\ x_B(t) \\ x_C(t) \\ x_D(t) \\ y_A(t) \\ y_B(t) \\ y_C(t) \\ y_D(t) \\ y_{N_2}(t) \\ \zeta_{L,A}(t) \\ \zeta_{L,B}(t) \\ \zeta_{L,C}(t) \\ \zeta_{L,D}(t) \\ \zeta_{g,A}(t) \\ \zeta_{g,B}(t) \\ \zeta_{g,C}(t) \\ \zeta_{g,D}(t) \\ \zeta_{g,N_2}(t) \\ m_l(t) \\ m_g(t) \\ V_l(t) \\ V_g(t) \end{matrix} \right), t_{end}, n$$

Startmasse im Reaktor Komponente:

$$m_{1,A} := 0.051 \text{ kg} \quad m_{1,B} := 0.006408 \text{ kg} \quad m_{1,C} := 0 \text{ kg} \quad m_{1,D} := 0 \text{ kg}$$

Starttemperatur:

$$T_1 := 66 \text{ }^\circ\text{C}$$

Reaktorvolumen:

$$V_1 := 0.07 \text{ L}$$

Startzeit, Endzeit, Schrittlänge, Schrittzahl, Kinetikparameter:

$$t_{start_1} := 0 \text{ s} \quad t_{end_1} := 15 \text{ min} \quad \Delta t_1 := 0.01 \text{ min} \quad n_1 := \frac{t_{end_1} - t_{start_1}}{\Delta t_1} = 1500$$

$$x_1 := \text{Startbed}(V_1, T_1, m_{1,A}, m_{1,B}, m_{1,C}, m_{1,D})_{40} = 0.714$$

Startmasse im Reaktor Komponente:

$$m_{2,A} := 0.04915 \text{ kg} \quad m_{2,B} := 0.03085 \text{ kg} \quad m_{2,C} := 0 \text{ kg} \quad m_{2,D} := 0 \text{ kg}$$

Starttemperatur:

$$T_2 := 24.5 \text{ }^\circ\text{C}$$

Reaktorvolumen:

$$V_2 := 0.11 \text{ L}$$

Startzeit, Endzeit, Schrittlänge, Schrittzahl, Kinetikparameter:

$$t_{start_2} := 0 \text{ s} \quad t_{end_2} := 166 \text{ min} \quad \Delta t_2 := 0.01 \text{ min} \quad n_2 := \frac{t_{end_2} - t_{start_2}}{\Delta t_2} = 16600$$

$$x_2 := \text{Startbed}(V_2, T_2, m_{2,A}, m_{2,B}, m_{2,C}, m_{2,D})_{40} = 0.333$$

Startmasse im Reaktor Komponente:

$$m_{3,A} := 0.03656 \text{ kg} \quad m_{3,B} := 0.02302 \text{ kg} \quad m_{3,C} := 0 \text{ kg} \quad m_{3,D} := 0 \text{ kg}$$

Starttemperatur:

$$T_3 := 24.75 \text{ }^\circ\text{C}$$

Reaktorvolumen:

$$V_3 := 0.082 \text{ L}$$

Startzeit, Endzeit, Schrittlänge, Schrittzahl, Kinetikparameter:

$$t_{start_3} := 0 \text{ s} \quad t_{end_3} := 166 \text{ min} \quad \Delta t_3 := 0.01 \text{ min} \quad n_3 := \frac{t_{end_3} - t_{start_3}}{\Delta t_3} = 16600$$

$$x_3 := \text{Startbed}(V_3, T_3, m_{3,A}, m_{3,B}, m_{3,C}, m_{3,D})_{40} = 0.333$$

$$\begin{bmatrix} m_{l_{A1}} \\ \vdots \end{bmatrix} := Lsg(V_1, T_1, m_{1_A}, m_{1_B}, m_{1_C}, m_{1_D}, x_1, t_{end_1}, n_1)$$

Startmasse im Reaktor Komponente:

$$m_{4_A} := 6.0586 \text{ kg}$$

$$m_{4_B} := 1.9014 \text{ kg}$$

$$m_{4_C} := 0 \text{ kg}$$

$$m_{4_D} := 0 \text{ kg}$$

Starttemperatur:

$$T_4 := 29.5 \text{ }^\circ\text{C}$$

Reaktorvolumen:

$$V_4 := 10 \text{ L}$$

Startzeit, Endzeit, Schrittlänge, Schrittzahl, Kinetikparameter:

$$t_{start_4} := 0 \text{ s}$$

$$t_{end_4} := 93 \text{ min}$$

$$\Delta t_4 := 0.001 \text{ min}$$

$$n_4 := \frac{t_{end_4} - t_{start_4}}{\Delta t_4} = 93000$$

$$x_4 := Startbed(V_4, T_4, m_{4_A}, m_{4_B}, m_{4_C}, m_{4_D})_{40} = 0.5$$

$$\begin{bmatrix} m_{l_{A4}} \\ \vdots \end{bmatrix} := Lsg(V_4, T_4, m_{4_A}, m_{4_B}, m_{4_C}, m_{4_D}, x_4, t_{end_4}, n_4)$$

$$\begin{bmatrix} m_{l_{A2}} \\ \vdots \end{bmatrix} := Lsg(V_2, T_2, m_{2_A}, m_{2_B}, m_{2_C}, m_{2_D}, x_2, t_{end_2}, n_2)$$

Startmasse im Reaktor Komponente:

$$m_{5_A} := 0.4918 \text{ kg}$$

$$m_{5_B} := 0.3078 \text{ kg}$$

$$m_{5_C} := 0 \text{ kg}$$

$$m_{5_D} := 0 \text{ kg}$$

Starttemperatur:

$$T_5 := 15.5 \text{ }^\circ\text{C}$$

Reaktorvolumen:

$$V_5 := 1 \text{ L}$$

Startzeit, Endzeit, Schrittlänge, Schrittzahl, Kinetikparameter:

$$t_{start_5} := 0 \text{ s}$$

$$t_{end_5} := 316 \text{ min}$$

$$\Delta t_5 := 0.001 \text{ min}$$

$$n_5 := \frac{t_{end_5} - t_{start_5}}{\Delta t_5} = 316000$$

$$x_5 := Startbed(V_5, T_5, m_{5_A}, m_{5_B}, m_{5_C}, m_{5_D})_{40} = 0.334$$

$$\begin{bmatrix} m_{l_{A5}} \\ \vdots \end{bmatrix} := Lsg(V_5, T_5, m_{5_A}, m_{5_B}, m_{5_C}, m_{5_D}, x_5, t_{end_5}, n_5)$$

$$\begin{bmatrix} m_{l_{A3}} \\ \vdots \end{bmatrix} := Lsg(V_3, T_3, m_{3_A}, m_{3_B})$$