

Let a function be defined with some parameters p_1, p_2, \dots , etc.

$$y = f(x, p_1, p_2, \dots, p_n)$$

then

$$dy = \left(\frac{\partial f}{\partial x} \right) \cdot dx + \sum_{k=1}^n \left[\left(\frac{\partial f}{\partial p_k} \right) \cdot dp_k \right]$$

and can write

$$\frac{dy}{y} = \frac{x}{y} \cdot \left(\frac{\partial f}{\partial x} \right) \cdot \left(\frac{dx}{x} \right) + \sum_{k=1}^n \left[\frac{p_k}{y} \cdot \left(\frac{\partial f}{\partial p_k} \right) \cdot \frac{dp_k}{p_k} \right]$$

or

$$\frac{dy}{y} = S_x \cdot \left(\frac{dx}{x} \right) + \sum_{k=1}^n \left[S_{(p_k)} \cdot \frac{dp_k}{p_k} \right]$$

where the sensitivity S is defined as

$$S_{(p_k)} = \frac{p_k}{y} \cdot \left(\frac{\partial f}{\partial p_k} \right)$$

In general, the sensitivities are functions of x , and the various nominal values of the parameters, and are not constant. They relate the fractional change in f for a given fractional change in the corresponding parameter, e.g., a sensitivity of 3 means that a 1% change in the parameter gives a 3% change in the function.