

$$\int_x^1 t$$

$$F1(x, m) := \int_x^1 \frac{\sqrt{(t^2 - x^2)(t^2 - m^2)}}{t} dt$$

$$FF1(x, m) := \frac{F1(x, m)}{1 - m^2 - m^2 \cdot \ln\left(\frac{1}{m}\right)}$$

$$FF1(x, m) := \frac{F1(x, m)}{\frac{1 - m^2}{2} - m^2 \cdot \ln\left(\frac{1}{m}\right)} \quad \text{Normalized function}$$

$$x1(x, m) := \frac{x - m}{1 - m}$$

How do we find a closed-form function, say G1(x1), driven from FF1(x,m)?

We have x1 as:

$$x := 0, 0.001..1 \quad m := 0.7$$

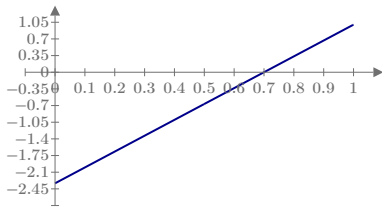
$$x1 := \frac{x - m}{1 - m}$$

Do we have to write x1 as a function? like:

$$x1(x, m) := \frac{x - m}{1 - m}$$

Finally, I would like to compare FF1 and G1 against x1 in plotts.

$$x := 0, 0.001..1 \quad m := 0.7$$



$$x1(x, m)$$

x

$$x1 = \frac{x - m}{1 - m}$$

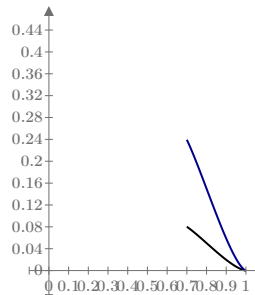
$$x = x1 \cdot (1 - m) + m$$

$$X(x1) := x1 \cdot (1 - m) + m$$

$$F1(0.1, m) = 0.137 + 0.283i$$

$$FF1(0.1, m) = 0.408 + 0.843i$$

Plots don't show in range where result is imaginary, use Re() and Im() to see real and imaginary parts

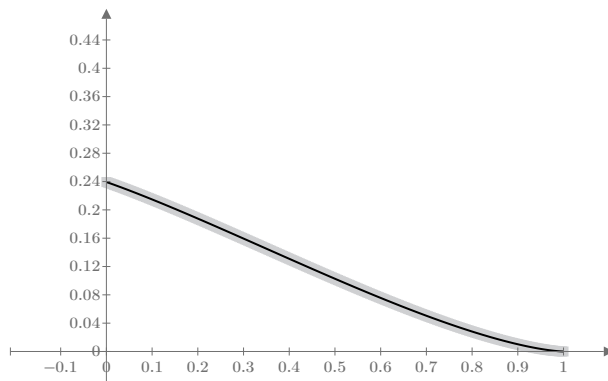


$$F1(x, m)$$

$$FF1(x, m)$$

x

$$G1(x1) := FF1(X(x1), m)$$



$$x1(x, m)$$

$$FF1(X(x1(x, m)), m)$$

$$G1(x1(x, m))$$