

Geometric Nonlinearity-Iterative Solution Approach Implementation

Incremental / Iterative Solution Approach -Newton-Raphson Method

$$E := 500000 \frac{\text{N}}{\text{mm}^2} \quad A := 100 \text{ mm}^2 \quad Z := 25 \text{ mm} \quad L := 2500 \text{ mm} \quad K_S := 1.350 \frac{\text{N}}{\text{mm}} \quad P := -80 \text{ N}$$

$$mIt := 100 \quad \delta := 1 \cdot 10^{-8} \quad n := 15 \quad i := 0..n + 1 \quad \Delta P := \frac{P}{n} = -5.333$$

IncNRSolve($\Delta P, n, \delta, mIt$) :=

$$w_{n+1} \leftarrow 0$$

$$Pa \leftarrow 0$$

$$cIt_n \leftarrow 0$$

for $i \in 1..n$

$$K_t \leftarrow \left[\left(\frac{E \cdot A}{L} \right) \cdot \left(\frac{Z + w_i}{L} \right)^2 \right] + \left[\frac{(E \cdot A)}{L^3} \right] \cdot \left[Z \cdot w_i + \frac{1}{2} \cdot (w_i)^2 \right] + K_S$$

$$\Delta w \leftarrow \frac{\Delta P}{K_t}$$

$$w_{total} \leftarrow w_i + \Delta w$$

$$Pa \leftarrow Pa + \Delta P$$

$$nIt \leftarrow 0$$

while 1

$$nIt \leftarrow nIt + 1$$

$$f \leftarrow \left[\frac{(E \cdot A)}{L^3} \right] \cdot \left(Z^2 \cdot w_{total} + 1.5 \cdot Z \cdot w_{total}^2 + 0.5 w_{total}^3 \right) + K_S \cdot w_{total} - Pa$$

break if $(|f| < \delta) \vee (nIt \geq mIt)$

$$K_t \leftarrow \left[\left(\frac{E \cdot A}{L} \right) \cdot \left(\frac{Z + w_{total}}{L} \right)^2 \right] + \left[\frac{(E \cdot A)}{L^3} \right] \cdot \left[Z \cdot w_{total} + \frac{1}{2} \cdot (w_{total})^2 \right] + K_S$$

$$\delta w \leftarrow \frac{-f}{K_t}$$

$$w_{total} \leftarrow w_{total} + \delta w$$

$$w_{i+1} \leftarrow w_{total}$$

$$cIt_{i \leftarrow nIt}$$

$$\begin{pmatrix} w \\ cIt \end{pmatrix}$$

Increment

Residual Force

Equilibrium Iterations

wNR := IncNRSolve(ΔP , n, δ , mIt)

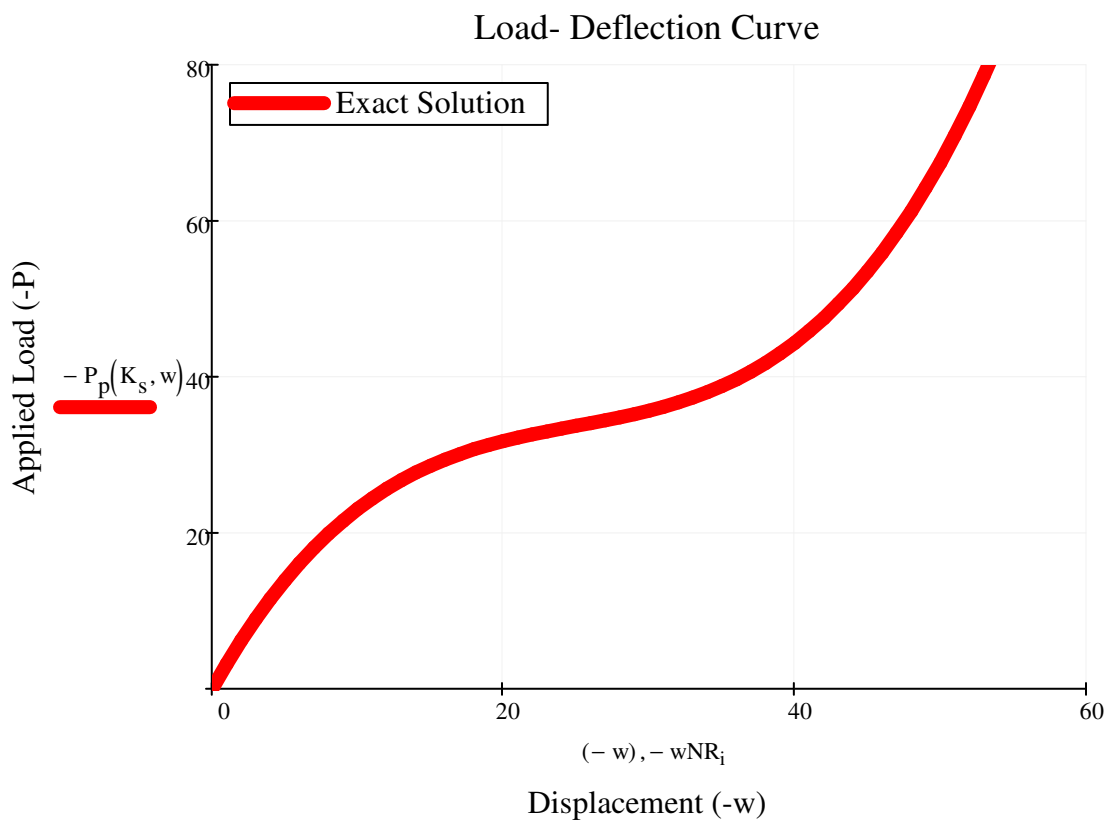
wNRr := wNR₁

cItNR := wNR₂

$$P_p(K_s, w) := \left[\left(\frac{E \cdot A}{L^3} \right) \cdot (Z^2 \cdot w + 1.5 \cdot Z \cdot w^2 + 0.5 \cdot w^3) + K_s \cdot w \right]$$

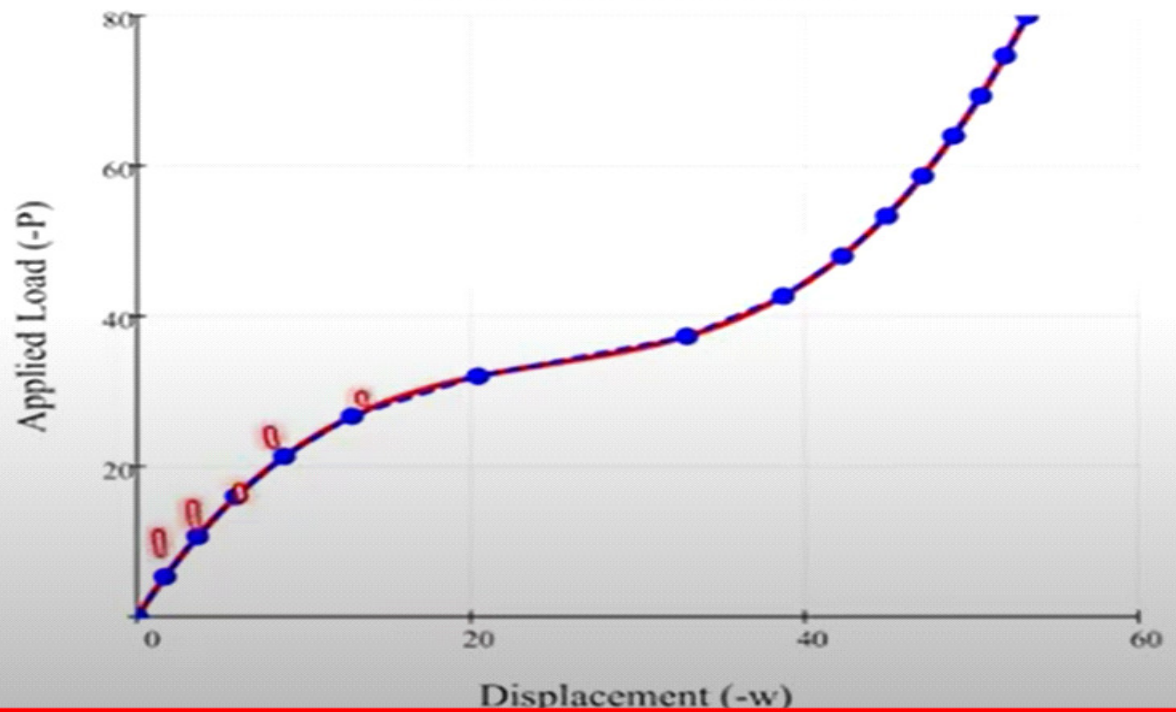
w := 0..-100

I can't get the second plot of Newton Raphson iterative solution(Blue dots) as shown in the picture below this plot. I also need the plot " Number of iterations" vs Increment" shown 2 pictures below



$mlt := 100$ $n := 15$ $i := 1..n + 1$ $P := -80$ $\Delta P := \frac{P}{n}$
 $wNR := IncNRSolve(\Delta P, n, \delta, mlt)$ $wNRr := wNR_1$ $cltNR := wNR_2$

Load-Deflection Curve



- Exact Solution
- Inc/It Solution with Newton Raphson Method

Number of Iterations - Newton Raphson Method

