

Cable length: $L_0 := 15 \cdot \text{m}$

Sections: $N_S := 10$

$i := 0.. N_S - 2$

Min. x: $a := 0 \cdot \text{m}$

Max. x: $b := 10 \cdot \text{m}$

$y_a := 7 \cdot \text{m}$

$y_b := 10 \cdot \text{m}$

Function for sections:

Abschnitte(a, b, x, y) :=

$$\left\{ \begin{array}{l} \Delta s_0 \leftarrow \sqrt{(x_0 - a)^2 + (y_0 - y_a)^2} - \frac{L_0}{N_S} \\ \text{for } i \in 1.. N_S - 2 \\ \Delta s_i \leftarrow \sqrt{(x_i - x_{i-1})^2 + (y_i - y_{i-1})^2} - \frac{L_0}{N_S} \\ \Delta s_9 \leftarrow \sqrt{(b - x_8)^2 + (y_b - y_8)^2} - \frac{L_0}{N_S} \\ \Delta s \end{array} \right.$$

Potential Energy:

$m_0 := 1 \cdot \text{kg}$

$$E_{\text{pot}}(x, y) := m_0 \cdot g \cdot \left(y_a + \sum_{i=0}^8 y_i + y_b \right)$$

Initial values:

$$x_i := a + (i + 1) \cdot \frac{b - a}{10}$$

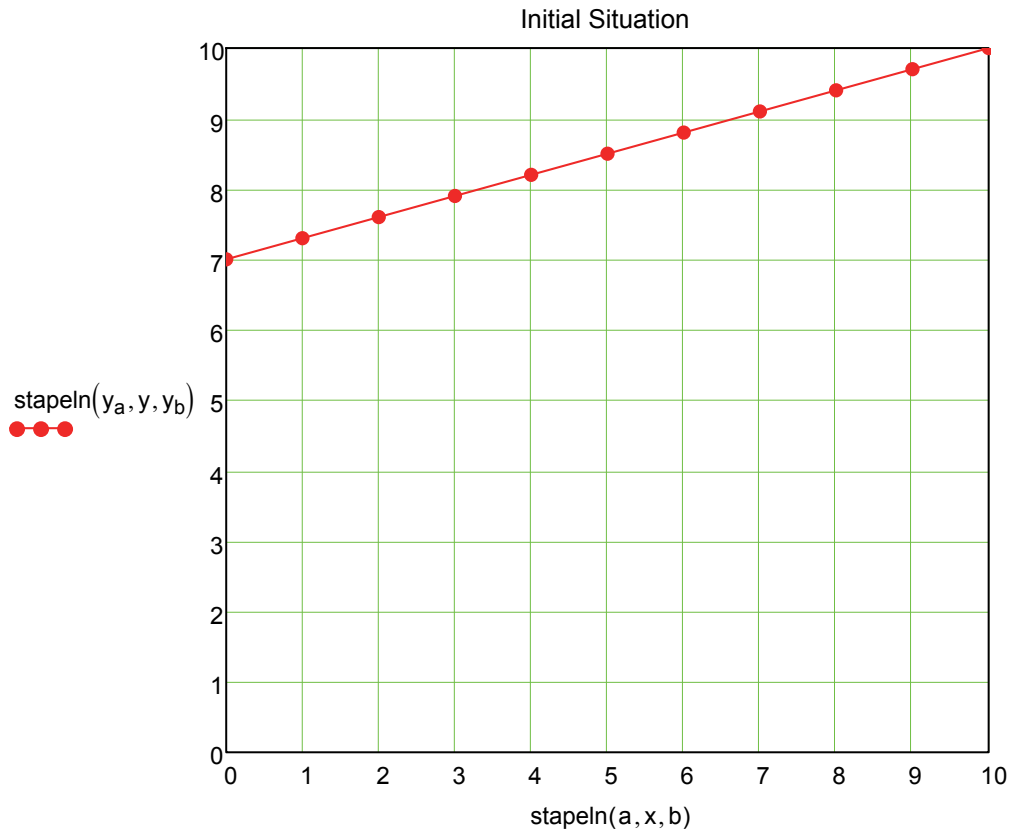
$$y_i := y_a + (i + 1) \cdot \frac{y_b - y_a}{10}$$

Abschnitte(a, b, x, y) =

$$\begin{pmatrix} -0.456 \\ -0.456 \\ -0.456 \\ -0.456 \\ -0.456 \\ -0.456 \\ -0.456 \\ -0.456 \\ -0.456 \\ -0.456 \end{pmatrix} \cdot \text{m}$$

$$\frac{\sqrt{(b - a)^2 + (y_b - y_a)^2}}{N_S} - \frac{L_0}{N_S} = -0.456 \cdot \text{m}$$

$$E_{\text{pot}}(x, y) = 916.922 \cdot \text{J}$$



Minimize for cable:

Vorgabe

Abschnitte(a, b, x, y) = 0

$\begin{pmatrix} x \\ y \end{pmatrix} := \text{Minimieren}(E_{\text{pot}}, x, y)$

ERR = 8.281×10^{-10}

TOL = 1×10^{-8}

CTOL = 1×10^{-9}

Abschnitte(a, b, x, y) =

	0
0	$1.668 \cdot 10^{-13}$
1	$5.915 \cdot 10^{-11}$
2	$1.468 \cdot 10^{-11}$
3	$2.605 \cdot 10^{-10}$
4	$1.678 \cdot 10^{-11}$
5	$2.807 \cdot 10^{-10}$
6	$6.59 \cdot 10^{-13}$
7	$1.279 \cdot 10^{-10}$
8	$6.22 \cdot 10^{-10}$
9	$3.631 \cdot 10^{-10}$

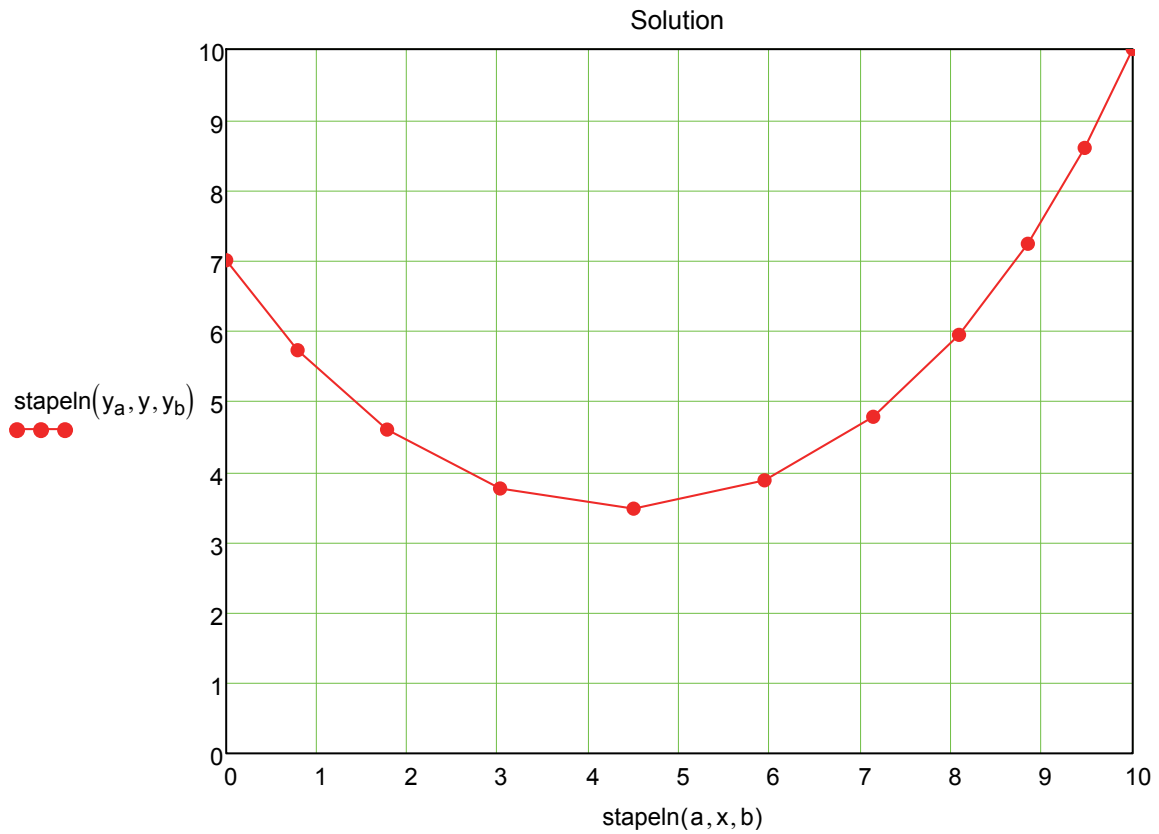
·m

$E_{\text{pot}}(x, y) = 637.164 \cdot \text{J}$

To get Valery's value:

$E_{\text{pot}}(x, y) - m_0 \cdot g \cdot (y_a + y_b) = 470.451 \cdot \text{J}$

$E_{\text{pot}}(x, y) - m_0 \cdot g \cdot (y_a + y_b) = 47.973 \cdot \text{kgf} \cdot \text{m}$



Maximize for arch:

Vorgabe

Abschnitte(a, b, x, y) = 0

$$\begin{pmatrix} x \\ y \end{pmatrix} := \text{Maximieren}(E_{\text{pot}}, x, y)$$

$$\text{ERR} = 9.508 \times 10^{-10}$$

$$\text{TOL} = 1 \times 10^{-8}$$

$$\text{CTOL} = 1 \times 10^{-9}$$

Abschnitte(a, b, x, y) =

	0
0	1.885 · 10 ⁻¹³
1	3.193 · 10 ⁻¹¹
2	8.249 · 10 ⁻¹⁰
3	4.083 · 10 ⁻¹⁰
4	5.805 · 10 ⁻¹²
5	1.427 · 10 ⁻¹⁰
6	1.489 · 10 ⁻¹⁰
7	5.601 · 10 ⁻¹¹
8	8.652 · 10 ⁻¹¹
9	5.163 · 10 ⁻¹¹

·m

$$E_{\text{pot}}(x, y) = 1.197 \times 10^3 \cdot \text{J}$$

To get Valery's value:

$$E_{\text{pot}}(x, y) - m_0 \cdot g \cdot (y_a + y_b) = 1.03 \times 10^3 \cdot \text{J}$$

$$E_{\text{pot}}(x, y) - m_0 \cdot g \cdot (y_a + y_b) = 105.027 \cdot \text{kgf} \cdot \text{m}$$

