



UNIVERSITY
OF MANITOBA

Introduction to Basics of FEA and Pro/MECHANICA

25.353 Lecture Series

G. Gary Wang

Department of Mechanical and Manufacturing Engineering
The University of Manitoba

What is Pro/MECHANICA

Pro/MECHANICA is an integrated and also independent Finite Element Analysis (FEA) module of Pro/E CAD/CAM system.

- Pro/MECHANICA Structure
- Pro/MECHANICA Thermal
- Pro/MECHANICA Motion

Pro/MECHANICA Structure

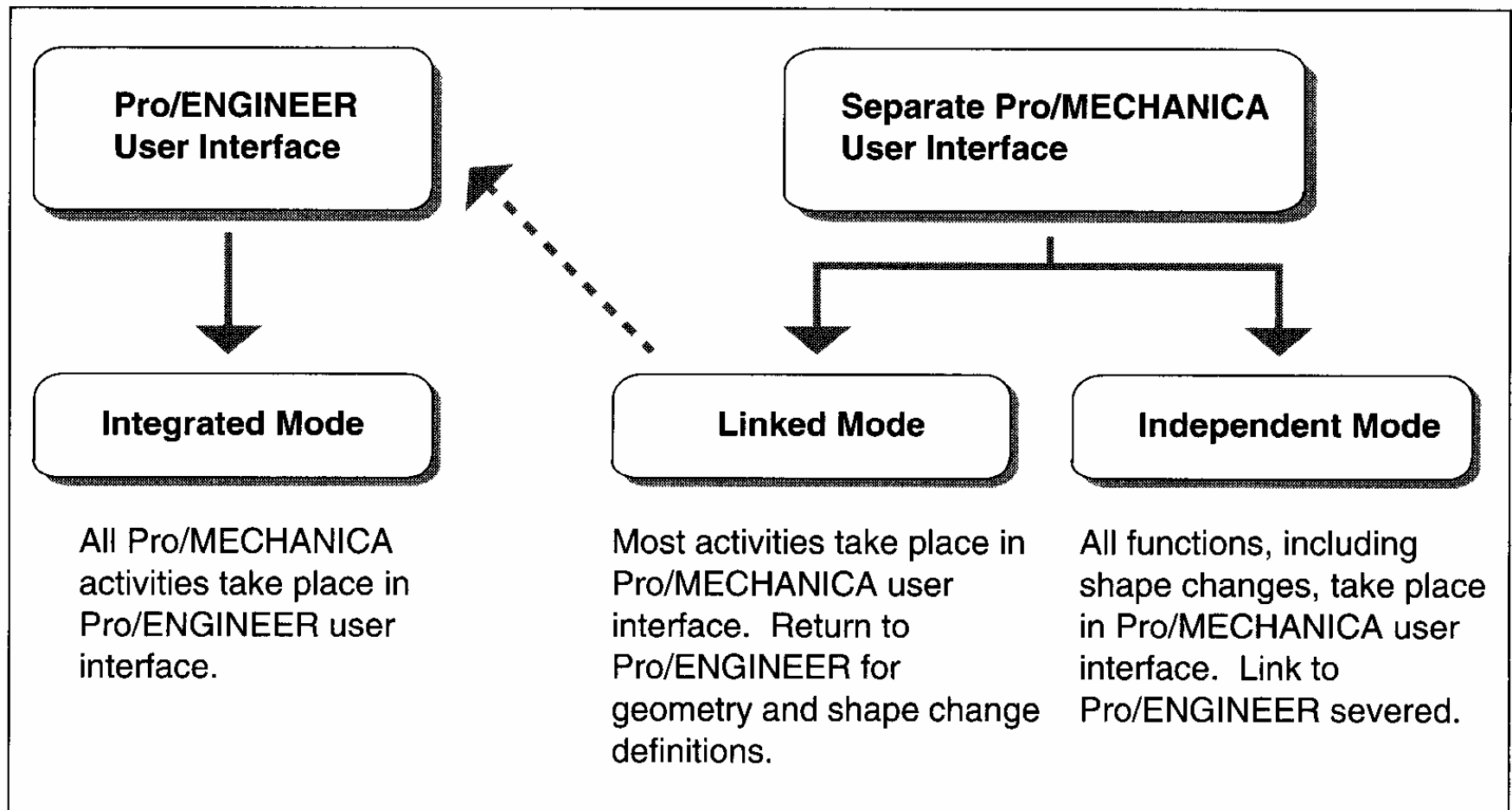
- Linear static stress analysis
- Modal analysis (mode shapes and natural frequencies)
- Buckling analysis
- Large deformation analysis (non-linear)

- **Pro/MECHANICA THERMAL** — a thermal analysis package that features many of the capabilities of Structure along with heat transfer analysis and thermal design optimization.
- **Pro/MECHANICA MOTION** — a motion analysis package that provides mechanism modeling and mechanism design optimization capabilities. This product enables you to analyze your mechanism's motion and forces.

Operation Modes

- **Integrated**
 - Easy design change
 - Cannot see mesh, less FEA
- **Linked**
 - Both interfaces; combination of the other two modes
 - Comparably more difficult to use
- **Independent**
 - Strong FEA
 - Independent to Pro/E; hard to modify

Operation Modes



Modes of Operation

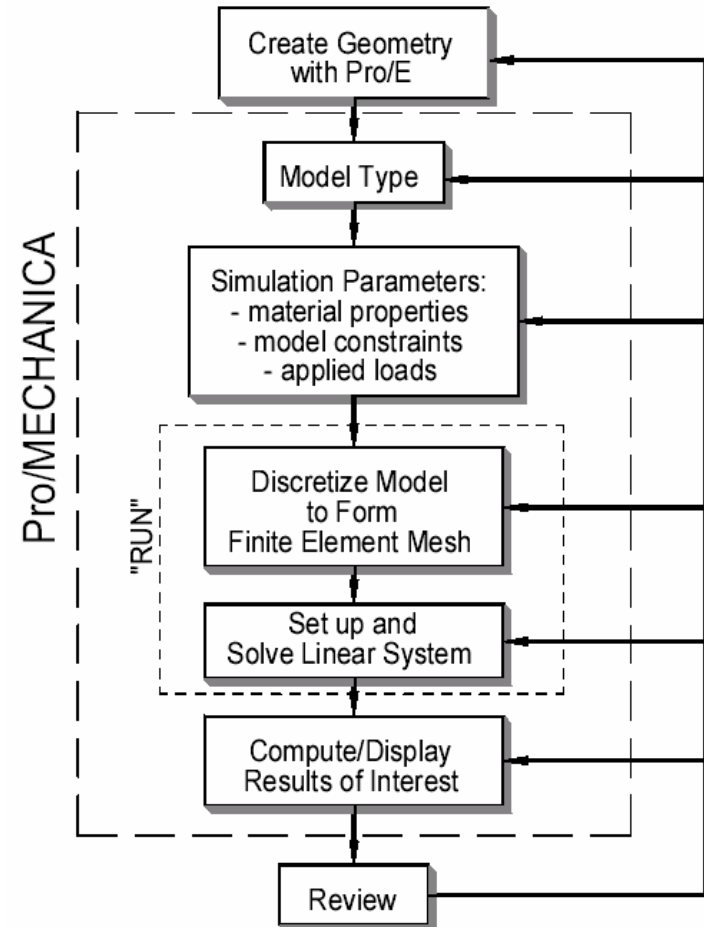
Integrated Mode	Independent Mode
Pro/E interface	Pro/M interface
all analyses available	all analyses available
2D and 3D models	2D and 3D models
some measures of results not available	all measures available
some analysis options not available (eg excluding elements)	all options available
all elements generated automatically	element creation manual or automatic
sensitivity and optimization using Pro/E parameters only	sensitivity and optimization uses Pro/M variables

Common Unit System

Quantity	System and Units			
	SI MNS	Metric mm-N-s	English FPS ft-lb-sec	English IPS in-lb-sec
length	m	mm	ft	in
time	s	s	sec	sec
mass	kg	tonne (1000 kg)	slug	lbf-sec ² / in
density	kg/m ³	tonne/mm ³	slug/ft ³	lbf-sec ² / in ⁴
gravity, g	9.81 m/s ²	9810 mm/s ²	32.2 ft/sec ²	386.4 in/sec ²
force	N	N	lbf	lbf
stress, pressure, Young's modulus	N/m ² = Pa	N/mm ² = MPa	lbf/ft ²	lbf/in ² = psi

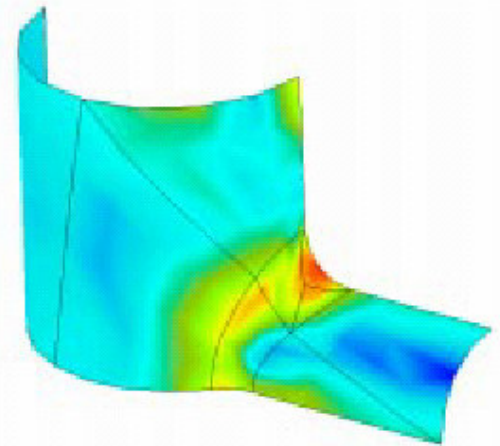
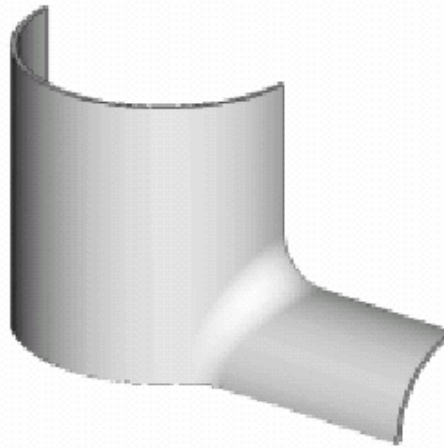
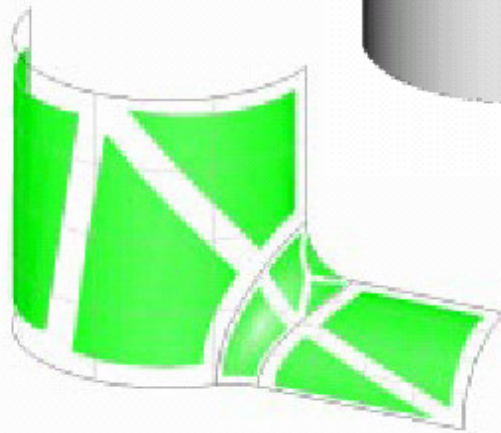
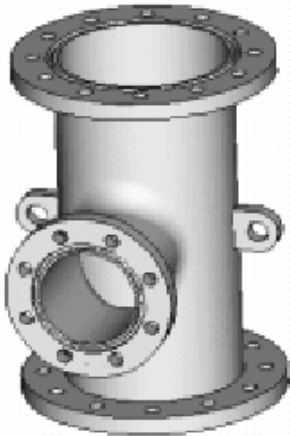
Steps in Preparing an FEA Model for Solution

1. Identify the model type
2. Specify the material properties, model constraints, and applied loads
3. Discretize the geometry to produce a finite element mesh
4. Solve the system of equations
5. Compute items of interest from the solution variables
6. Display and critically review results and, if necessary, repeat the analysis



A CAD Model is NOT a FEA Model!

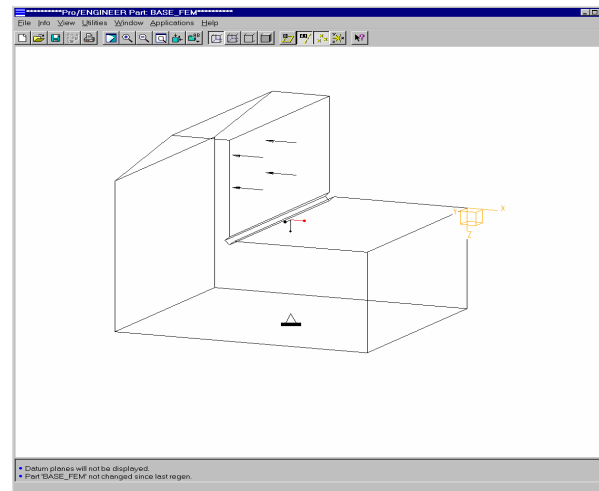
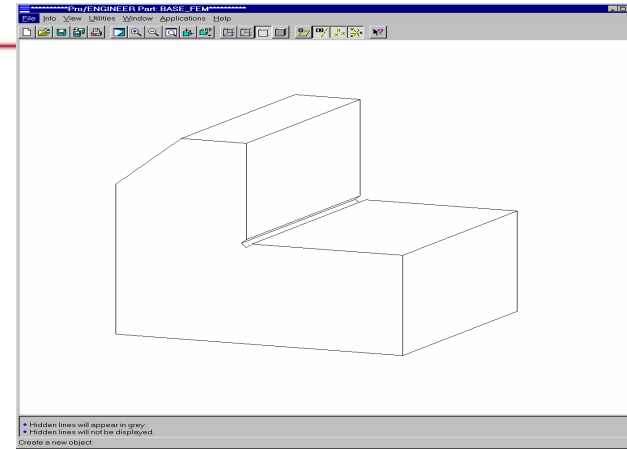
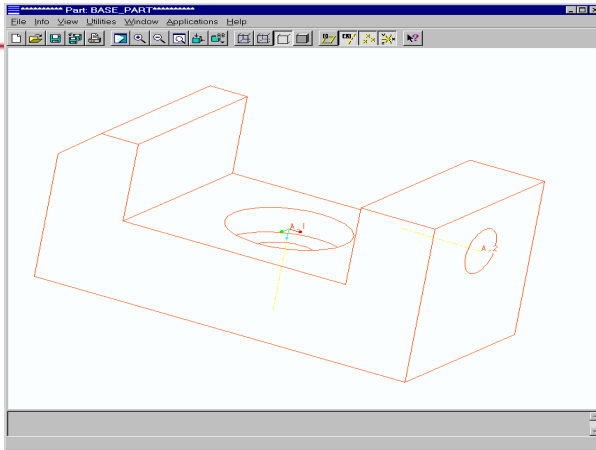
Use the simplest model possible that will yield sufficiently reliable results of interest at the lowest computational cost.



Difference between a CAD & a FEA Model

- A CAD model is to provide a detailed document for manufacturing.
- A FEA model simply captures the *rough geometry* of the design and its *loading conditions*.
 - ◇ Elimination all unimportant design details that have minor effect on the results of FEA.
 - ◇ Use of part symmetry to dramatically reduce the size of the model.
 - ◇ Elimination of uninterested portion of the design.

Involved Models in the Tutorial



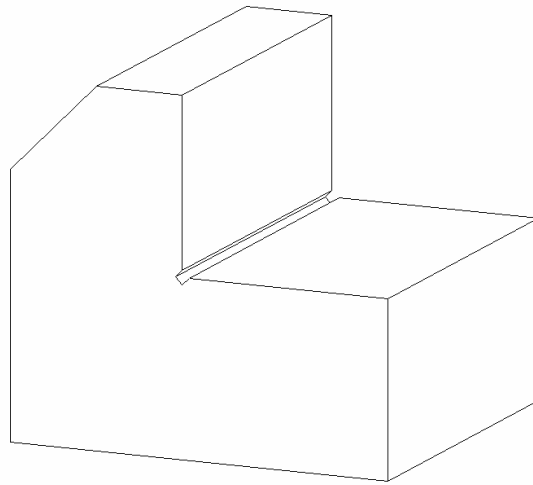
(a) A CAD Model

(b) A Simplified CAD Model

(c) A FEA Model

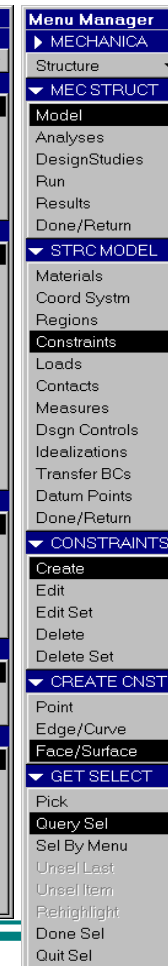
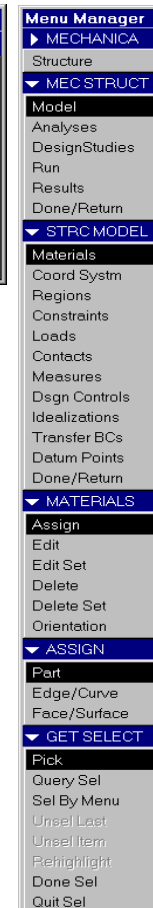
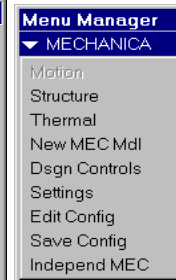
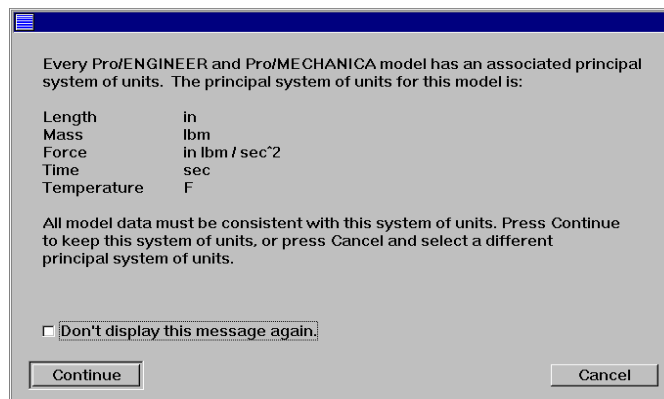
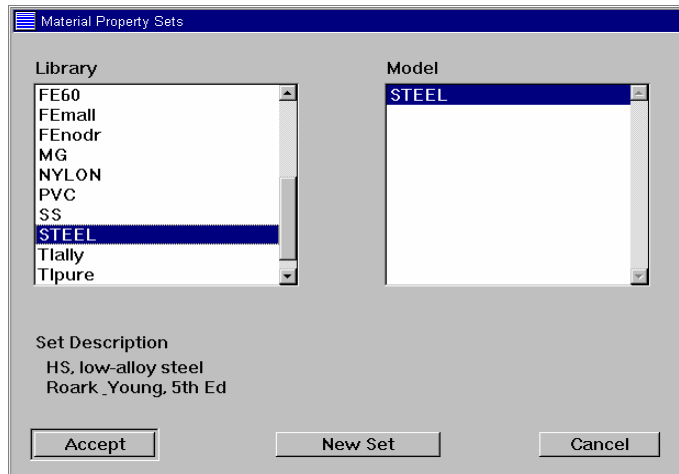
Procedure of the Lab

- Preparation of the Model / Create the geometry in Fig. 49



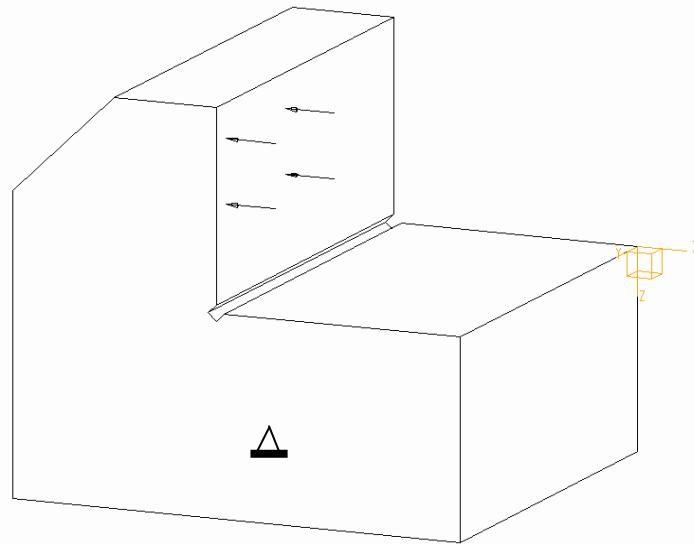
Procedure of the Lab

- Start Pro/Mechanica from Pro/E



Building a FEA Model

- Materials
- Loads
- Constraints



Pre-processing

- Invisible in the Integrated mode

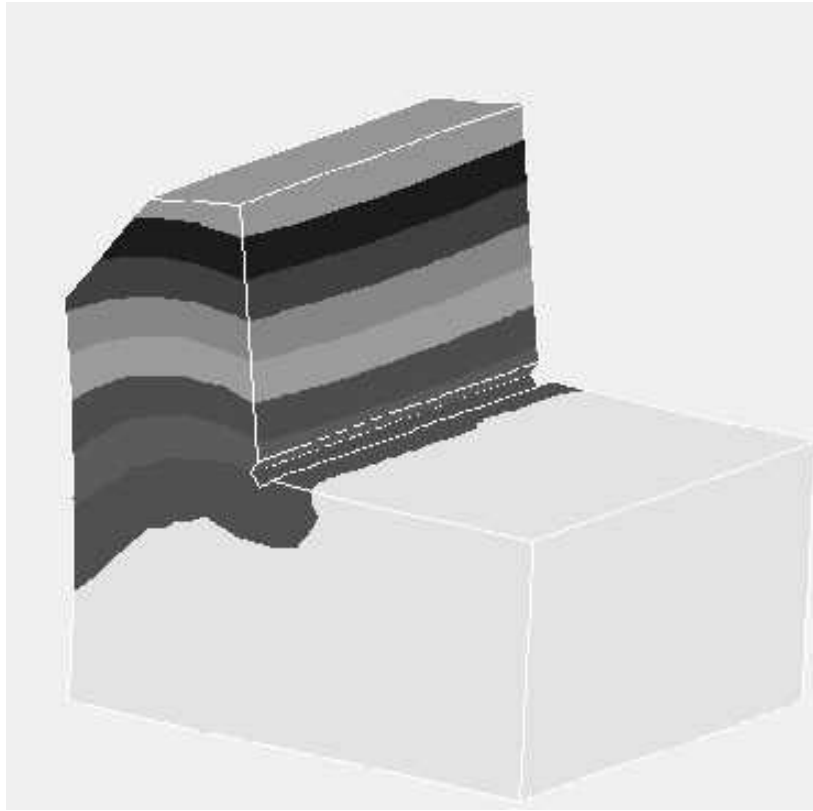
Analysis

- Quick Check
- Multi-pass Adaptive

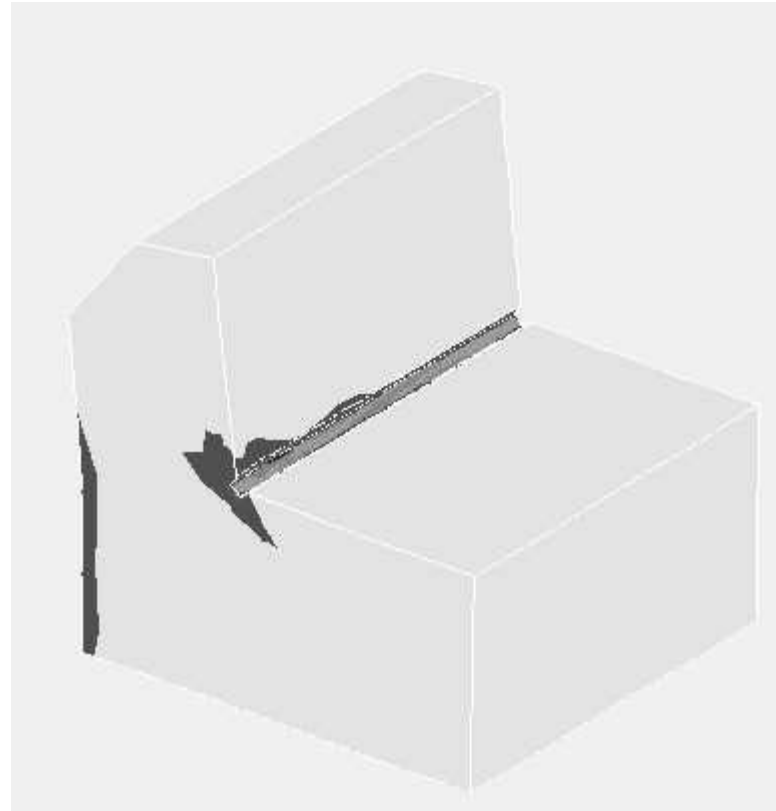
Post-processing

- Displacement
- Von-mises stress
- Strain energy

Result Models

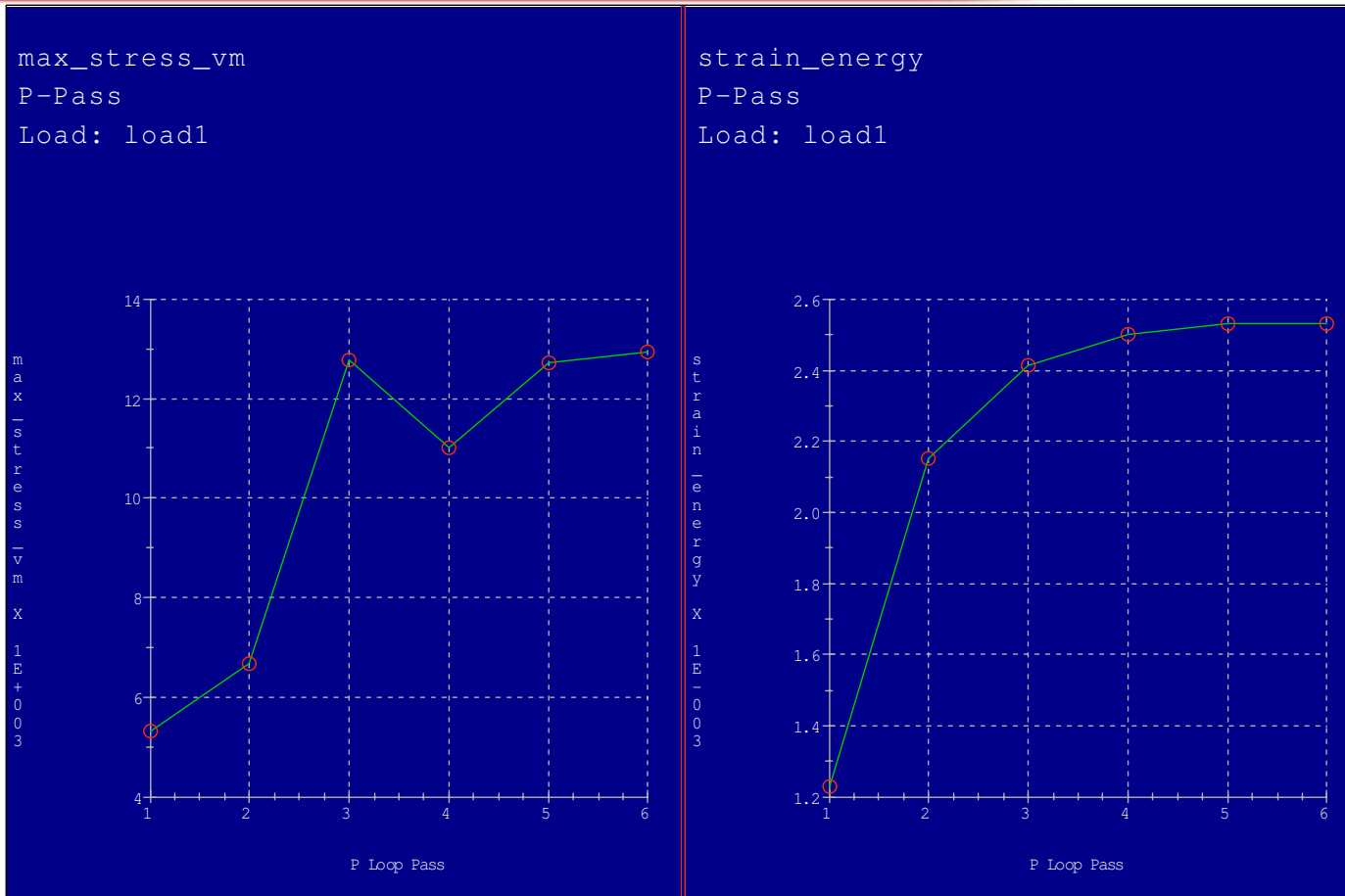


(a) Deformation



(b) Von Mises Stress

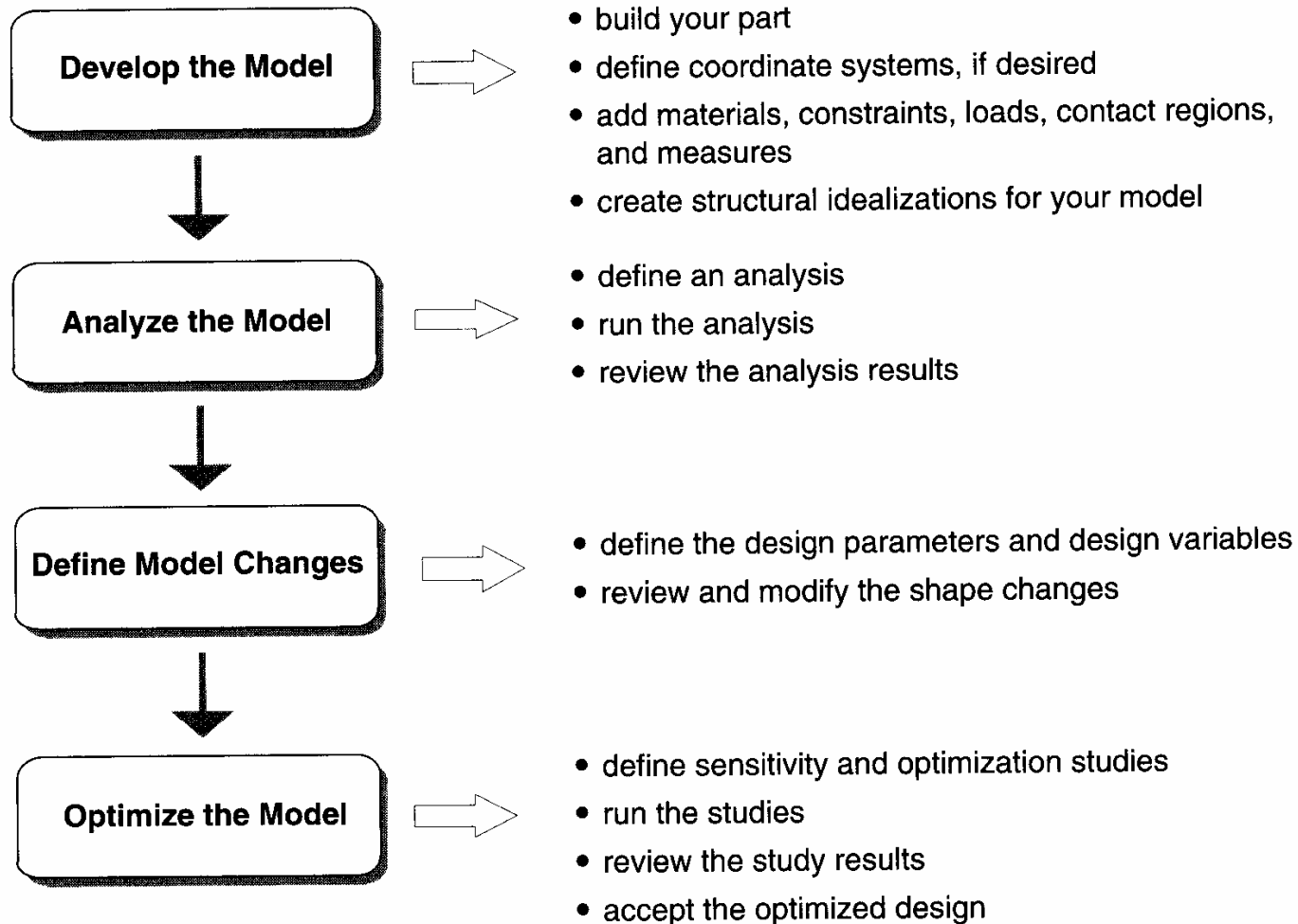
Convergence Check



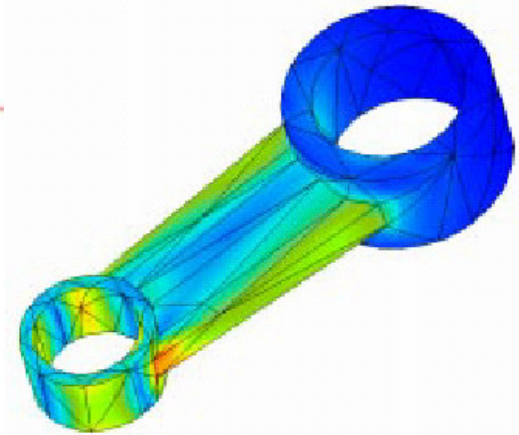
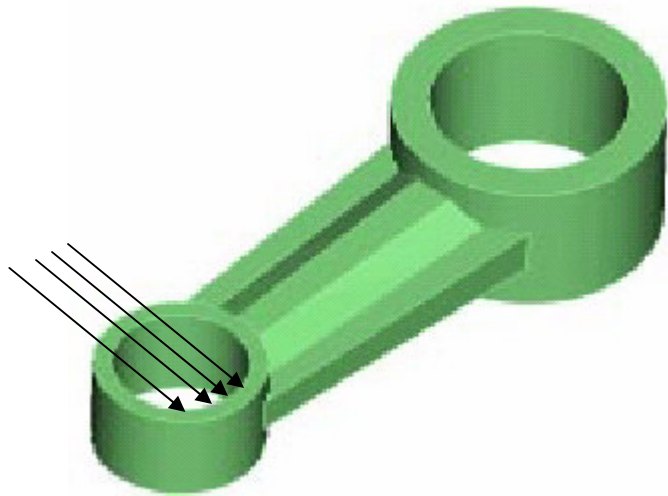
(a) Von Mises

(b) Strain Energy

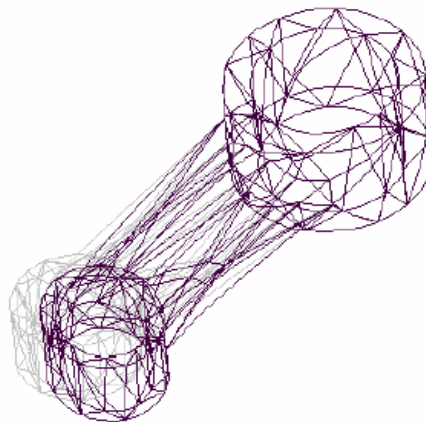
General Design/FEA Cycle



Analysis

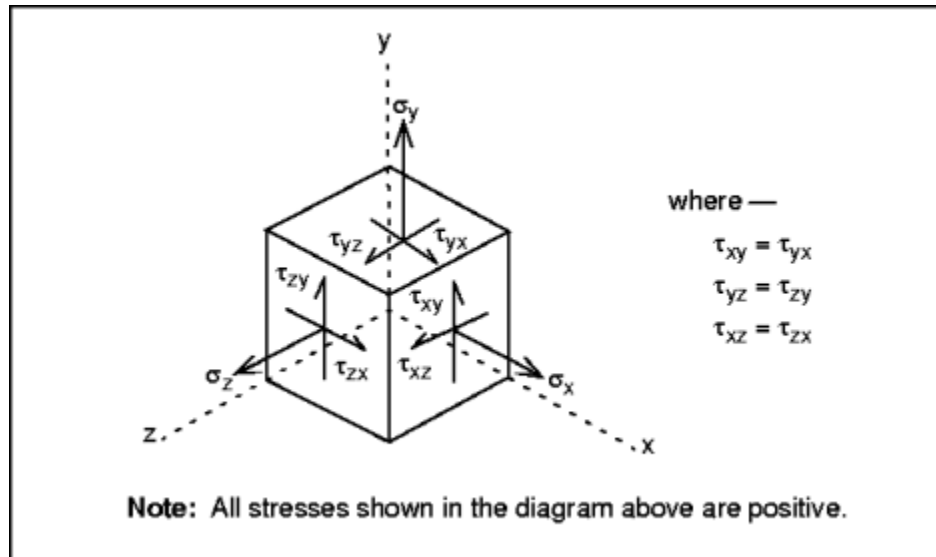


Contours of the Von Mises stress



Total deformation of the part

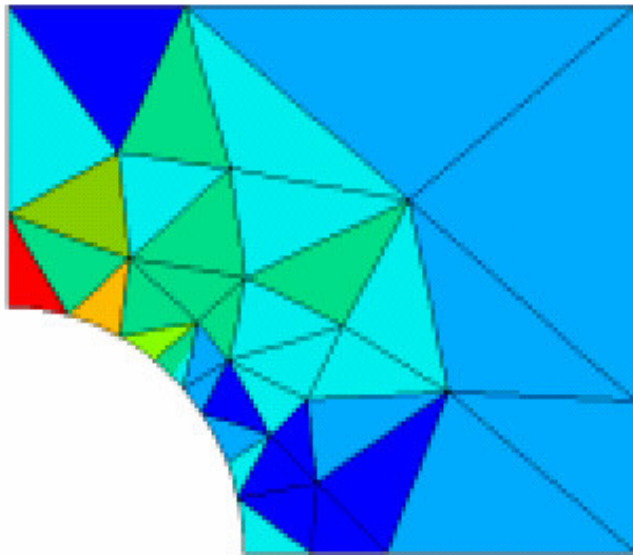
Von Mises Stress



The Von Mises stress is obtained by combining all the stress components at a point

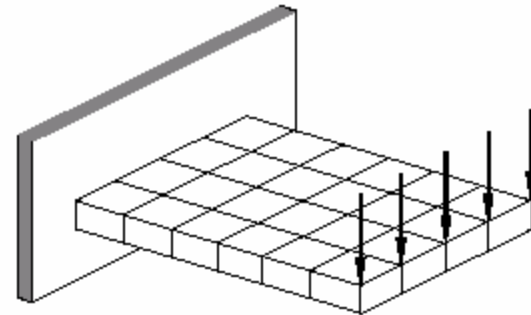
Convergence of FEA

- No FEA solution should be accepted unless the convergence properties have been examined

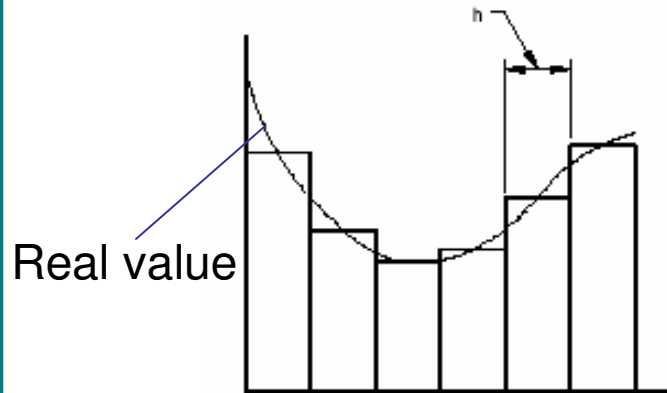


Cost vs. Accuracy

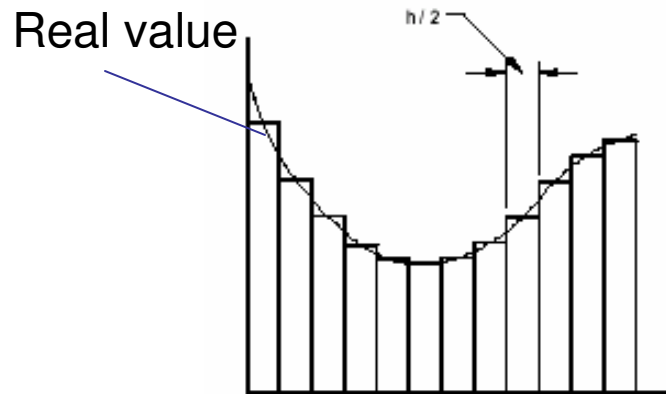
Simulation vs. Experiment



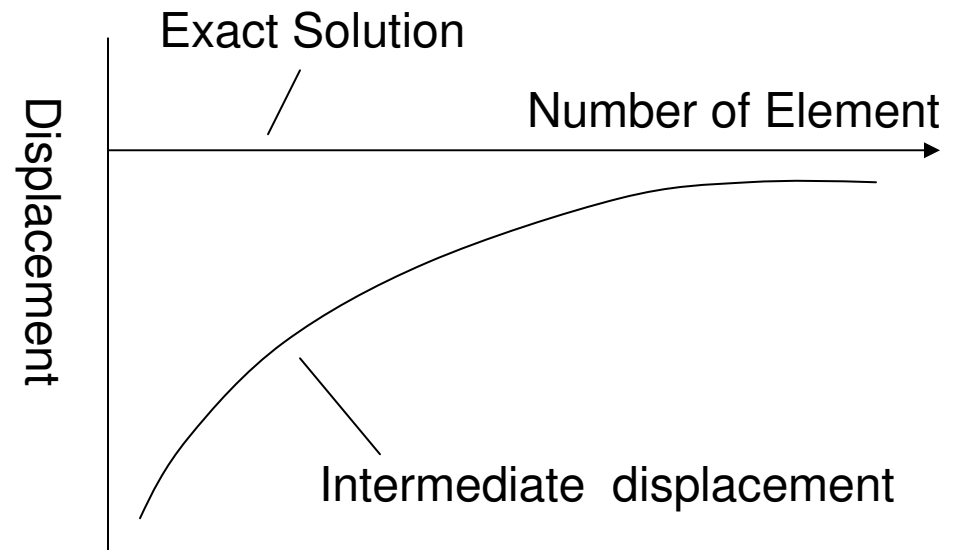
Convergence of H-elements



(a) first order elements lead to constant stress within each element



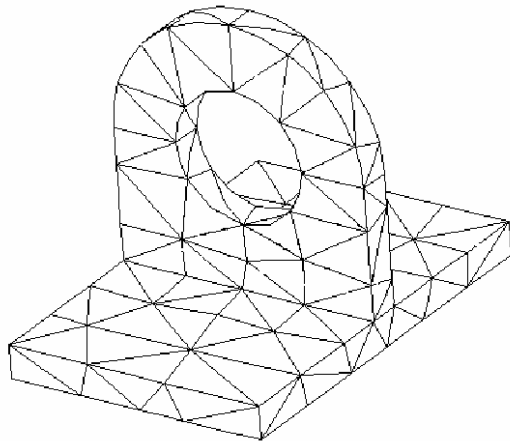
(b) error is reduced by reducing the element size $O(h)$



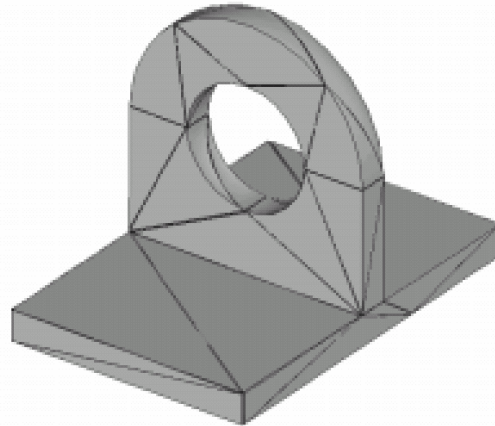
H – size of element

Convergence of P-elements

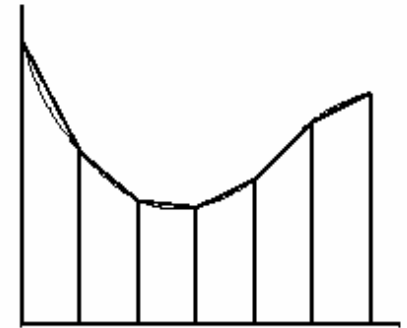
- Up to 9th order polynomials in Pro/MECHANICA
- The same mesh can be used throughout the convergence analysis, rather than recreating meshes or local mesh refinement required by h-codes.
- The mesh is virtually always more coarse and contains fewer elements than h-codes.



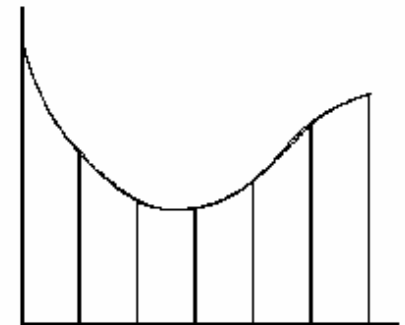
A mesh of h-elements



A mesh of p-elements



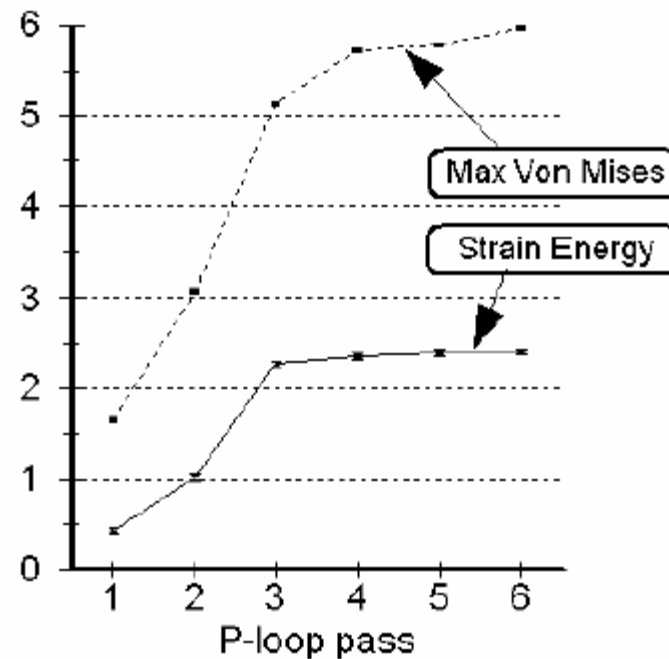
(c) second order element leads to linear stress variation within each element



(d) higher order element will reduce error even further without changing the element size

Convergence of P-elements (Cont'd)

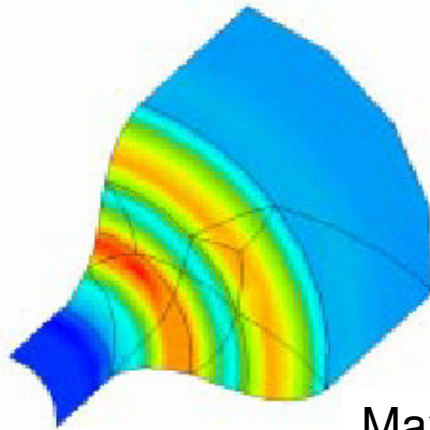
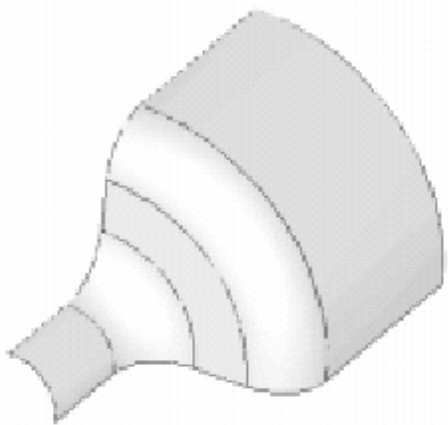
- Automatic mesh generators is more effective for p-elements rather than h-element.
- Mesh is tied directly to the geometry.



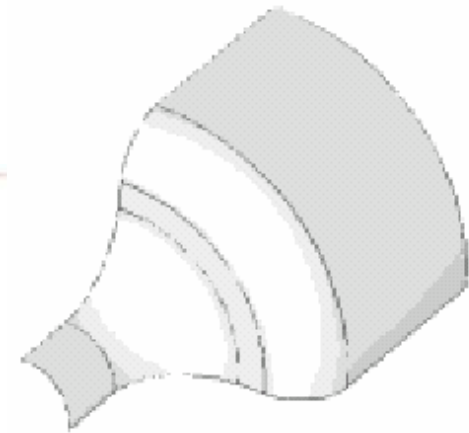
Convergence Methods

- **Quick Check** - the model is run only for a polynomial of order 3. The results of a Quick Check should never be trusted.
- **Single Pass Adaptive** - the single pass adaptive method performs one pass at a low polynomial order, assesses the accuracy of the solution, modifies the p-level of “problem elements”, and does a final pass with some elements raised to an order that should provide reasonable results.
- **Multi-Pass Adaptive** - The ultimate in convergence analysis. Multiple “p-loop” passes are made through the solver, with edge orders of “problem elements” being increased with each pass. This iterative approach continues until either the solution converges to a specified accuracy or the maximum specified edge order (default 6, maximum 9) is reached.

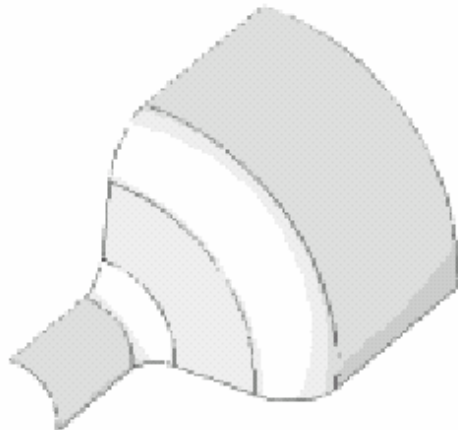
Sensitivity Study



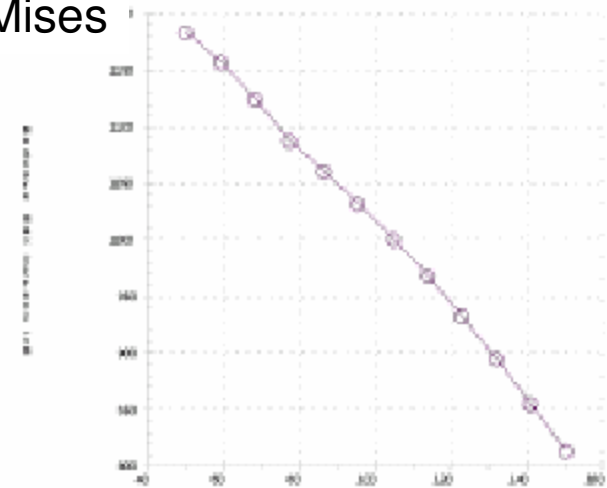
Max Von Mises



Max fillet radius



Min fillet radius



Fillet radius

Design Optimization

Optimization: A fascinating, useful, mathematical tool

An Optimization Model:

Min Mass of a Mug as a function of dimensions (D: Diameter, Height, Thickness) -- *Objective*

Subject to

Mug Volume \geq A Constant -- *Inequality Constraint*

$H/D = 1.65$ -- *Equality Constraint*

$D, H, T > 0$ -- *Variables*

Find: $D^*, H^*, \text{ and } T^*$ -- *Optimum*

Design Optimization

Another Optimization Model:

Min Manufacturing Cost of the Mug -- *Objective*

Subject to

Mug Volume $>$ Constant 1 -- *Inequality Constraint*

Mug Mass \leq Constant 2

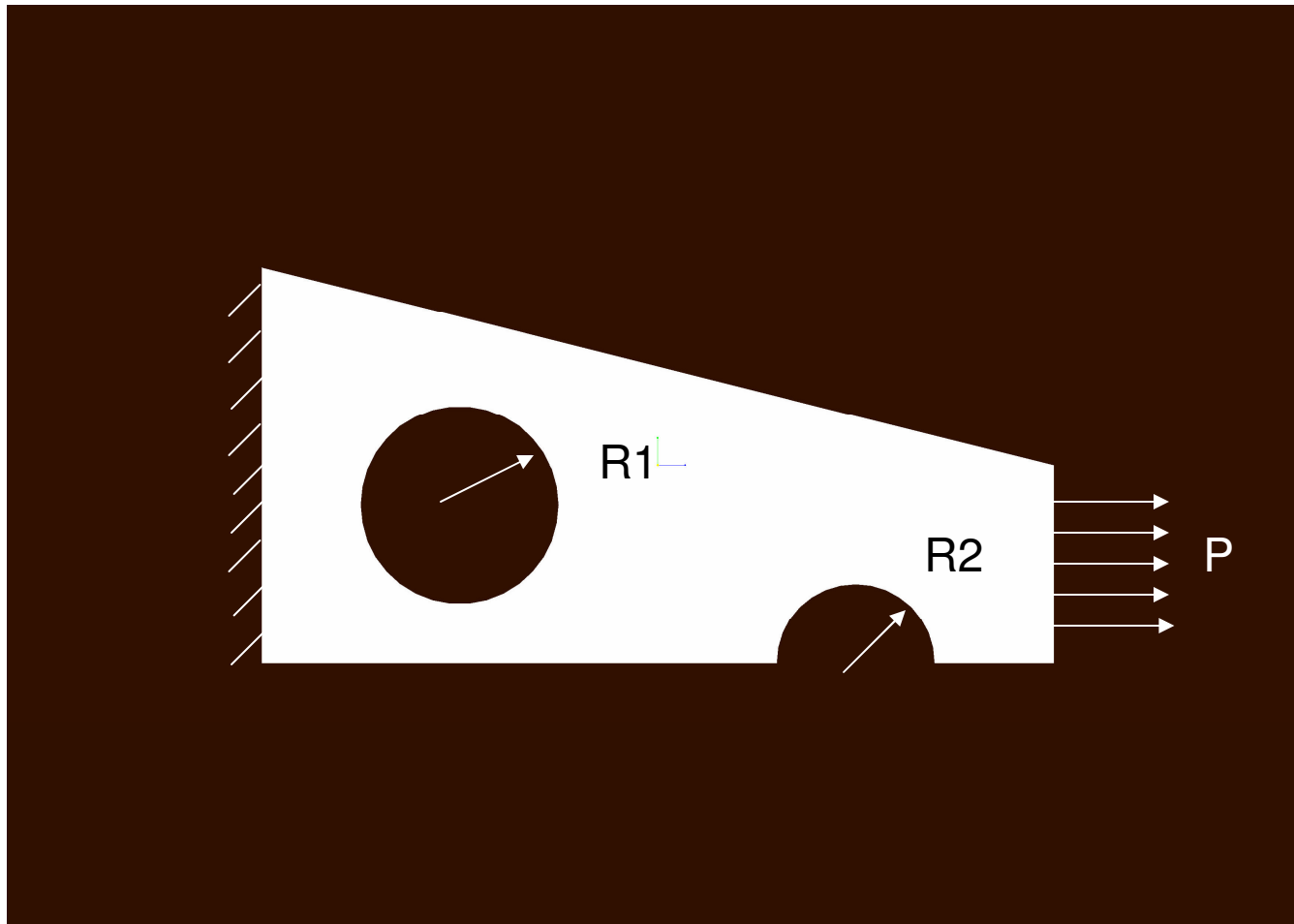
Strength $>$ Constant 3

H/D = 1.65 -- *Equality Constraint*

D, H, T, material, tolerances, etc. -- *Variables*

Find: D*, H*, T*, etc.* -- *Optimum*

Example



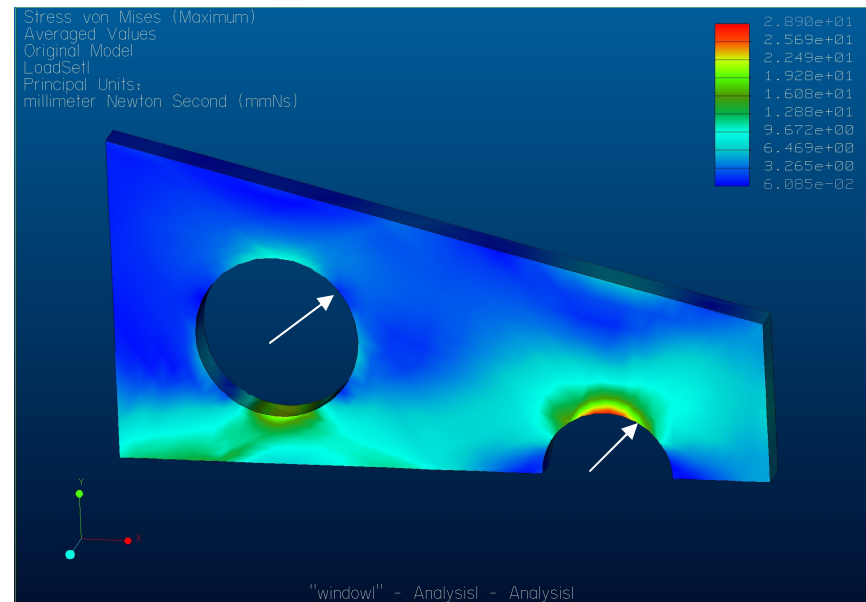
Design Optimization

Design Variables: R1 and R2

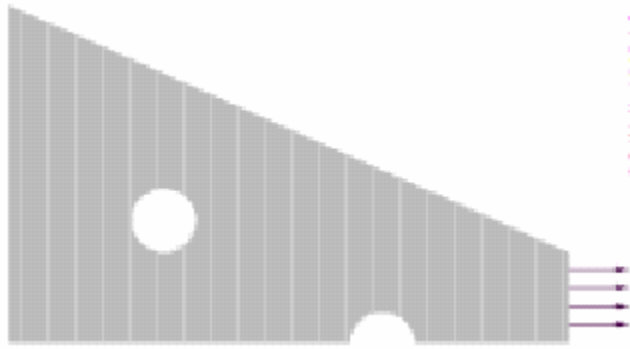
Constraints: Max stress

Min and max values for these variables

Objective Function: Reduce the total mass



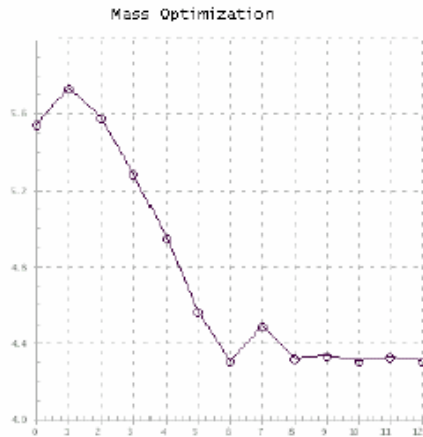
Design Optimization



Minimum values of design variables

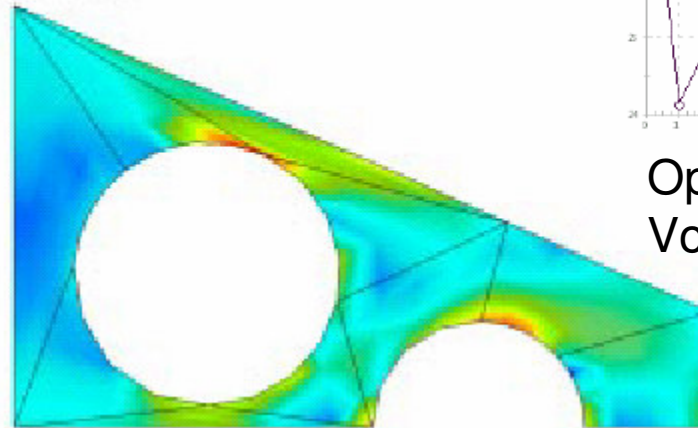


Maximum values of design variables

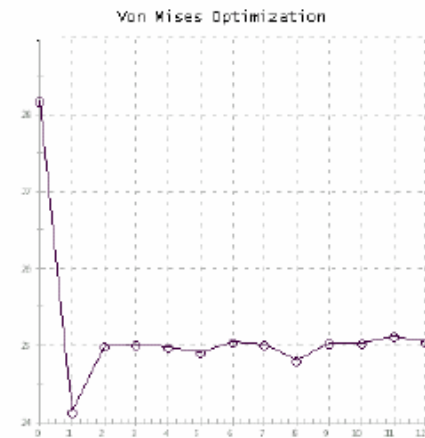


Optimization history: total mass

Stress: Von Mises (Maximum)
 Avg. Max +2.5037E+01
 Avg. Min +1.0183E+00
 Original Model
 Load: endload



Von Mises stress distribution in optimized plate



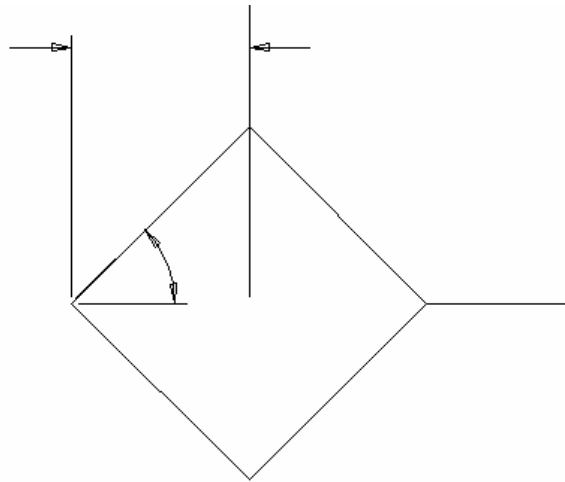
Optimization history:
 Von Mises stress

For the lab: Design Studies

- A standard design study is the most basic and simple - Finite Element Analysis
- A sensitivity design study
 - design variables and their range
- Optimization
 - desired goal (such as minimum mass of the body)
 - geometric constraints (such as dimensions or locations of geometric entities), material constraints (such as maximum allowed stress)
 - and one or more design variables

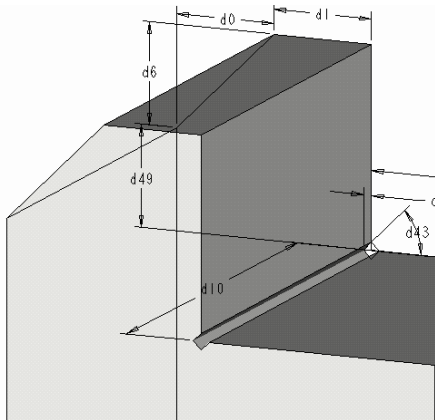
Parameter Sensitivity Study

- Define a design parameter (groove size)

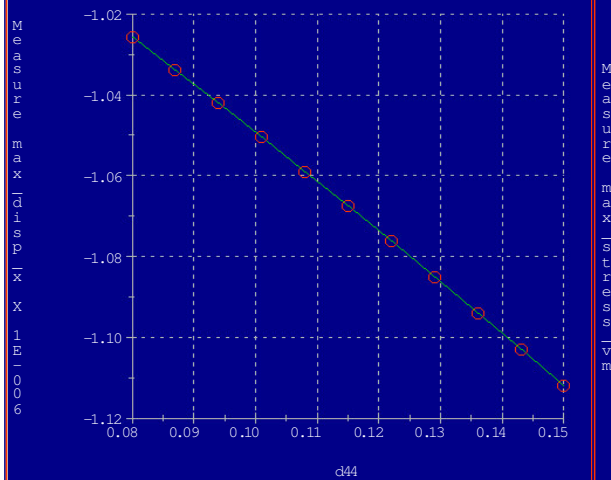


- Define a design study
- Perform the study and plot displacement and stress

Sensitivity Study

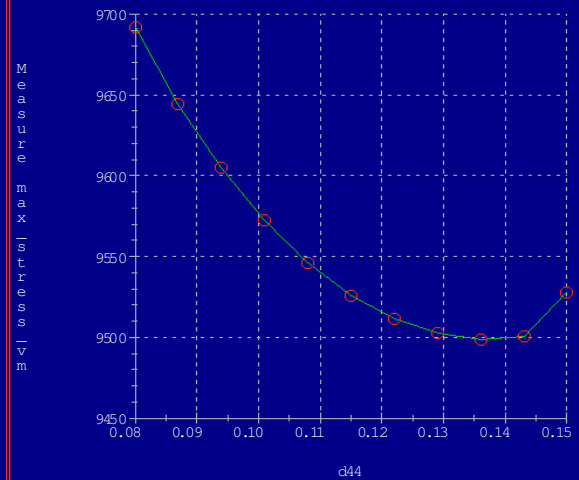


max_disp_x
Design Var
Load: load1



"window6" - study1 - anlys1

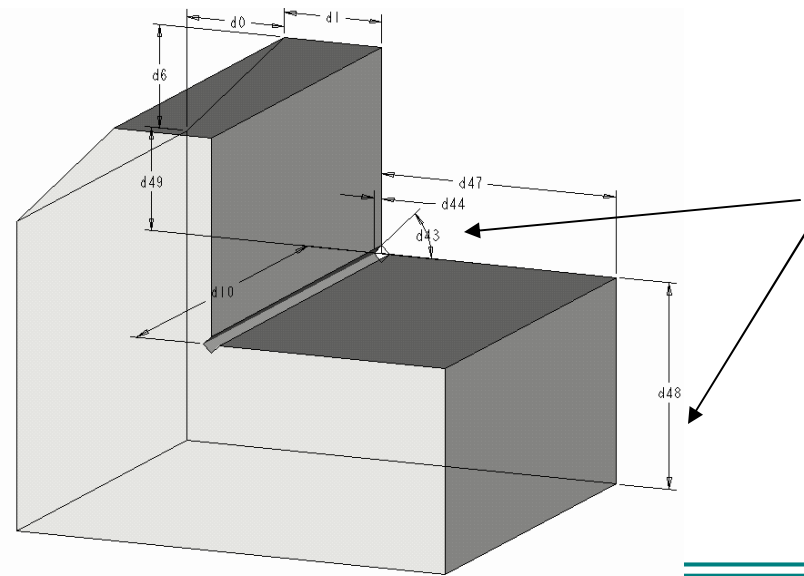
max_stress_vm
Design Var
Load: load1



"window7" - study1 - anlys1

Design Optimization

- Objective: minimize the total mass
 - Constraints: maximum load and deformation
1. Define relations to control the model generation (two design parameters; one is the groove size and the other is the overall fixture size.)

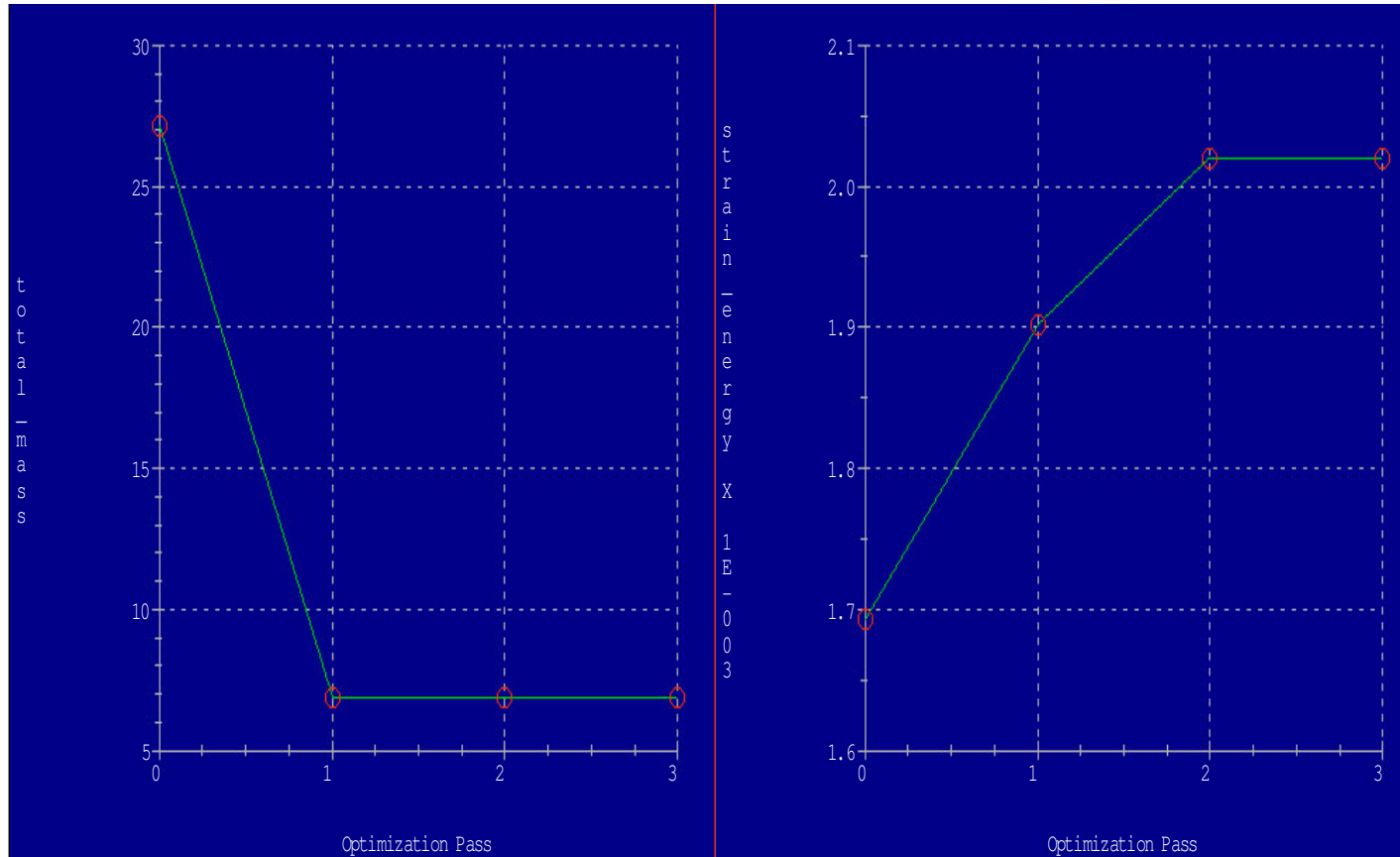


Two design variables

Design Optimization

- Objective: minimize the total mass
 - Constraints: maximum Von Mises stress and deformation
2. Specify ranges of variables, objective, and constraints
 3. Perform the optimization
 4. Results plotting and convergence check

Optimal Design



The Total Mass and Strain Energy Convergence Plots in the Optimization

Quick Questions

- A CAD model should be simplified for FEA.
- Unimportant portion of a design can be eliminated if a FEA is carefully defined.
- A FEA model only includes information of product geometry, loads and constraints.
- Pro/Mechanica has three convergence methods, namely, quick check, single pass adaptive, and multi-pass adaptive.
- Von-mises stress is a better index than strain energy for analysis convergence check.
- Pro/Mechanica can run independently to Pro/E.
- What are the three necessary components of an optimization problem?

Summary

- General process of FEA
- Inputs to FEA (4 basic things)
- H and P-elements
- Convergence check
- Sensitivity Analysis
- Optimization