

CHAPTER 5: Structural Steel Columns - ASD Design

5.1 Wide Flange Columns

Description

The selection of steel columns, subject to axial load and bending, can sometimes involve a tedious, iterative process. The first step requires guessing at a suitable trial section or using an elaborate set of formulas to select a first trial selection for the steel columns. The second step requires checking the first trial section to ensure that it satisfies the AISC Specification (specifically, the AISC interaction equations). If the first trial selection is not satisfactory, then the process must be repeated with a second trial section. In some cases additional iterations are required to ensure that the lowest weight section is obtained.

This application allows the user to rapidly check trial sections and to determine that the standards of the AISC Specification, Eqs. (H1-1) and (H1-2), are met. For input, the user only needs to enter the flange width, the section depth and the section weight. The necessary section properties and parameters are then computed by this application. Once the trial section is found satisfactory, the user may enter the actual values of the flange width, the section depth, the flange thickness and the web thickness to check that AISC Specification, Eqs. (H1-1) and (H1-2) are satisfied.

This application computes the section properties, compact section criteria, lateral bracing lengths, and slenderness ratios of I or H shaped column sections. In addition, it computes the actual and allowable axial and bending stresses, the amplification factors and moment modifiers, and the beam-column interaction equations following the AISC Specification for a column with axial load and end moments about one or both axes. (Formulas from Sections B, E, F and H of the AISC Specification are computed within this application.)

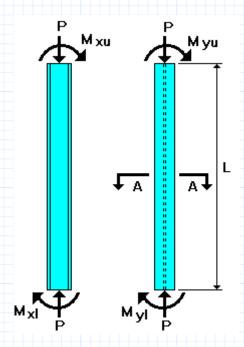
The required input includes the axial load and end moments about one or both axes, unbraced column length, effective length factors, yield strength, indication as to whether the column is free to sway about one or both axis directions, assumed depth, width and weight of section for initial trials, plus the flange and web thicknesses for check of the final section.

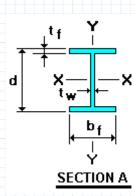
A summary listing input values, the solution of the interaction equations, and the computed values are shown on pages 17-19.

Reference: AISC "Specification for Structural Steel Buildings -- Allowable Stress Design and Plastic Design with Commentary." June 1, 1989

Input

Notation





Input Variables

Yield strength of steel: $F_y = 36 \text{ } \text{ksi}$

Column axial load: P = 200 kip

Unbraced column length: $L = 11.5 \ ft$

End moment about the X axis, at the upper $M_{xu} \coloneqq 120 \; kip \cdot ft$ end of the column:

End moment about the X axis, at the lower end of the column: $M_{xl} = -120 \ kip \cdot ft$

End moment about the
Y axis, at the upper end
of the column:

$$M_{yu} \coloneqq 40 \; kip \cdot ft$$

End moment about the Y axis, at the lower end of the column:

$$M_{yl} = -40 \ kip \cdot ft$$

Note: Positive values of M indicate clockwise moments and negative values indicate counterclockwise moments.

Effective length factor relative to the X axis:

$$K_x = 1.0$$

Effective length factor relative to the Y axis:

$$K_y = 1.0$$

Variable "X_Sway" defined as 0 if sidesway is prevented, and 1 if sidesway is permitted:

$$X_Sway \coloneqq 0$$

Variable "Y_Sway" defined as 0 if sidesway is prevented, and 1 if sidesway is permitted:

$$Y_Sway \coloneqq 0$$

Section Dimensions and Weight

Enter estimated values for the section depth, flange width and section weight. Define the flange and web thickness equal to 0 inches for preliminary trial section selections, or enter the actual section depth, flange width, web thickness, flange thickness and section weight if checking a specific section.

Section depth:

$$d \coloneqq 14.32 in$$

Flange width:

$$b_f = 14.605 \ in$$

Web thickness:

$$t_w \coloneqq 0.525 \ in$$

Flange thickness:

$$t_f = 0.860 \ in$$

Section weight $W = 109 \frac{lb}{ft}$

Computed Section Properties

- A cross section area of member
- Ix moment of inertia about the X axis
- rx radius of gyration about the X axis
- Sx section modulus about the X axis
- Iy moment of inertia about the Y axis
- ry radius of gyration about the Y axis
- Sy section modulus about the Y axis
- r_T radius of gyration of the compression flange + 1/3 of compression web area about an axis in the plane of the web

Computed Variables

- fa axial compressive stress
- fb_xu bending stress about the X axis at the upper end of the column
- fb_xl bending stress about the X axis at the lower end of the column
- fb_yu bending stress about the Y axis at the upper end of the column
- fb_yl bending stress about the Y axis at the lower end of the column
- Fa allowable compressive axial stress (AISC Specification, Eqs. (E2-1) and (E2-2))
- F_{bx} allowable bending stress about the X axis (AISC Specification, Eqs. (F1-1), (F1-2), (F1-3) and (F1-5))

Fby allowable bending stress about the Y axis (AISC Specification, Identity (F2-2) and Eq. (F2-3) Euler's stress about the X axis divided by a factor of safety (AISC Specification, Sect. H-1) Euler's stress about the Y axis divided by a factor of safety (AISC Specification, Sect. H-1) C_{c} slenderness ratio separating elastic and inelastic behavior (AISC Specification, Eq. (E2-1)) Cmx moment modifier coefficient about the X axis (AISC Specification, Sect. H-1) Cmy moment modifier coefficient about the Y axis (AISC Specification, Sect. H-1) moment modifier factor (AISC Specification, Sect. F1-3) C_{b} Lc maximum unbraced length of a compact section at which allowable strong axis (X axis) bending may be 0.66Fy (AISC Specification, Eq. (F1-2)) maximum unbraced length of a section at which allowable strong axis (X axis) Lu bending may be 0.60Fy (AISC Specification, Eq. (F1-2)) a variable defined within this application to reflect compact section criteria of AISC CF Specification, Table B5.1. (CF = 2 if both flange and web are compact, 1 if flange is compact, and 0 if neither the flanges nor the web are compact.) FR maximum ratio of half the flange to the flange thickness, for a compact shape (AISC Specification, Table B5.1) maximum ratio of half the flange to the flange thickness, for a non-compact shape FRmax (AISC Specification, Table B5.1) WR(fa) maximum ratio of the section depth to the web thickness for webs in compression or combined flexural and axial compression, as a function of axial stress

Calculations

This application is limited to steel with a yield strength less than or equal to 65 ksi:

$$F_y := if(F_y > 65 \cdot ksi, 65 \cdot ksi, F_y)$$
 $F_y = 36 \ ksi$

Dimensions and Properties

The approximate area and moment of inertia of fillets between the web and flanges of rolled sections are computed assuming circular fillets with a radius of 0.4 inches for W8 shapes, 0.5 inches for W10 shapes, and 0.6 inches for W12 and W14 sections. Some computed properties may vary slightly from values tabulated in the AISC Manual due to varying assumptions of fillet sizes. The distance between the inner face of the flanges is used to distinguish between shapes.

Clear distance between flanges:

$$T \coloneqq d - 2 \cdot t_f$$
 $T = 12.6 in$

Estimated radius of circular radius fillets between flange and web:

$$r := if(T \le 7.13 \ in, 0.4 \ in, if(T \le 8.86 \ in, 0.5 \ in, 0.6 \ in)) = 0.6 \ in$$

Area of four circular radius fillets:

$$A_o := 4 \cdot r^2 \cdot \left(1 - \frac{\pi}{4}\right) = 0.309 \ in^2$$

Moment of inertia of four circular radius fillets:

$$I_o \coloneqq r^4 \cdot \left(\frac{1}{3} - \frac{\pi}{16} - \frac{1}{36 \cdot \left(1 - \frac{\pi}{4}\right)}\right) \qquad I_o = 0.00098 \ in^4$$

Distance from the centroid of a fillet to the face of the web or flange:

$$z \coloneqq r \cdot \left(1 - \frac{1}{6 \cdot \left(1 - \frac{\pi}{4}\right)}\right) \qquad z = 0.134 \ in$$

Cross section area of member:

$$A \coloneqq \text{if}\left(t_f = 0 \cdot in, \frac{W}{3.4} \cdot \frac{in^2 \cdot ft}{lb}, 2 \cdot b_f \cdot t_f + t_w \cdot (d - 2 \cdot t_f) + A_o\right) = 32.045 \ in^2$$

Estimated flange thickness:

$$t_{f} \coloneqq \mathbf{if} \left(t_{f} = 0 \cdot \mathbf{in}, \frac{\left(\frac{8 \cdot b_{f}}{5} + \frac{d}{2} \right) - \sqrt{\left(\frac{8 \cdot b_{f}}{5} + \frac{d}{2} \right)^{2} - \frac{16}{5} \cdot \left(A - A_{o} \right)}}{2}, t_{f} \right) = 0.86 \ \mathbf{in}$$

Estimated web thickness:

$$t_w \coloneqq \text{if}\left(t_w = 0 \ in, \frac{5}{8} \cdot t_f, t_w\right) \qquad \qquad t_w = 0.525 \ in$$

Estimated section weight if the entered flange thickness is 0 inches, or the actual section weight entered:

$$W := if \left(W = 0 \cdot \frac{lb}{ft}, A \cdot 3.4 \cdot \frac{lb}{ft \cdot in^2}, W \right) \qquad W = 109 \frac{lb}{ft}$$

Moment of inertia about the X axis:

$$I_{x} \coloneqq \frac{b_{f} \cdot t_{f} \cdot \left(d - t_{f}\right)^{2}}{2} + \frac{t_{w} \cdot \left(d - 2 \cdot t_{f}\right)^{3}}{12} + \frac{b_{f} \cdot t_{f}^{3}}{6} + I_{o} + A_{o} \cdot \left(\frac{d}{2} - t_{f} - z\right)^{2} \qquad I_{x} = 1238.6 \ in^{4}$$

Section modulus about the X axis:

$$S_x = \frac{2 \cdot I_x}{d} \qquad S_x = 173 \text{ in}^3$$

Radius of gyration about the X axis:

$$r_x = \sqrt{rac{I_x}{A}}$$
 $r_x = 6.22 \ in$

Moment of inertia about the Y axis:

$$I_y \coloneqq rac{t_f \cdot b_f^{\ 3}}{6} + rac{\left(d - 2 \cdot t_f
ight) \cdot t_w^{\ 3}}{12} + I_o + A_o \cdot \left(rac{t_w}{2} + z
ight)^2 = 446.733 \ \emph{in}^4$$

Section modulus about the Y axis:

$$S_y \coloneqq \frac{2 \cdot I_y}{b_{\scriptscriptstyle f}}$$
 $S_y = 61.18 \; in^3$

Radius of gyration about the Y axis:

$$r_y\!\coloneqq\!\sqrt{rac{I_y}{A}}$$
 $r_y\!=\!3.73~in$

Area of one flange and the ratio of section depth to the area of the compression flange:

$$A_f \! \coloneqq \! b_f \! \cdot \! t_f \qquad \qquad A_f \! = \! 12.56 \, \, in^2 \qquad \qquad \frac{d}{A_f} \! = \! 1.14 \, \, in^{-1}$$

Radius of gyration of a T-section comprised of the compression flange plus 1/3 of the compression web area:

$$r_{T} \coloneqq \sqrt{\frac{\frac{1}{12} \cdot t_{f} \cdot b_{f}^{\ 3} + \frac{1}{12} \cdot \frac{d - 2 \cdot t_{f}}{6} \cdot t_{w}^{\ 3} + \frac{1}{2} \cdot \left(I_{o} + A_{o} \cdot \left(\frac{t_{w}}{2} + z\right)^{2}\right)}{b_{f} \cdot t_{f} + \frac{d - 2 \cdot t_{f}}{6} \cdot t_{w} + \frac{A_{o}}{2}}$$

$$r_T = 4.02 \ in$$

Axial and Bending Stresses

Axial stress:

$$f_a = \frac{P}{A}$$
 $f_a = 6.2 \ ksi$

Bending stress due to moment about the X axis at the upper end of the column:

$$f_{b_xu} \coloneqq \frac{M_{xu}}{S_x} = 8.3 \text{ ksi}$$

Bending stress due to moment about the X axis at the lower end of the column:

$$f_{b_xl}\!:=\!rac{M_{xl}}{S}$$
 $f_{b_xl}\!=\!-8.3~ksi$

Bending stress due to moment about the Y axis at the upper end of the column:

$$f_{b_yu} \coloneqq \frac{M_{yu}}{S_{x}}$$
 $f_{b_yu} = 7.8 \ ksi$

Bending stress due to moment about the Y axis at the lower end of the column:

$$f_{b_yl} := \frac{M_{yl}}{S_y}$$
 $f_{b_yl} = -7.8 \ ksi$

Slenderness ratios about the X and Y axes:

$$\frac{K_x \cdot L}{r_x} = 22.2 \qquad \frac{K_y \cdot L}{r_y} = 37$$

Larger slenderness ratio:

$$SR := if\left(\frac{K_x \cdot L}{r_x} > \frac{K_y \cdot L}{r_y}, \frac{K_x \cdot L}{r_x}, \frac{K_y \cdot L}{r_y}\right) \qquad SR = 37$$

If SR is >200 a larger section or bracing is required.

Modulus of elasticity of steel:

$$E \coloneqq 29000 \ ksi$$

Column slenderness ratio separating elastic and inelastic buckling (AISC Specification, Eq. (E2-1)):

$$C_c \coloneqq \sqrt{\frac{2 \cdot \pi^2 \cdot E}{F_y}} = 126.099$$

Allowable axial stress (AISC Specification, Eqs. (E2-1) and (E2-2)) combined with SR substituted for Kl/r:

$$F_{a} \coloneqq \text{if} \left[\left\langle \left\langle SR > C_{c} \right\rangle \cdot \left(SR \leq 200 \right) \right\rangle, \frac{12 \ \pi^{2} \cdot E}{23 \ SR^{2}}, \text{if} \left[SR > 200, 0 \ \textit{ksi}, \frac{\left(1 - \frac{SR^{2}}{2 \cdot C_{c}^{2}} \right) \cdot F_{y}}{\frac{5}{3} + \frac{3 \ SR}{8 \ C_{c}} - \frac{SR^{3}}{8 \cdot C_{c}^{3}}} \right] \right]$$

$$F_a = 19.4 \ ksi$$

Ratio of the smaller end moment Mxa, to the larger end moment Mxb about the X axis:

$$\boldsymbol{M}_{xa}\!\coloneqq\!\mathbf{if}\left(\left|\boldsymbol{M}_{xu}\right|\!<\!\left|\boldsymbol{M}_{xl}\right|,\boldsymbol{M}_{xu},\boldsymbol{M}_{xl}\right)$$

$$M_{xb} \coloneqq \operatorname{if} \left(M_{xa} = M_{xu}, M_{xl}, M_{xu} \right)$$

3 e

$$\frac{M_{xa}}{M_{xb}} = -1$$

Ratio of the smaller end moment Mya, to the larger end moment Myb about the Y axis:

$$\boldsymbol{M}_{ya}\!\coloneqq\!\operatorname{if}\left(\left|\boldsymbol{M}_{yu}\right|\!<\!\left|\boldsymbol{M}_{yl}\right|,\boldsymbol{M}_{yu},\!\boldsymbol{M}_{yl}\right)$$

$$M_{yb} := if(M_{ya} = M_{yu}, M_{yl}, M_{yu})$$

$$\frac{M_{ya}}{M_{yb}} = -1$$

Moment modifier factor Cb (AISC Specification, Sect. F1-3):

$$C_b \coloneqq 1.75 + 1.05 \cdot \frac{M_{xa}}{M_{xb}} + 0.3 \cdot \left(\frac{M_{xa}}{M_{xb}}\right)^2$$

$$C_b \coloneqq \operatorname{if} \left(\left(X_Sway = 0 \right) \cdot \left(f_a > 0 \cdot ksi \right), 1.0, \operatorname{if} \left(C_b < 2.3, C_b, 2.3 \right) \right)$$

$$C_b = 1$$

When the ends of the member are braced to prevent sidesway in the X direction and the axial stress is greater than 0 ksi, then Cb equals 1.0.

Compact Section Criteria

Limiting ratio of one-half the flange width to the flange thickness for compact shapes (AISC Specification, Table B5.1):

$$FR \coloneqq \frac{65}{\sqrt{\frac{F_y}{ksi}}}$$

$$FR = 10.833$$

Limiting ratio of one-half the flange width to the flange thickness for non-compact shapes (AISC Specification, Table B5.1):

$$FR_{max} := \frac{95}{\sqrt{\frac{F_y}{k \sin x}}}$$

$$FR_{max} = 15.833$$

Section depth to web thickness ratio for webs in compression or combined flexural and axial compression for compact sections (AISC Specification, Table B5.1) modified by expressing

the limiting ratio as a function of fa:

$$WR\left\langle f_{a}\right\rangle \coloneqq \mathbf{if}\left(\frac{f_{a}}{F_{y}}\leq0.16\,,\frac{640}{\sqrt{\frac{F_{y}}{ksi}}}\cdot\left(1-3.74\cdot\frac{f_{a}}{F_{y}}\right),\frac{257}{\sqrt{\frac{F_{y}}{ksi}}}\right)$$

Actual ratios of one-half the flange width to flange thickness and section depth to web thickness, and the limiting ratios for a compact flange FR, a compact web $WR(f_a)$, and the maximum permissible flange ratio for a non-compact section FR_{max} :

$$\frac{b_f}{2 \cdot t_f} = 8.5$$
 $FR = 10.8$ $FR_{max} = 15.8$ $\frac{d}{t_w} = 27.3$ $WR(f_a) = 42.8$

Variable CF defined to test for compact section criteria. If both the web and flange are compact, CF = 2; if the flange is non-compact and the web is compact, CF = 1; and if the web is non-compact and the flange is either compact or non-compact, CF = 0.:

$$CF \coloneqq \text{if}\left(\left(\frac{b_{f}}{2 \cdot t_{f}} \leq FR\right) \cdot \left(\frac{d}{t_{w}} \leq WR\left(f_{a}\right)\right), 2, \text{if}\left(\left(\frac{b_{f}}{2 \cdot t_{f}} \geq FR\right) \cdot \left(\frac{d}{t_{w}} \leq WR\left(f_{a}\right)\right), 1, 0\right)\right)$$

$$CF = 2$$

Lateral bracing lengths, Lu and Lc (AISC Specifications, Eq. (F1-2)):

$$L_u \coloneqq \frac{20000}{\frac{d}{b_f \cdot t_f} \cdot \frac{F_y}{ksi}} = 40.607 \ ft$$

$$L_{c1} \coloneqq \frac{76 \cdot b_f}{\sqrt{\frac{F_y}{ksi}}} = 15.416 \; ft$$

$$L_c := if (L_{c1} < L_u, L_{c1}, L_u) = 15.416 \ ft$$

Allowable bending stress for adequately braced, compact and non-compact sections (AISC Specifications, Eqs. (F1-1), (F1-2), (F1-3) and (F1-5), combined):

$$F1' \coloneqq F_y \boldsymbol{\cdot} \left(0.79 - 0.002 \boldsymbol{\cdot} \mathbf{if} \left(\frac{b_f}{2 \boldsymbol{\cdot} t_f} \boldsymbol{<} FR, FR, \frac{b_f}{2 \boldsymbol{\cdot} t_f} \right) \boldsymbol{\cdot} \sqrt{\frac{F_y}{ksi}} \right)$$

 $\frac{L}{r_T}$ = 34.3

$$F1 \coloneqq \text{if} \left\langle \left\langle L \leq L_c \right\rangle \cdot \left(CF = 2 \right), 0.66 \cdot F_y, \text{if} \left\langle \left\langle L \leq L_c \right\rangle \cdot \left(CF = 1 \right), F1', \text{if} \left\langle \left\langle L \leq L_c \right\rangle \cdot \left(CF = 0 \right), 0.60 \cdot F_y, 0 \cdot \textit{ksi} \right\rangle \right\rangle \right\rangle$$

$$F1 = 23.8 \ \textit{ksi}$$

If F1 = 0 ksi, the allowable bending stress is controlled by AISC Specification Eqs. (F1-6), (F1-7) or (F1-8).

Allowable bending stress for compact and non-compact sections with unbraced lengths greater than Lc (AISC Specification, Eqs. (F1-6) and (F1-7) combined):

$$R_{1} \coloneqq \sqrt{\frac{102 \cdot 10^{3} \cdot C_{b} \cdot ksi}{F_{y}}} \qquad R_{1} = 53.2$$

$$R_{2} \coloneqq \sqrt{\frac{510 \cdot 10^{3} \cdot C_{b} \cdot ksi}{F_{y}}} \qquad R_{2} = 119$$

$$F2' \coloneqq \left\| \text{ if } \left(\frac{L}{r_{T}} \ge R_{1} \right) \wedge \left(\frac{L}{r_{T}} \le R_{2} \right) \right\| = 0 \text{ } ksi$$

$$\left\| \left\| \left(\frac{1}{r_{T}} \ge R_{1} \right) \wedge \left(\frac{L}{r_{T}} \right)^{2} \right\| = 0 \text{ } ksi$$

$$\left\| \left\| \left(\frac{1}{r_{T}} \ge R_{1} \right) \wedge \left(\frac{L}{r_{T}} \right)^{2} \right\| = 0 \text{ } ksi$$

$$\left\| \left\| \left(\frac{1}{r_{T}} \right)^{2} \right\| = 0 \text{ } ksi$$

$$\left\| \left\| \frac{1}{r_{T}} + \frac{$$

$$F2\coloneqq \mathrm{if}\left(F2'\!>\!0.60 \bullet F_y, 0.60 \bullet F_y, F2'\right)$$

AISC Specification, Eq. (F1-8):

$$F3 \coloneqq \text{if}\left(\frac{12 \cdot 10^{3} \cdot C_{b} \cdot \textbf{ksi}}{\frac{L \cdot d}{A_{f}}} > 0.60 \cdot F_{y}, 0.60 \cdot F_{y}, \frac{12 \cdot 10^{3} \cdot C_{b} \cdot \textbf{ksi}}{\frac{L \cdot d}{A_{f}}}\right)$$

$$F3 = 21.6 \ ksi$$

Allowable bending stress equal to the largest value of F1, F2 or F3:

$$F_{bx} = if(F1 > 0 \cdot ksi, F1, if(F2 > F3, F2, F3))$$
 $F_{bx} = 23.8 \ ksi$

Allowable bending stress for bending about the Y axis for compact or non-compact sections (AISC Specification, Identity (F2-2) and Eq. (F2-3) combined) and with maximum flange ratio for a compact section substituted for the actual ratio if it is larger:

$$\begin{split} F_{by} \coloneqq & F_y \cdot \left(1.075 - 0.005 \cdot \left(\text{if} \left(\frac{b_f}{2 \cdot t_f} \right) \cdot FR, \frac{b_f}{2 \cdot t_f}, FR \right) \cdot \sqrt{\frac{F_y}{ksi}} \right) \right) \\ F_{by} = & 27 \ ksi \end{split}$$

Fby ranges from a lower limit of 0.60Fy to an upper limit of 0.75Fy.

Euler's stress for the X and Y directions, divided by a factor or safety and using the actual unbraced length and corresponding radius of gyration in the plain of bending (AISC Specification, Sect. H-1):

$$F'_{ex} \coloneqq \frac{12 \cdot \pi^2 \cdot E}{23 \cdot \left(\frac{K_x \cdot L}{r_x}\right)^2} \qquad F'_{ex} = 303.1 \text{ ksi}$$

$$F'_{ey} \coloneqq \frac{12 \cdot \pi^2 \cdot E}{23 \cdot \left(\frac{K_y \cdot L}{r_y}\right)^2}$$
 $F'_{ey} = 109.3 \ ksi$

Moment modifier coefficients C_{mx} and C_{my} (AISC Specification, Sect. H-1):

$$C_{mx} \coloneqq \text{if}\left(X_Sway = 0, 0.6 - 0.4 \cdot \left(\frac{M_{xa}}{M_{xb}}\right), 0.85\right) = 1$$

$$C_{my} \coloneqq \text{if} \left(Y_Sway = 0 \,, 0.6 - 0.4 \cdot \left(\frac{M_{ya}}{M_{yb}} \right), 0.85 \right) = 1$$

AISC Specification, Eqs. (H1-1) and (H1-2) for combined axial compression and bending, expressed as functions of bending stresses about the X and Y axes:

$$H1_1\left\langle f_{bx}, f_{by} \right\rangle \coloneqq \frac{f_a}{F_a} + \frac{C_{mx} \cdot f_{bx}}{\left(1 - \frac{f_a}{F_{ex}'}\right) \cdot F_{bx}} + \frac{C_{my} \cdot f_{by}}{\left(1 - \frac{f_a}{F_{ey}'}\right) \cdot F_{by}}$$

$$H1_2 \left\langle f_{bx}, f_{by} \right\rangle \coloneqq \frac{f_a}{0.60 \cdot F_y} + \frac{f_{bx}}{F_{bx}} + \frac{f_{by}}{F_{by}}$$

At upper end of column:

$$H1_{1}(|f_{b_{xu}}|,|f_{b_{yu}}|) = 0.987$$

$$H1_2(|f_{b_xu}|,|f_{b_yu}|) = 0.93$$

At lower end of column:

$$H1_{1}(|f_{b|xl}|,|f_{b|yl}|) = 0.987$$

$$H1_{2}\left(\left|f_{b_{x}l}\right|,\left|f_{b_{y}l}\right|\right) = 0.93$$

Maximum value of H1_1 or H1_2:

$$HEQ \coloneqq \begin{bmatrix} H1_1 \left(f_{b_xu}, f_{b_yu} \right) & H1_1 \left(f_{b_xl}, f_{b_yl} \right) \\ H1_2 \left(f_{b_xu}, f_{b_yu} \right) & H1_2 \left(f_{b_xl}, f_{b_yl} \right) \end{bmatrix}$$

$$\max(HEQ) = 0.987$$

If the maximum value of interaction equations H1_1 or H1_2 is less than or equal 1.0 the section is adequate If the section is too small or too large, a new trial section may be entered.

Summary

Enter section designation: W14x109

Input

Yield strength of steel: $F_y = 36 \text{ ksi}$

Column axial load: $P = 200 \ kip$

Unbraced column length: L=11.5 ft

End moment about the X axis, at the $M_{xu} = 120 \; kip \cdot ft$ upper end of the column:

End moment about the X axis, at the $M_{xl} = -120 \ kip \cdot ft$ lower end of the column:

End moment about the Y axis, at the upper end of the column: $M_{yu}=40 \; kip \cdot ft$

End moment about the Y axis, at the lower end of the column: $M_{yl} = -40 \ kip \cdot ft$

Effective length factor relative to the X axis: $K_x = 1$

Effective length factor relative to the Y axis: $K_y = 1$

Variable "X_Sway" defined as 0 if sidesway is prevented, and 1 if $X_Sway = 0$ sidesway is permitted:

 $Y_Sway=0$

Variable "Y_Sway" defined as 0 if sidesway is prevented, and 1 if sidesway is permitted:

Section dimensions and weight entered:

Section depth: d = 14.32 in

Flange width: $b_f = 14.605 in$

Web thickness: $t_w = 0.525 \ in$

Flange thickness: $t_f = 0.86 \ in$

Section weight per unit length: $W = 109 \frac{lb}{ft}$

Maximum value of H1_1 or H1_2: max(HEQ) = 0.987

Note: If the maximum value of H1_1 or H1_2 is significantly larger than 1.0 a stronger section must be used.

Estimated trial weight for follow-up estimates, assuming no change in bf or d:

$$\max(HEQ) \cdot W = 107.602 \frac{lb}{ft}$$

$$W = 109 \frac{lb}{ft}$$

Intermediate Computed Values:

(Refer to document for definitions.)

$$A = 32.045 \ in^2$$
 $f_a = 6.241 \ ksi$ $F_a = 19.428 \ ksi$

$$I_x = (1.239 \cdot 10^3) in^4$$
 $f_{b_x xu} = 8.324 ksi$ $F_{bx} = 23.76 ksi$

$$r_x = 6.217 \ in$$
 $f_{b \ xl} = -8.324 \ ksi$ $F'_{ex} = 303.088 \ ksi$

$$S_x = 172.989 \ in^3$$
 $f_{b_yu} = 7.846 \ ksi$ $F_{by} = 27 \ ksi$

$$I_y = 446.733 \ in^4$$
 $f_{b_yl} = -7.846 \ ksi$ $F'_{ey} = 109.316 \ ksi$

$$r_y = 3.734 \ in$$
 $C_c = 126.099$

$$T_y = 3.734 \text{ int}$$
 $K_x \cdot L = 22.197$ $C_c = 120$ $C_b = 1$

$$S_y = 01.173 \text{ m}$$
 $C_b = 1$

$$r_T$$
=4.02 in
$$\frac{K_y \cdot L}{r_y}$$
=36.96 C_{mx} =1

$$rac{d}{d} = 1.14 \; in^{-1}$$
 $C_{my} = 1$

$$A_f$$

$$L_c = 15.416 \ ft$$

$$\frac{b_f}{2 \cdot t_f} = 8.491$$

$$FR = 10.833$$

$$L_u\!=\!40.607\;ft$$

 $WR\left\langle f_{a}\right\rangle =42.833$

$$\frac{d}{t_w} = 27.276$$

$$FR_{max} = 15.833$$

$$CF = 2$$