### 5.1 Wide Flange Columns

## Description

The selection of steel columns, subject to axial load and bending, can sometimes involve a tedious, iterative process. The first step requires guessing at a suitable trial section or using an elaborate set of formulas to select a first trial selection for the steel columns. The second step requires checking the first trial section to ensure that it satisfies the AISC Specification (specifically, the AISC interaction equations). If the first trial selection is not satisfactory, then the process must be repeated with a second trial section. In some cases additional iterations are required to ensure that the lowest weight section is obtained.

This application allows the user to rapidly check trial sections and to determine that the standards of the AISC Specification, Eqs. (H1-1) and (H1-2), are met. For input, the user only needs to enter the flange width, the section depth and the section weight. The necessary section properties and parameters are then computed by this application. Once the trial section is found satisfactory, the user may enter the actual values of the flange width, the section depth, the flange thickness and the web thickness to check that AISC Specification, Eqs. (H1-1) and (H1-2) are satisfied.

This application computes the section properties, compact section criteria, lateral bracing lengths, and slenderness ratios of I or H shaped column sections. In addition, it computes the actual and allowable axial and bending stresses, the amplification factors and moment modifiers, and the beam-column interaction equations following the AISC Specification for a column with axial load and end moments about one or both axes. (Formulas from Sections B, $\mathrm{E}, \mathrm{F}$ and H of the AISC Specification are computed within this application.)

The required input includes the axial load and end moments about one or both axes, unbraced column length, effective length factors, yield strength, indication as to whether the column is free to sway about one or both axis directions, assumed depth, width and weight of section for initial trials, plus the flange and web thicknesses for check of the final section.

A summary listing input values, the solution of the interaction equations, and the computed values are shown on pages 17-19.

Reference: AISC "Specification for Structural Steel Buildings -- Allowable Stress Design and Plastic Design with Commentary." June 1, 1989

## Input

Notation


## Input Variables

Yield strength of steel: $\quad F_{y}:=36 k s i$
Column axial load: $\quad P:=200 \mathrm{kip}$
Unbraced column length: $\quad L:=11.5 \mathrm{ft}$
End moment about the X axis, at the upper end of the column:

End moment about the X axis, at the lower $\quad M_{x l}:=-120 \mathrm{kip} \cdot \mathrm{ft}$ end of the column:

End moment about the Y axis, at the upper end $\quad M_{y u}:=40 \mathrm{kip} \cdot \mathrm{ft}$ of the column:

End moment about the Y axis, at the lower end $\quad M_{y l}:=-40 \mathrm{kip} \cdot \mathrm{ft}$ of the column:

Note : Positive values of M indicate clockwise moments and negative values indicate counterclockwise moments.

Effective length factor relative to the X axis:

$$
K_{x}:=1.0
$$

Effective length factor relative to the Y axis:

$$
K_{y}:=1.0
$$

Variable "X_Sway"
defined as 0 if sidesway
is prevented, and 1 if
X_Sway:=0
sidesway is permitted:

Variable "Y_Sway"
defined as 0 if sidesway
is prevented, and 1 if
$Y \_S w a y:=0$
sidesway is permitted:

## Section Dimensions and Weight

Enter estimated values for the section depth, flange width and section weight. Define the flange and web thickness equal to 0 inches for preliminary trial section selections, or enter the actual section depth, flange width, web thickness, flange thickness and section weight if checking a specific section.

Section depth: $\quad d:=14.32$ in
Flange width: $\quad b_{f}:=14.605$ in

Web thickness: $\quad t_{w}:=0.525$ in
Flange thickness: $\quad t_{f}:=0.860 \mathrm{in}$

Section weight per unit length:

$$
W:=109 \frac{l b}{f t}
$$

## Computed Section Properties

A cross section area of member
Ix moment of inertia about the X axis
rx radius of gyration about the X axis
$\mathrm{S}_{\mathrm{x}} \quad$ section modulus about the X axis
Iy moment of inertia about the Y axis
ry radius of gyration about the Y axis
Sy section modulus about the Y axis
$r_{T}$ radius of gyration of the compression flange $+1 / 3$ of compression web area about an axis in the plane of the web

## Computed Variables

fa axial compressive stress
$\mathrm{fb}_{\mathrm{b}} \mathrm{xu}$ bending stress about the X axis at the upper end of the column
fb_xl bending stress about the X axis at the lower end of the column
$\mathrm{fb}_{\mathrm{b}}$ yu bending stress about the Y axis at the upper end of the column
fb_yl bending stress about the Y axis at the lower end of the column

Fa allowable compressive axial stress
(AISC Specification, Eqs. (E2-1) and (E2-2))
Fbx allowable bending stress about the X axis
(AISC Specification, Eqs. (F1-1), (F1-2), (F1-3) and (F1-5))

Fby allowable bending stress about the Y axis
(AISC Specification, Identity (F2-2) and Eq. (F2-3)

F'ex Euler's stress about the X axis divided by a factor of safety (AISC Specification, Sect. H-1)

F'ey Euler's stress about the Y axis divided by a factor of safety (AISC Specification, Sect. H-1)

Cc slenderness ratio separating elastic and inelastic behavior (AISC Specification, Eq. (E2-1))

Cmx moment modifier coefficient about the X axis (AISC Specification, Sect. $\mathrm{H}-1$ )

Cmy moment modifier coefficient about the Y axis (AISC Specification, Sect. H-1)

Cb moment modifier factor (AISC Specification, Sect. F1-3)
Lc maximum unbraced length of a compact section at which allowable strong axis ( X axis) bending may be 0.66 Fy
(AISC Specification, Eq. (F1-2))

Lu maximum unbraced length of a section at which allowable strong axis (X axis)
bending may be 0.60 Fy
(AISC Specification, Eq. (F1-2))

CF a variable defined within this application to reflect compact section criteria of AISC Specification, Table B5.1. (CF = 2 if both flange and web are compact, 1 if flange is compact, and 0 if neither the flanges nor the web are compact.)

FR maximum ratio of half the flange to the flange thickness, for a compact shape (AISC Specification, Table B5.1)

FRmax maximum ratio of half the flange to the flange thickness, for a non-compact shape (AISC Specification, Table B5.1)

WR(fa) maximum ratio of the section depth to the web thickness for webs in compression or combined flexural and axial compression, as a function of axial stress

## Calculations

This application is limited to steel with a yield strength less than or equal to 65 ksi :

$$
F_{y}:=\text { if }\left(F_{y}>65 \cdot k s i, 65 \cdot k s i, F_{y}\right) \quad F_{y}=36 k s i
$$

## Dimensions and Properties

The approximate area and moment of inertia of fillets between the web and flanges of rolled sections are computed assuming circular fillets with a radius of 0.4 inches for W8 shapes, 0.5 inches for W10 shapes, and 0.6 inches for for W12 and W14 sections. Some computed properties may vary slightly from values tabulated in the AISC Manual due to varying assumptions of fillet sizes. The distance between the inner face of the flanges is used to distinguish between shapes.

Clear distance between flanges:

$$
T:=d-2 \cdot t_{f} \quad T=12.6 \mathrm{in}
$$

Estimated radius of circular radius fillets between flange and web:

$$
r:=\operatorname{if}(T \leq 7.13 \mathrm{in}, 0.4 \mathrm{in}, \operatorname{if}(T \leq 8.86 \mathrm{in}, 0.5 \mathrm{in}, 0.6 \mathrm{in}))=0.6 \mathrm{in}
$$

Area of four circular radius fillets:

$$
A_{o}:=4 \cdot r^{2} \cdot\left(1-\frac{\pi}{4}\right)=0.309 \mathrm{in}^{2}
$$

Moment of inertia of four circular radius fillets:

$$
\left.I_{o}:=r^{4} \cdot\left(\frac{1}{3}-\frac{\pi}{16}-\frac{1}{36 \cdot\left(1-\frac{\pi}{4}\right)}\right)\right) \quad I_{o}=0.00098 \mathrm{in}^{4}
$$

Distance from the centroid of a fillet to the face of the web or flange:

$$
z:=r \cdot\left(1-\frac{1}{6 \cdot\left(1-\frac{\pi}{4}\right)}\right) \quad z=0.134 \mathrm{in}
$$

Cross section area of member:

$$
A:=\text { if }\left(t_{f}=0 \cdot i n, \frac{W}{3.4} \cdot \frac{i n^{2} \cdot f t}{l b}, 2 \cdot b_{f} \cdot t_{f}+t_{w} \cdot\left(d-2 \cdot t_{f}\right)+A_{o}\right)=32.045 \mathrm{in}^{2}
$$

Estimated flange thickness:

$$
t_{f}:=\operatorname{if}\left\{t_{f}=0 \cdot i n, \frac{\left(\frac{8 \cdot b_{f}}{5}+\frac{d}{2}\right)-\sqrt{\left(\frac{8 \cdot b_{f}}{5}+\frac{d}{2}\right)^{2}-\frac{16}{5} \cdot\left(A-A_{o}\right)}}{2}, t_{f}\right)=0.86 \mathrm{in}
$$

Estimated web thickness:

$$
t_{w}:=\text { if }\left(t_{w}=0 \text { in }, \frac{5}{8} \cdot t_{f}, t_{w}\right) \quad t_{w}=0.525 \text { in }
$$

Estimated section weight if the entered flange thickness is 0 inches, or the actual section weight entered:

$$
W:=\text { if }\left(W=0 \cdot \frac{l b}{f t}, A \cdot 3.4 \cdot \frac{l b}{f t \cdot i n^{2}}, W\right) \quad W=109 \frac{l b}{f t}
$$

Moment of inertia about the X axis:

$$
I_{x}:=\frac{b_{f} \cdot t_{f} \cdot\left(d-t_{f}\right)^{2}}{2}+\frac{t_{w} \cdot\left(d-2 \cdot t_{f}\right)^{3}}{12}+\frac{b_{f} \cdot t_{f}{ }^{3}}{6}+I_{o}+A_{o} \cdot\left(\frac{d}{2}-t_{f}-z\right)^{2} \quad I_{x}=1238.6 \mathrm{in}^{4}
$$

Section modulus about the X axis:

$$
S_{x}:=\frac{2 \cdot I_{x}}{d} \quad S_{x}=173 \mathrm{in}^{3}
$$

Radius of gyration about the X axis:

$$
r_{x}:=\sqrt{\frac{I_{x}}{A}} \quad r_{x}=6.22 \mathrm{in}
$$

Moment of inertia about the Y axis:

$$
I_{y}:=\frac{t_{f} \cdot b_{f}{ }^{3}}{6}+\frac{\left(d-2 \cdot t_{f}\right) \cdot t_{w}{ }^{3}}{12}+I_{o}+A_{o} \cdot\left(\frac{t_{w}}{2}+z\right)^{2}=446.733 \mathrm{in}^{4}
$$

Section modulus about the Y axis:

$$
S_{y}:=\frac{2 \cdot I_{y}}{b_{f}} \quad S_{y}=61.18 \mathrm{in}^{3}
$$

Radius of gyration about the Y axis:

$$
r_{y}:=\sqrt{\frac{I_{y}}{A}} \quad r_{y}=3.73 \text { in }
$$

Area of one flange and the ratio of section depth to the area of the compression flange:

$$
A_{f}:=b_{f} \cdot t_{f} \quad A_{f}=12.56 \mathrm{in}^{2} \quad \frac{d}{A_{f}}=1.14 \mathrm{in}^{-1}
$$

Radius of gyration of a T-section comprised of the compression flange plus $1 / 3$ of the compression web area:

$$
\begin{aligned}
& r_{T}:=\sqrt{\frac{\frac{1}{12} \cdot t_{f} \cdot b_{f}{ }^{3}+\frac{1}{12} \cdot \frac{d-2 \cdot t_{f}}{6} \cdot t_{w}{ }^{3}+\frac{1}{2} \cdot\left(I_{o}+A_{o} \cdot\left(\frac{t_{w}}{2}+z\right)^{2}\right)}{b_{f} \cdot t_{f}+\frac{d-2 \cdot t_{f}}{6} \cdot t_{w}+\frac{A_{o}}{2}}} \\
& r_{T}=4.02 \mathrm{in}
\end{aligned}
$$

## Axial and Bending Stresses

Axial stress:

$$
f_{a}:=\frac{P}{A} \quad f_{a}=6.2 \mathrm{ksi}
$$

Bending stress due to moment about the X axis at the upper end of the column:

$$
f_{b_{\_} x u}:=\frac{M_{x u}}{S_{x}} \quad f_{b_{-} x u}=8.3 \mathrm{ksi}
$$

Bending stress due to moment about the X axis at the lower end of the column:

$$
f_{b_{-} x l}:=\frac{M_{x l}}{S_{x}} \quad f_{b_{-} x l}=-8.3 k s i
$$

Bending stress due to moment about the Y axis at the upper end of the column:

$$
f_{b \_y u}:=\frac{M_{y u}}{S_{y}} \quad f_{b_{-} y u}=7.8 \mathrm{ksi}
$$

Bending stress due to moment about the Y axis at the lower end of the column:

$$
f_{b \_y l}:=\frac{M_{y l}}{S_{y}} \quad f_{b \_y l}=-7.8 k s i
$$

Slenderness ratios about the X and Y axes:

$$
\frac{K_{x} \cdot L}{r_{x}}=22.2 \quad \frac{K_{y} \cdot L}{r_{y}}=37
$$

Larger slenderness ratio:

$$
S R:=\text { if }\left(\frac{K_{x} \cdot L}{r_{x}}>\frac{K_{y} \cdot L}{r_{y}}, \frac{K_{x} \cdot L}{r_{x}}, \frac{K_{y} \cdot L}{r_{y}}\right) \quad S R=37
$$

If SR is $>200$ a larger section or bracing is required.
Modulus of elasticity of steel:

$$
E:=29000 k s i
$$

Column slenderness ratio separating elastic and inelastic buckling (AISC Specification, Eq. (E2-1)):

$$
C_{c}:=\sqrt{\frac{2 \cdot \pi^{2} \cdot E}{F_{y}}}=126.099
$$

Allowable axial stress (AISC Specification, Eqs. (E2-1) and (E2-2)) combined with SR substituted for $\mathrm{Kl} / \mathrm{r}$ :

$$
\begin{aligned}
& F_{a}:=\text { if }\left\{\left(\left(S R>C_{c}\right) \cdot(S R \leq 200)\right), \frac{12 \pi^{2} \cdot E}{23 S R^{2}}, \text { if }\left\{S R>200,0 k s i, \frac{\left(1-\frac{S R^{2}}{2 \cdot C_{c}^{2}}\right) \cdot F_{y}}{\frac{5}{3}+\frac{3 S R}{8 C_{c}}-\frac{S R^{3}}{8 \cdot C_{c}^{3}}}\right)|\mid\right. \\
& F_{a}=19.4 \mathrm{ksi}
\end{aligned}
$$

Ratio of the smaller end moment $\mathrm{Mxa}^{\text {a }}$, to the larger end moment Mxb about the X axis:

$$
\begin{aligned}
& M_{x a}:=\operatorname{if}\left(\left|M_{x u}\right|<\left|M_{x l}\right|, M_{x u}, M_{x l}\right) \\
& M_{x b}:=\operatorname{if}\left(M_{x a}=M_{x u}, M_{x l}, M_{x u}\right)
\end{aligned}
$$

$$
\frac{M_{x a}}{M_{x b}}=-1
$$

Ratio of the smaller end moment Mya, to the larger end moment Myb about the Y axis:

$$
\begin{aligned}
& M_{y a}:=\mathrm{if}\left(\left|M_{y u}\right|<\left|M_{y l}\right|, M_{y u}, M_{y l}\right) \\
& M_{y b}:=\text { if }\left(M_{y a}=M_{y u}, M_{y l}, M_{y u}\right) \\
& \frac{M_{y a}}{M_{y b}}=-1
\end{aligned}
$$

Moment modifier factor Cb (AISC Specification, Sect. F1-3):

$$
\begin{aligned}
& C_{b}:=1.75+1.05 \cdot \frac{M_{x a}}{M_{x b}}+0.3 \cdot\left(\frac{M_{x a}}{M_{x b}}\right)^{2} \\
& C_{b}:=\text { if }\left(\left(X_{-} S w a y=0\right) \cdot\left(f_{a}>0 \cdot k s i\right), 1.0, \text { if }\left(C_{b}<2.3, C_{b}, 2.3\right)\right) \\
& C_{b}=1
\end{aligned}
$$

When the ends of the member are braced to prevent sidesway in the X direction and the axial stress is greater than 0 ksi , then Cb equals 1.0.

## Compact Section Criteria

Limiting ratio of one-half the flange width to the flange thickness for compact shapes (AISC Specification, Table B5.1):

$$
F R:=\frac{65}{\sqrt{\frac{F_{y}}{k s i}}}
$$

$$
F R=10.833
$$

Limiting ratio of one-half the flange width to the flange thickness for non-compact shapes (AISC Specification, Table B5.1):

$$
F R_{\max }:=\frac{95}{\sqrt{\frac{F_{y}}{k s i}}} \quad F R_{\max }=15.833
$$

Section depth to web thickness ratio for webs in compression or combined flexural and axial compression for compact sections (AISC Specification, Table B5.1) modified by expressing
the limiting ratio as a function of fa:

$$
W R\left(f_{a}\right):=\text { if }\left(\frac{f_{a}}{F_{y}} \leq 0.16, \frac{640}{\sqrt{\frac{F_{y}}{k s i}}} \cdot\left(1-3.74 \cdot \frac{f_{a}}{F_{y}}\right), \frac{257}{\sqrt{\frac{F_{y}}{k s i}}}\right)
$$

Actual ratios of one-half the flange width to flange thickness and section depth to web thickness, and the limiting ratios for a compact flange FR, a compact web WR(fa), and the maximum permissible flange ratio for a non-compact section FRmax:

$$
\begin{array}{lll}
\frac{b_{f}}{2 \cdot t_{f}}=8.5 & F R=10.8 & F R_{\max }=15.8 \\
\frac{d}{t_{w}}=27.3 & W R\left(f_{a}\right)=42.8 &
\end{array}
$$

Variable CF defined to test for compact section criteria. If both the web and flange are compact, $\mathrm{CF}=2$; if the flange is non-compact and the web is compact, $\mathrm{CF}=1$; and if the web is non-compact and the flange is either compact or non-compact, $\mathrm{CF}=0$.:

$$
C F:=\text { if }\left(\left(\frac{b_{f}}{2 \cdot t_{f}} \leq F R\right) \cdot\left(\frac{d}{t_{w}} \leq W R\left(f_{a}\right)\right), 2, \text { if }\left(\left(\frac{b_{f}}{2 \cdot t_{f}} \geq F R\right) \cdot\left(\frac{d}{t_{w}} \leq W R\left(f_{a}\right)\right), 1,0\right)\right)
$$

$$
C F=2
$$

Lateral bracing lengths, Lu and Lc (AISC Specifications, Eq. (F1-2)):

$$
\begin{aligned}
& L_{u}:=\frac{20000}{\frac{d}{b_{f} \cdot t_{f}} \cdot \frac{F_{y}}{k s i}}=40.607 \mathrm{ft} \\
& L_{c 1}:=\frac{76 \cdot b_{f}}{\sqrt{\frac{F_{y}}{k s i}}}=15.416 \mathrm{ft} \\
& L_{c}:=\text { if }\left(L_{c 1}<L_{u}, L_{c 1}, L_{u}\right)=15.416 \mathrm{ft}
\end{aligned}
$$

Allowable bending stress for adequately braced, compact and non-compact sections (AISC Specifications, Eqs. (F1-1), (F1-2), (F1-3) and (F1-5), combined):
$F 1^{\prime}:=F_{y} \cdot\left(0.79-0.002 \cdot \mathrm{if}\left(\frac{b_{f}}{2 \cdot t_{f}}<F R, F R, \frac{b_{f}}{2 \cdot t_{f}}\right) \cdot \sqrt{\frac{F_{y}}{k s i}}\right)$
$F 1^{\prime}=23.8 k s i$
$F 1:=\operatorname{if}\left(\left\langle L \leq L_{c}\right) \cdot(C F=2), 0.66 \cdot F_{y}\right.$, if $\left(\left\langle L \leq L_{c}\right) \cdot(C F=1), F 1^{\prime}\right.$, if $\left.\left.\left(\left(L \leq L_{c}\right) \cdot(C F=0), 0.60 \cdot F_{y}, 0 \cdot k s i\right)\right\rangle\right)$
$F 1=23.8 k s i$

If F1 $=0 \mathrm{ksi}$, the allowable bending stress is controlled by AISC Specification Eqs. (F1-6), (F1-7) or (F1-8).

Allowable bending stress for compact and non-compact sections with unbraced lengths greater than Lc (AISC Specification, Eqs. (F1-6) and (F1-7) combined):

$$
\begin{aligned}
& \frac{L}{r_{T}}=34.3 \\
& R_{1}:=\sqrt{\frac{102 \cdot 10^{3} \cdot C_{b} \cdot k s i}{F_{y}}} \quad R_{1}=53.2 \\
& R_{2}:=\sqrt{\frac{510 \cdot 10^{3} \cdot C_{b} \cdot k s i}{F_{y}}} \quad R_{2}=119 \\
& F 2^{\prime}:=\| \text { if }\left(\frac{L}{r_{T}} \geq R_{1}\right) \wedge\left(\frac{L}{r_{T}} \leq R_{2}\right) \quad=0 k s i \\
& F 2:=\operatorname{if}\left(F 2^{\prime}>0.60 \cdot F_{y}, 0.60 \cdot F_{y}, F 2^{\prime}\right) \quad F 2=0 \mathrm{ksi}
\end{aligned}
$$

AISC Specification, Eq. (F1-8):

$$
\begin{aligned}
& F 3:=\text { if }\left(\frac{12 \cdot 10^{3} \cdot C_{b} \cdot k s i}{\frac{L \cdot d}{A_{f}}}>0.60 \cdot F_{y}, 0.60 \cdot F_{y}, \frac{12 \cdot 10^{3} \cdot C_{b} \cdot k s i}{\frac{L \cdot d}{A_{f}}}\right) \\
& F 3=21.6 \mathrm{ksi}
\end{aligned}
$$

Allowable bending stress equal to the largest value of F1, F2 or F3:

$$
F_{b x}:=\operatorname{if}(F 1>0 \cdot k s i, F 1, \text { if }(F 2>F 3, F 2, F 3)) \quad F_{b x}=23.8 \mathrm{ksi}
$$

Allowable bending stress for bending about the Y axis for compact or non-compact sections (AISC Specification, Identity (F2-2) and Eq. (F2-3) combined) and with maximum flange ratio for a compact section substituted for the actual ratio if it is larger:

$$
\begin{aligned}
& F_{b y}:=F_{y} \cdot\left(1.075-0.005 \cdot\left(\text { if }\left(\frac{b_{f}}{2 \cdot t_{f}}>F R, \frac{b_{f}}{2 \cdot t_{f}}, F R\right) \cdot \sqrt{\frac{F_{y}}{k s i}}\right)\right) \\
& F_{b y}=27 \mathrm{ksi}
\end{aligned}
$$

Fby ranges from a lower limit of 0.60 Fy to an upper limit of 0.75 Fy .

Euler's stress for the X and Y directions, divided by a factor or safety and using the actual unbraced length and corresponding radius of gyration in the plain of bending (AISC Specification, Sect. H-1):

$$
\begin{array}{ll}
F_{e x}^{\prime}:= & \frac{12 \cdot \pi^{2} \cdot E}{23 \cdot\left(\frac{K_{x} \cdot L}{r_{x}}\right)^{2}}
\end{array} \quad F_{e x}^{\prime}=303.1 \mathrm{ksi}
$$

Moment modifier coefficients Cmx and Cmy (AISC Specification, Sect. H-1):

$$
\begin{aligned}
& C_{m x}:=\text { if }\left(X_{-} \text {Sway }=0,0.6-0.4 \cdot\left(\frac{M_{x a}}{M_{x b}}\right), 0.85\right)=1 \\
& C_{m y}:=\text { if }\left(Y \_S w a y=0,0.6-0.4 \cdot\left(\frac{M_{y a}}{M_{y b}}\right), 0.85\right)=1
\end{aligned}
$$

AISC Specification, Eqs. (H1-1) and (H1-2) for combined axial compression and bending, expressed as functions of bending stresses about the X and Y axes:

$$
H 1 \_1\left(f_{b x}, f_{b y}\right):=\frac{f_{a}}{F_{a}}+\frac{C_{m x} \cdot f_{b x}}{\left(1-\frac{f_{a}}{F_{e x}^{\prime}}\right) \cdot F_{b x}}+\frac{C_{m y} \cdot f_{b y}}{\left(1-\frac{f_{a}}{F_{e y}^{\prime}}\right) \cdot F_{b y}}
$$

$$
H 1 \_2\left(f_{b x}, f_{b y}\right):=\frac{f_{a}}{0.60 \cdot F_{y}}+\frac{f_{b x}}{F_{b x}}+\frac{f_{b y}}{F_{b y}}
$$

At upper end of column:

$$
\begin{aligned}
& H 1 \_1\left(\left|f_{b_{-} x u}\right|,\left|f_{b_{\_} y u}\right|\right)=0.987 \\
& H 1 \_2\left(\left|f_{b_{-} x u}\right|,\left|f_{b_{\_} y u}\right|\right)=0.93
\end{aligned}
$$

At lower end of column:

$$
\begin{aligned}
& H 1 \_1\left(\left|f_{b_{-} x}\right|,\left|f_{b \_y l}\right|\right)=0.987 \\
& H 1 \_2\left(\left|f_{b_{-} x}\right|,\left|f_{b_{\_} y l}\right|\right)=0.93
\end{aligned}
$$

Maximum value of H1_1 or H1_2:

$$
\begin{aligned}
& H E Q:=\left[\begin{array}{ll}
H 1 \_1\left(f_{b_{-} x u}, f_{b_{-} y u}\right) & H 1 \_1\left(f_{b_{-x l}}, f_{b_{-y}}\right) \\
H 1 \_2\left(f_{b_{-} x u}, f_{b_{-} y u}\right) & H 1 \_2\left(f_{b_{-} x l}, f_{b_{-} l}\right)
\end{array}\right] \\
& \max (H E Q)=0.987
\end{aligned}
$$

If the maximum value of interaction equations $\mathrm{H} 1 \_1$ or $\mathrm{H} 1 \_2$ is less than or equal 1.0 the section is adequate If the section is too small or too large, a new trial section may be entered.

## Summary

## Enter section designation: W14x109

## Input

Yield strength of steel:

$$
F_{y}=36 \mathrm{ksi}
$$

Column axial load:
$P=200$ kip

Unbraced column length:
$L=11.5 \mathrm{ft}$

End moment about the X axis, at the upper end of the column:

End moment about the X axis, at the lower end of the column:

End moment about the Y axis, at the upper end of the column:

End moment about the Y axis, at the lower end of the column:

Effective length factor relative to the X axis:

Effective length factor relative to the Y axis:

Variable "X_Sway" defined as 0 if sidesway is prevented, and 1 if sidesway is permitted:

Variable "Y_Sway" defined as 0 if sidesway is prevented, and 1 if sidesway is permitted:
$Y_{\_} S w a y=0$
$M_{x u}=120 \mathrm{kip} \cdot \mathrm{ft}$
$M_{x l}=-120 \mathrm{kip} \cdot f t$
$M_{y u}=40 \mathrm{kip} \cdot \mathrm{ft}$
$M_{y l}=-40 \mathrm{kip} \cdot \mathrm{ft}$
$K_{x}=1$
$K_{y}=1$
$X \_S w a y=0$

## Section dimensions and weight entered:

Section depth:
Flange width:
Web thickness:
Flange thickness:
Section weight per unit length:

Maximum value of H1_1 or H1_2:

$$
d=14.32 \text { in }
$$

$$
b_{f}=14.605 \mathrm{in}
$$

$$
t_{w}=0.525 \mathrm{in}
$$

$t_{f}=0.86 i n$

$$
W=109 \frac{l b}{f t}
$$

$$
\max (H E Q)=0.987
$$

Note: If the maximum value of H1_1 or H1_2 is significantly larger than 1.0 a stronger section must be used.

Estimated trial weight for follow-up estimates, assuming no change in bf

$$
\max (H E Q) \cdot W=107.602 \frac{l b}{f t}
$$ or d :

$$
W=109 \frac{l b}{f t}
$$

## Intermediate Computed Values:

(Refer to document for definitions.)

$$
\begin{array}{lll}
A=32.045 \mathrm{in}^{2} & f_{a}=6.241 \mathrm{ksi} & F_{a}=19.428 \mathrm{ksi} \\
I_{x}=\left(1.239 \cdot 10^{3}\right) \mathrm{in}^{4} & f_{b_{-} x u}=8.324 \mathrm{ksi} & F_{b x}=23.76 \mathrm{ksi} \\
r_{x}=6.217 \mathrm{in} & f_{b_{-} x l}=-8.324 \mathrm{ksi} & F_{e x}^{\prime}=303.088 \mathrm{ksi} \\
S_{x}=172.989 \mathrm{in}^{3} & f_{b_{-} y u}=7.846 \mathrm{ksi} & F_{b y}=27 \mathrm{ksi} \\
I_{y}=446.733 \mathrm{in}^{4} & f_{b_{-y l}}=-7.846 \mathrm{ksi} & F_{e y}^{\prime}=109.316 \mathrm{ksi} \\
r_{y}=3.734 \mathrm{in} & \frac{K_{x} \cdot L}{r_{x}}=22.197 & C_{c}=126.099 \\
S_{y}=61.175 \mathrm{in}^{3} & & C_{b}=1 \\
r_{T}=4.02 \mathrm{in} & \frac{K_{y} \cdot L}{r_{y}}=36.96 & C_{m x}=1 \\
\frac{d}{\Delta}=1.14 \mathrm{in}^{-1} & & C_{m y}=1
\end{array}
$$

$A_{f}$

$$
\begin{array}{lll}
L_{c}=15.416 \mathrm{ft} & \frac{b_{f}}{2 \cdot t_{f}}=8.491 & F R=10.833 \\
L_{u}=40.607 \mathrm{ft} & \frac{d}{t_{w}}=27.276 & F R_{\max }=15.833
\end{array}
$$

$W R\left(f_{a}\right)=42.833$
$C F=2$

