

Hexadecimal and binary conversions and functions

Hexadecimal or binary numbers are represented as strings, decimal numbers as numbers. The following functions work with unsigned integers only. The intention is to have a possibility to handle register values of microcontrollers or other integrated circuits.

```
hex2dec(Hex) := || HEXC ← "0123456789ABCDEF .hx"
|| len ← strlen(Hex)
|| Dec ← 0
|| j ← 0
|| idx ← 0
|| while idx < len
||   || digit ← substr(Hex, len - idx - 1, 1)
||   || cpos ← search(HEXC, digit, 0)
||   || if cpos < 0
||   ||   || error("wrong hex digit")
||   || if (cpos < 16)
||   ||   || Dec ← Dec + cpos • 16j
||   ||   || j ← j + 1
||   || idx ← idx + 1
|| return Dec
```

Hexadecimals have a prefix "0x" or a suffix "h". They consist of the digits 0..9,A..F and are case sensitive. It is allowed to insert blanks or dots to separate the digits. Maximum size is 49 bits $\sim 5.6 \cdot 10^{14}$. Bigger values will not be represented exactly.

$hex2dec("0x1234") = 4660$

$hex2dec("1234h") = 4660$

$hex2dec("12 34") = 4660$

$hex2dec("0AFFE DEADh") = 2952715949$

$hex2dec("0x1 FFFF FFFF FFFF") = 562949953421311$

$hex2dec("12.34") = 4660$

```
bin2dec(Bin) := || BINC ← "01 .b"
|| len ← strlen(Bin)
|| Dec ← 0
|| j ← 0
|| idx ← 0
|| while idx < len
||   || digit ← substr(Bin, len - idx - 1, 1)
||   || cpos ← search(BINC, digit, 0)
||   || if cpos < 0
||   ||   || error("wrong binary digit")
||   || if (cpos < 2)
||   ||   || Dec ← Dec + cpos • 2j
||   ||   || j ← j + 1
||   || idx ← idx + 1
|| return Dec
```

Binary numbers have a prefix "0b" or a suffix "b". They consist of the digits 0,1. It is allowed to insert blanks or dots to separate the digits. Maximum size is 49 bits $\sim 5.6 \cdot 10^{14}$. Bigger values will not be represented exactly.

$bin2dec("01110111010111b") = 7639$

$bin2dec("01 1101 1101 0111b") = 7639$

$hex2dec("1DD7") = 7639$

$bin2dec("0b 0001 1101 1101 0111") = 7639$

Conversion of a decimal to hexadecimal or binary:

```

dec2hex(Dec) := |HEXC ← "0123456789ABCDEF"
                  |j ← 0
                  |Hex ← "h"
                  |rem ← Dec - 16 · floor( $\frac{Dec}{16}$ )
                  |digit ← substr(HEXC, rem, 1)
                  |Hex ← concat(digit, Hex)
                  |j ← j + 1
                  |div ← floor( $\frac{Dec}{16}$ )
                  |while div > 0
                      ||rem ← div - 16 · floor( $\frac{div}{16}$ )
                      ||digit ← substr(HEXC, rem, 1)
                      ||Hex ← concat(digit, Hex)
                      ||j ← j + 1
                      ||div ← floor( $\frac{div}{16}$ )
                      ||if (j = 4) ∧ (div > 0)
                          |||Hex ← concat(" ", Hex)
                          |||j ← 0
                      ||
                  |
                  |if hex2dec(substr(Hex, 0, 1)) > 9
                  |||Hex ← concat("0", Hex)
                  |
                  |return Hex
  
```

$$dec2hex(2952715949) = "0AFFE DEADh"$$

$$dec2hex(257) = "101h"$$

```

dec2bin(Dec) := |BINC ← "01"
                  |j ← 0
                  |Bin ← "b"
                  |rem ← Dec - 2 · floor( $\frac{Dec}{2}$ )
                  |digit ← substr(BINC, rem, 1)
                  |Bin ← concat(digit, Bin)
                  |j ← j + 1
                  |div ← floor( $\frac{Dec}{2}$ )
                  |while div > 0
                      ||rem ← div - 2 · floor( $\frac{div}{2}$ )
                      ||digit ← substr(BINC, rem, 1)
                      ||Bin ← concat(digit, Bin)
                      ||j ← j + 1
                      ||div ← floor( $\frac{div}{2}$ )
                      ||if (j = 4) ∧ (div > 0)
                          |||Bin ← concat(" ", Bin)
                          |||j ← 0
                      ||
                  |
                  |return Bin
  
```

$$dec2bin(2952715949) = "1010 1111 1111 1110 1101 1110 1010 1101b"$$

$$dec2bin(257) = "1 0000 0001b"$$

Helper function to detect the base

```
base(x) := || if IsString(x)
    ||| lenx ← strlen(x)
    ||| if (substr(x, lenx - 1, 1) = "h") ∨ (substr(x, 1, 1) = "x")
    |||   ||| base ← 16
    ||| else if (substr(x, lenx - 1, 1) = "b") ∨ (substr(x, 1, 1) = "b")
    |||   ||| base ← 2
    ||| else
    |||   ||| error("wrong base")
    ||| else
    |||   ||| base ← 10
```

$$\text{base}("0x1234") = 16$$

$$\text{base}("1234h") = 16$$

$$\text{base}("0b0110101") = 2$$

$$\text{base}("0 1 2 3 4h") = 16$$

$$\text{base}(1234) = 10$$

bitfield extracts a sequence of bits from a starting position with a defined length. The result is a decimal

```
bitfield(x, start, len) := || bas ← base(x)
    || if bas = 16
    ||| dec ← hex2dec(x)
    ||| else if bas = 2
    |||| dec ← bin2dec(x)
    |||| else if bas = 10
    |||| | dec ← x
    |||| else
    |||| | error("Unknown base")
    ||| b1 ← 2start
    ||| tmp1 ← floor( $\frac{\text{dec}}{b1}$ )
    ||| b2 ← 2len
    ||| field ← tmp1 - b2 · floor( $\frac{\text{tmp1}}{b2}$ )
    ||| return field
```

$$\text{REGISTER} := \text{"AFFEDEADh"}$$

$$\text{bitfield}(\text{REGISTER}, 0, 8) = 173$$

$$\text{hex2dec}("AD") = 173$$

$$\text{REGISTER} := \text{"1010 1111 1111 1110 1101 1110 1010 1101b"}$$

$$\text{bitfield}(\text{REGISTER}, 0, 8) = 173$$

$$\text{REGISTER} := \text{"1 FFFF FFFF FFFFh"}$$

$$\text{hex2dec}(\text{REGISTER}) = 562949953421311$$

$$\text{base}(\text{REGISTER}) = 16$$

$$\text{bitfield}(\text{REGISTER}, 4, 8) = 234$$

$$\text{hex2dec}("EA") = 234$$

$$\text{base}(\text{REGISTER}) = 2$$

Logic functions with hexadecimal, decimal or binary parameters, the result is a binary. The size of the result is determined by the biggest size of the parameters.

```

AND(x,y) := || bas ← base(x)
              if bas = 16
                || binx ← dec2bin(hex2dec(x))
              else if bas = 2
                || binx ← dec2bin(bin2dec(x))
              else if bas = 10
                || binx ← dec2bin(x)
              else
                || error("Unknown base")

              bas ← base(y)
              if bas = 16
                || biny ← dec2bin(hex2dec(y))
              else if bas = 2
                || biny ← dec2bin(bin2dec(y))
              else if bas = 10
                || biny ← dec2bin(y)
              else
                || error("Unknown base")

              i ← strlen(binx) - 2
              j ← strlen(biny) - 2
              res ← "b"
              while (i ≥ 0) ∧ (j ≥ 0)
                || bx ← substr(binx, i, 1)
                || by ← substr(biny, j, 1)
                if bx ≠ ""
                  || bit ← str2num(bx) ∧ str2num(by)
                  || res ← concat(num2str(bit), res)
                else
                  || res ← concat("", res)
                i ← i - 1
                j ← j - 1
              return res
  
```

```

OR(x,y) := || bas ← base(x)
              if bas = 16
                || binx ← dec2bin(hex2dec(x))
              else if bas = 2
                || binx ← dec2bin(bin2dec(x))
              else if bas = 10
                || binx ← dec2bin(x)
              else
                || error("Unknown base")

              bas ← base(y)
              if bas = 16
                || biny ← dec2bin(hex2dec(y))
              else if bas = 2
                || biny ← dec2bin(bin2dec(y))
              else if bas = 10
                || biny ← dec2bin(y)
              else
                || error("Unknown base")

              i ← strlen(binx) - 2
              j ← strlen(biny) - 2
              res ← "b"
              while (i ≥ 0) ∨ (j ≥ 0)
                || bx ← if(i < 0, "0", substr(binx, i, 1))
                || by ← if(j < 0, "0", substr(biny, j, 1))
                if (bx ≠ "") ∧ (by ≠ "")
                  || bit ← str2num(bx) ∨ str2num(by)
                  || res ← concat(num2str(bit), res)
                else
                  || res ← concat("", res)
                i ← i - 1
                j ← j - 1
              return res
  
```

```

 $XOR(x, y) :=$ 
   $bas \leftarrow base(x)$ 
  if  $bas = 16$ 
     $\parallel binx \leftarrow dec2bin(hex2dec(x))$ 
  else if  $bas = 2$ 
     $\parallel binx \leftarrow dec2bin(bin2dec(x))$ 
  else if  $bas = 10$ 
     $\parallel binx \leftarrow dec2bin(x)$ 
  else
     $\parallel error("Unknown base")$ 
   $bas \leftarrow base(y)$ 
  if  $bas = 16$ 
     $\parallel biny \leftarrow dec2bin(hex2dec(y))$ 
  else if  $bas = 2$ 
     $\parallel biny \leftarrow dec2bin(bin2dec(y))$ 
  else if  $bas = 10$ 
     $\parallel biny \leftarrow dec2bin(y)$ 
  else
     $\parallel error("Unknown base")$ 
   $i \leftarrow strlen(binx) - 2$ 
   $j \leftarrow strlen(biny) - 2$ 
   $res \leftarrow "b"$ 
  while  $(i \geq 0) \vee (j \geq 0)$ 
     $\parallel bx \leftarrow if(i < 0, "0", substr(binx, i, 1))$ 
     $\parallel by \leftarrow if(j < 0, "0", substr(biny, j, 1))$ 
    if  $(bx \neq "") \wedge (by \neq "")$ 
       $\parallel\parallel bit \leftarrow str2num(bx) \oplus str2num(by)$ 
       $\parallel\parallel res \leftarrow concat(num2str(bit), res)$ 
    else
       $\parallel\parallel res \leftarrow concat(" ", res)$ 
     $i \leftarrow i - 1$ 
     $j \leftarrow j - 1$ 
  return  $res$ 

```

```

 $NOT(x) :=$ 
   $bas \leftarrow base(x)$ 
  if  $bas = 16$ 
     $\parallel binx \leftarrow dec2bin(hex2dec(x))$ 
  else if  $bas = 2$ 
     $\parallel binx \leftarrow dec2bin(bin2dec(x))$ 
  else if  $bas = 10$ 
     $\parallel binx \leftarrow dec2bin(x)$ 
  else
     $\parallel error("Unknown base")$ 
   $i \leftarrow strlen(binx) - 2$ 
   $res \leftarrow "b"$ 
  while  $(i \geq 0)$ 
     $\parallel bx \leftarrow substr(binx, i, 1)$ 
    if  $bx \neq "$ 
       $\parallel\parallel bit \leftarrow str2num(bx) \oplus 1$ 
       $\parallel\parallel res \leftarrow concat(num2str(bit), res)$ 
    else
       $\parallel\parallel res \leftarrow concat(" ", res)$ 
     $i \leftarrow i - 1$ 
  return  $res$ 

```

$ID(x, y) := y$ helper function for set_bitfield

$$XOR("1011\ 0100b", "0xFF") = "0100\ 1011b"$$

$$NOT("1011\ 0100b") = "0100\ 1011b"$$

$$AND("0b101", 15) = "101b"$$

$$AND(5, "1111b") = "101b"$$

$$OR(5, 2) = "111b"$$

$$OR("0xA5", "0b0101\ 1010") = "1111\ 1111b"$$

Shift shifts the binary representation of the parameter left (pos > 0) or right (pos < 0), filling up with zeroes. The result is an integer:

```
SHIFT(x, pos) := || bas ← base(x)
                  || if bas = 16
                  ||| dec ← hex2dec(x)
                  ||| else if bas = 2
                  |||| dec ← bin2dec(x)
                  ||| else if bas = 10
                  |||| dec ← x
                  ||| else
                  |||| error("Unknown base")
                  ||| dec ← floor(dec • 2pos)
```

$$dec2bin(SHIFT("0101\ 0010b", 2)) = "1\ 0100\ 1000b"$$

$$dec2bin(SHIFT("0101\ 0010b", 0)) = "101\ 0010b"$$

$$dec2bin(SHIFT("0101\ 0010b", -1)) = "10\ 1001b"$$

$$dec2bin(SHIFT("0101\ 0010b", -2)) = "1\ 0100b"$$

set_bitfield inserts a bitfield at a start position with defined length into a value using a function like AND, OR or XOR. This allows to set, reset or invert individual bits. The function ID allows to completely replace the bitfield.

```
set_bitfield(reg, bitf, start, len, func) := || mask ← hex2dec("1 FFFF FFFF FFFFh")
                                              || mask ← mask - (2len - 1) • 2start
                                              || res ← AND(reg, mask)
                                              || regfield ← bitfield(reg, start, len)
                                              || regfield ← func(regfield, bitf)
                                              || regfield ← SHIFT(regfield, start)
                                              || res ← OR(res, regfield)
```

$$REGISTER := "1010\ 1101b"$$

$$set_bitfield(REGISTER, "111b", 2, 3, XOR) = "1011\ 0001b"$$

invert bits 2,3,4

$$set_bitfield(REGISTER, "110b", 2, 3, ID) = "1011\ 1001b"$$

replace bits 2-4

$$set_bitfield(REGISTER, "0b", 5, 1, AND) = "1000\ 1101b"$$

clear bit 5

$$set_bitfield(REGISTER, "1b", 6, 1, OR) = "1110\ 1101b"$$

set bit 6

clear(REGISTER)