

Top Rail Calculations

Material Info: Steel Pipe ASTM A53 $F_y := 35 \cdot \text{ksi}$ $F_u := 60 \cdot \text{ksi}$ $E := 29000 \cdot \text{ksi}$

$r_{rail_info} = ?$

Max Span = $L := 4 \text{ ft}$

Load Requirements:
 Uniform Load = $w := 50 \text{ plf}$
 Concentrated = $P := 200 \text{ lb}$

Load requirements based on ASCE 7-10 section 4.5.1

Uniform Loading

Concentrated Loading

$V_0 := P = 200 \text{ lb}$

$V_1 := \frac{w \cdot L}{2} = 100 \text{ lb}$

$V_2 := \frac{P}{2} = 100 \text{ lb}$

$M_1 := \frac{w \cdot L^2}{8} = 100 \text{ lb} \cdot \text{ft}$

$M_2 := \frac{P \cdot L}{4} = 200 \text{ lb} \cdot \text{ft}$

$\Delta_1 := \frac{5 \cdot w \cdot L^4}{384 \cdot E \cdot r_{rail}} = ? \text{ in}$

$\Delta_2 := \frac{P \cdot L^3}{48 \cdot E \cdot r_{rail}} = ? \text{ in}$

Deflection, Moment, and Shear is based on Table 3-23
 Uniform Loading based on Case 1
 Concentrated Loading based on Case 7&8
 Vo based on point load at support

Moment of inertia if the rail is $r_{rail} = ? \text{ in}^4$

$V_{max} = 200 \text{ lb}$

$M_{max} = 200 \text{ lb} \cdot \text{ft}$

$\Delta_{max} = ? \text{ in}$

Check member for shear:
 Spec. Chapter G, section G6

$F_{cr1} := \frac{1.6 \cdot E}{\left(\frac{L_v}{\text{outdiameter}_{rail}} \right)^4 \cdot \left(\frac{\text{outdiameter}_{rail}}{\text{thickness}_{rail}} \right)^5} = ? \frac{\text{lb}}{\text{in}^2}$

$L_v =$ distance from max shear to zero shear; $L_v := \frac{L}{2} = 2 \text{ ft}$

$F_{cr2} := \frac{0.78 \cdot E}{\left(\frac{\text{outdiameter}_{rail}}{\text{thickness}_{rail}} \right)^3} = ? \frac{\text{lb}}{\text{in}^2}$

Fcr shall be the larger of Fcr1 and Fcr2 but
 shall not exceed $0.6 \cdot F_y = 21000 \frac{\text{lb}}{\text{in}^2}$

$F_{cr} = ? \frac{\text{lb}}{\text{in}^2}$

$V_n := \frac{F_{cr} \cdot \text{area}_{rail}}{2} = ?$

$V_n \geq 1.6 \cdot V_{max} = ?$

V_n is greater then or equal to $1.6 \cdot V_{max}$ therefor Pipe 1-1/4STD is ok in shear.

Check member in flexure:
 Spec. Chapter F, section F8

$\frac{\text{outdiameter}_{rail}}{\text{thickness}_{rail}} < \frac{0.45 \cdot E}{F_y} = ?$

Ratio shall be 1 for section to apply

$\frac{\text{outdiameter}_{rail}}{\text{thickness}_{rail}} < \frac{0.07 \cdot E}{F_y} = ?$

If 1 compact; If 0 refer below

$\frac{\text{outdiameter}_{rail}}{\text{thickness}_{rail}} < \frac{0.31 \cdot E}{F_y} = ?$

If above is 1 ignore. If above is 0 then
 1=noncompact, 0=slender

$M_p := F_y \cdot Z_{rail} = ?$

Since member is compact Local Buckling does not apply

$M_{allow_0} := M_p = ?$

$M_{allow_0} \geq 1.6 \cdot M_{max} = ?$

Mallow is greater then or equal to $1.6 \cdot M_{max}$ therefor Pipe 1-1/4STD is ok in flexure.